

# PREPARATORY PROBLEMS 

AND

## WORKED SOLUTIONS

Melbourne, Australia July 5 - 14, 1998

## A Note to Mentors

During the 29th International Chemistry Olympiad in Montreal, the International Jury resolved to reduce the number of preparatory theoretical problems from about 50 (that had been common practice in recent years) to 25 . We have achieved that aim (almost we have 26 theory problems but as you will see, Problem 26 is more of a study guide) and have taken pains to ensure that the exercises cover the Level 3 areas that will be represented in the 30th IChO examinations in Melbourne. For your convenience, we have included the list of topics that are generally accepted as the basis for examination questions for the International Chemistry Olympiad - this is the same list of topics that we inherited from Montreal.

More importantly, the problems have been designed to challenge and stimulate the interests of the best pre-university chemistry students in your country! We have also provided detailed worked answers for each problem and hope that your students will learn a considerable amount of chemistry from these worked solutions without your continual assistance.

This year we have 4 detailed preparatory laboratory exercises that cover the skills that your students need to show in Melbourne. We have tried to highlight the procedures in each exercise that need some particular caution, even for students of Olympiad level but our warnings cannot be comprehensive - your students will still need your careful supervision. We have also not included specific details for handling or disposal of the products of these lab exercises, as these will vary greatly from country to country, but we know that you will employ best-practice to responsibly dispose or recycle the materials that your students use and produce. Students should of course also make themselves aware of any hazards associated with the chemicals that they will be using in any exercise and we encourage you to bring these to their attention.

For our junior colleagues who will spend many hours over the coming months thinking about these exercises, we will provide an opportunity to discuss these exercises (and other matters) with their fellow students from all over the world, even before they come together in Melbourne. We have set up a web-based chat forum so that they can get to know one another (after all - isn't that one of the main reasons for the Olympiads?) and we encourage you to bring the chat forum to their attention and indeed, enter into the discussion yourselves.

Finally, despite the valiant proof-reading efforts of my colleagues, it would be surprising if you don't uncover a bug or two still lurking here. Such deficiencies are of course my responsibility, so please don't hesitate to bring them to my attention. Corrections will be regularly sent by email to each delegation and published on the web page whose address is given below. Corrected copies of this document in several formats will also be available for downloading from the web page.
Good luck in your preparations, and we look forward to meeting you in Melbourne.

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## Scientific Jury of the 30th International Chemistry Olympiad

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## Draft Syllabus for the International Chemistry Olympiad

## Classification of the chemical topics

Group 1: These topics are included in the overwhelming majority of secondary school chemistry programs.
Group 2: These topics are included in a substantial number of secondary school programs; however, if not covered, it would be expected that the Olympiad level students from every country would have been introduced to these topics.
Group 3: These topics are not included in the majority of secondary school programs.
For a host nation it is no longer necessary to have preparatory problems on Group 1 and Group 2 topics, although, in the latter case, a listing of the specific topics of that Group which might be part of the Olympiad Examination is to be given by the host nation. Any topics in Group 3 which might appear on the Olympiad Examination must be covered in the preparatory problems.

## INORGANIC CHEMISTRY

## ELECTRONIC CONFIGURATION

| 1 | main groups |
| :--- | :--- |
| 2 | transition metals |
| 3 | lanthanide and actinide metals |
| 4 | Pauli exclusion Principle |
| 5 | Hund's Rule |
| TRENDS IN THE PERIODIC |  |
| TABLE (MAIN GROUPS) |  |
| 6 | electronegativity |
| 7 | electron affinity |
| 8 | first ionization energy |
| 9 | atomic size |
| 10 | ionic size |
| 11 | highest oxidation number |
| TRENDS IN PHYSICAL |  |
| PROPERTIES (MAIN GROUPS) |  |

12 melting point 1
13 boiling point
1
14 metal character 1
15 magnetic properties 2
16 thermal properties 3

## STRUCTURES

17 metal structures 3
18 ionic crystal structures. Simple molecular structures with central atom
19 exceeding the octet rule 3

20 stereochemistry

## NOMENCLATURE

21 main group compounds ..... 1
22 transition metal compounds ..... 1
23 simple metal complexes ..... 2
24 multicenter metal complexes ..... 3
25 coordination number ..... 1
STOICHIOMETRY
26 balancing equations ..... 1
27 mass and volume relationships ..... 1
28 empirical formula ..... 1
29 Avogadro's number ..... 1
30 concentration calculations ..... 1
ISOTOPES
31 counting of nucleons ..... 1
32 radioactive decay ..... 1
33 nuclear reaction (alpha, beta, gamma, neutrino) ..... 2
NATURAL CYCLES
34 nitrogen ..... 2
35 oxygen ..... 2
36 carbon ..... 2
s-BLOCKproducts of reaction of group I and IImetals
37 with water, basicity of the products ..... 138 products of reaction of the metals withhalogens
$39 \begin{aligned} & \text { products of reaction of the metals with } \\ & \text { oxygen }\end{aligned}$
40 heavier elements are more reactive 1

## p-BLOCK

42 stoichiometry of simplest nonmetal hydrides
43 properties of metal hydrides 3
$44 \mathrm{acid} /$ base properties of $\mathrm{CH}_{4}, \mathrm{NH}_{3}, \mathrm{H}_{2} \mathrm{~S}$, $\mathrm{H}_{2} \mathrm{O}$, HX
45 NO reaction with $\mathrm{O}_{2}$ to form $\mathrm{NO}_{2}$
1
46 equilibrium between $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4} \quad 1$
47 products of reaction of $\mathrm{NO}_{2}$ with water 1
$48 \mathrm{HNO}_{2}$ and its salts are reductants 1
$49 \mathrm{HNO}_{3}$ and its salts are oxidants 1
$50 \mathrm{~N}_{2} \mathrm{H}_{4}$ is a liquid and reductant 3
51 there exists acids like $\mathrm{H}_{2} \mathrm{~N}_{2} \mathrm{O}_{2}, \mathrm{HN}_{3} \quad 3$
52 to remember, what are products of reduction of nitrates or $\mathrm{HNO}_{3}$ with different metals and reductors
53 reaction of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ with iodine 2
54 other thioacids polyacids, peroxoacids 3 B(III), Al(III), Si(IV), P(V) S(IV), S(VI), $\mathrm{O}(\mathrm{II}), \mathrm{F}(\mathrm{I}), \mathrm{Cl}(\mathrm{I}), \mathrm{Cl}(\mathrm{III}), \mathrm{Cl}(\mathrm{V})$ and Cl (VIII) are normal oxidation states of 2nd and 3rd row elements in compounds
55 with halogens and in oxoanions
56 compounds of nonmetals with other oxidation states
57 the preferred oxidation states are $\mathrm{Sn}(\mathrm{II})$, Pb (II), Bi(III)
58 products of reactions of nonmetal oxides with water and stoichiometry of resulting acids
59 reactions of halogens with water 2
60 reactivity and oxidizing power of halogens decrease from $\mathrm{F}_{2}$ to $\mathrm{I}_{2}$
61 differences of chemistry between row 4 and row 3 elements

## d-BLOCK

62 common oxidation states of the common d-block metals are $\mathrm{Cr}(\mathrm{III}), \mathrm{Cr}(\mathrm{VI}), \mathrm{Mn}(\mathrm{II})$, Mn (IV), Mn (VII), Fe (II), Fe (III), Co (II), $\mathrm{Ni}(\mathrm{II}), \mathrm{Cu}(\mathrm{I}), \mathrm{Cu}(\mathrm{II}), \mathrm{Ag}(\mathrm{I}), \mathrm{Zn}(\mathrm{II}), \mathrm{Hg}(\mathrm{I})$, Hg (II)
63 colors of the listed common ions in aqueous solution
64 other oxidation stales and chemistry of other d-block elements
$65 \mathrm{Cr}, \mathrm{Mn}, \mathrm{Fe}, \mathrm{Ni}, \mathrm{Co}, \mathrm{Zn}$ dissolve in dil HCI ;
$\mathrm{Cu}, \mathrm{Ag}, \mathrm{Hg}$ do not dissolve

41 Li combine with $\mathrm{H}_{2}$ and $\mathrm{N}_{2}$, forming LiH and $\mathrm{Li}_{3} \mathrm{~N}$

66 products of the dissolution are ( $2+$ ) cations 2
67 passivation of $\mathrm{Cr}, \mathrm{Fe}$ (and also Al ) 2 $\mathrm{Cr}(\mathrm{OH})_{3}$ and $\mathrm{Zn}(\mathrm{OH})_{2}$ are amphoteric, other common hydroxides are not
$68 \mathrm{MnO}_{4}^{-}, \mathrm{CrO}_{4}{ }^{2-}, \mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ are strong oxidants

69 products of reduction of $\mathrm{MnO}_{4}^{-}$ depending on pH
70 polyanions other than $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-} 3$
OTHER INORGANIC PROBLEMS
71 industrial production of $\mathrm{H}_{2} \mathrm{SO}_{4}, \mathrm{NH}_{3}$, $\mathrm{Na}_{2} \mathrm{CO}_{3}, \mathrm{Na}, \mathrm{Cl}_{2}, \mathrm{NaOH}$
72 chemistry of lanthanides and actinides 3
73 chemistry of noble gases

## ORGANIC CHEMISTRY

## ALKANES

74 isomers of butane 1
75 naming (IUPAC) 1
76 trends in physical properties 1
substitution (eg with $\mathrm{Cl}_{2}$ )
77 - products 1
78 - free radicals 2
79 - initiation/termination of the chain $\quad 2$
cycloalkanes
80 - names 1
81 - strain in small rings 2
82 - chair/boat conformation 2

## ALKENES

83 planarity 1
$84 \mathrm{E} / \mathrm{Z}$ (cis/trans) isomerism 1
85 addition of $\mathrm{Br}_{2}, \mathrm{HBr}$ - products 1
86 - Markovnikoff rule 2
87 - carbonium ions in addition reaction 3
88 - relative stability of carbonium ions 3
89 - 1,4-addition lo alkadiene 3

## ALKYNES

90 linear geometry 1
91 acidity 2

## ARENES

92 formula of benzene

| 93 | delocalization of electrons | 1 |
| :--- | :--- | :--- |
| 94 | stabilisation by resonance | 1 |
| 95 | Huckel (4n+2) rule | 3 |
| 96 | aromaticity of heterocycles | 3 |
| 97 | nomenclature (IUPAC) of heterocycles | 3 |
| 98 | polycyclic aromatic compound | 3 |
| 99 | effect of first substituent: - on reactivity | 2 |
| 100 | - on direction of substitution | 2 |
| 101 | explanation of substituent effects | 2 |
| HALOGEN COMPOUNDS |  |  |
| 102 hydrolysis reactions | 2 |  |
| 103 | exchange of halogens | 3 |
| 104 reactivity (primary vs secondary vs | 2 |  |
| $\quad$ tertiary) | 2 |  |
| 105 | ionic mechanism | 2 |
| 106 | side products (elimination) | 2 |
| 107 reactivity (aliphatic vs aromatic) | 2 |  |
| 108 Wurtz (RX + Na) reaction | 3 |  |
| 109 | halogen derivatives \& pollution | 3 |

## ALCOHOLS, PHENOLS

110 hydrogen bonding - alcohols vs ethers 1
111 acidity of alcohols vs phenols 2
112 dehydration to alkenes 1
113 dehydration to ethers 2
114 esters with inorganic acids 2
115 iodoform reaction 2
116 reactions of primary/sec./tert.:Lucas
reagent
117 formula of glycerin 1
CARBONYL COMPOUNDS
118 nomenclature 1
119 keto/enol tautomerism 2
120 preparation-oxidation of alcohols 1
121 - from carbon monoxide 3
122 reactions: - oxidation of aldehydes 1
123 - reduction with Zn metal 2
124 - addition of HCN 2
125 of $\mathrm{NaHSO}_{3} \quad 2$
126 of $\mathrm{NH}_{2} \mathrm{OH} \quad 2$
127 - aldol condensation 3
128 - Cannizzaro $\left(\mathrm{PhCH}_{2} 0 \mathrm{H}\right.$
disproportionation)
129 - Grignard reaction 2
130 - Fehling ( $\mathrm{Cu}_{2} \mathrm{O}$ ) and Tollens (Ag mirror) 2
CARBOXYLIC ACIDS
131 inductive effect and strength

132 equivalence of oxygen atoms in anions 2
133 preparation: - from esters 2
134 - from nitriles 2
134 products of reaction with alcohols (esters) 1
136 mechanism of esterification 2
137 isotopes in mechanism elucidation 3
138 nomenclature: acid halides 2
139 preparation of acid chlorides 2
140 amides from acid chlorides 2
141 nitriles from acid chlorides 3
142 properties \& preparation of anhydrides 2
143 oxalic acid: name and formula 1
144 multifunctional acids 2
145 optical activity (eg. lactic acid) 2
146 R/S nomenclature 3
147 plant vs animal fats - differences 2
NITROGEN COMPOUNDS
148 amines are basic 1
149 comparing aliphatic vs aromatic 2
$150 \begin{aligned} & \text { names: primary, secondary, tertiary, } \\ & \text { quaternary }\end{aligned}$
151 identification of primary/sec/tert/quatern. in lab.
preparation of amines
152 - from halogen compounds 2
153 - from nitro compounds $\left(\mathrm{PhNH}_{2}\right.$ from
$\left.\mathrm{PhNO}_{2}\right)$
154 - from amides (Hoffmann) 3
155 mechanism of Hoffmann $r$. in acidic/basic medium 3
156 basicity amines vs amides 2
diazotation products
157 - of aliphatic amines 3
158 - of aromatic amines 3
$159 \begin{aligned} & \text { dyes: color vs structure (chromophore } \\ & \text { groups) }\end{aligned}$
160 nitrocompounds: aci/nitro tautomerism 3
161 Beckmann (oxime - amide)
rearrangements

## SOME LARGE MOLECULES

162 hydrophilic/hydrophobic groups 2
163 micelle structure 3
164 preparation of soaps 1
products of polymerization of
165 - styrene 2
166 - ethene 1
167 - polyamides 3
168 - phenol + aldehydes 3
169 - polyurethanes 3

## 170 polymers - cross-linking <br> 171 - structures (isotactic etc) <br> 172 - chain mechanism of formation <br> 173 rubber composition <br> BIOCHEMISTRY <br> AMINO ACIDS AND PEPTIDES

174 ionic structure of aminoacids
175 isoelectric point
17620 aminoacids (classification in groups)
17720 aminoacids (all structures)
178 ninhydrin reaction (incl. equation)
179 separation by chromatography
180 separation by electrophoresis
181 peptide linkage

## PROTEINS

182 primary structure of proteins
183 -S-S- bridges
184 sequence analysis
185 secondary structures
186 details of alpha-helix structure
187 tertiary structure
188 denaturation by change of pH , temp., metals, EtOH
189 quaternary structure
190 separation of proteins (molecule size and solubility)
191 metabolism of proteins (general)
192 proteolysis
193 transamination
194 four pathways of catabolism of amino acids

195 decarboxylation of amino acids
196 urea cycle (only results)

## FATTY ACIDS AND FATS

197 IUPAC names from $\mathrm{C}_{4}$ to $\mathrm{C}_{18}$
200 beta-oxidation of fatty acids (formulas \& ATP balance) ..... 3
201 fatty acids \& fats anabolism ..... 3
202 phosphoglycerides ..... 3
203 membranes ..... 3
204 active transport ..... 3
ENZYMES
228 difference between ribose and
2-deoxyribose ..... 3
229 base combination CG and AT ..... 3
230 - "- (hydrogen bonding structures) ..... 3
231 difference between DNA and RNA ..... 3
232 difference between mRNA and tRNA ..... 3
233 hydrolysis of nucleic acids ..... 3
234 semiconservative replication of DNA ..... 3 ..... 3
235 DNA-ligase ..... 3
236 RNA synthesis (transcription) without details ..... 3
237 reverse transcriptase ..... 3
238 use of genetic code ..... 3
239 start and stop codons ..... 3
240 translation steps ..... 3
206 nomenclature, kinetics, coenzymes, function of ATP etc ..... 3
CARBOHYDRATES
207 glucose and fructose:chain formulas ..... 2
208 - Fischer projections ..... 2
209 - Haworth formulas ..... 3
210 osazones ..... 3
211 maltose as reducing sugar ..... 2
212 difference between starch \& cellulose ..... 2
213 difference between alpha- and beta-D glucose ..... 2
214 metabolism from starch to acetyl-CoA ..... 3
215 catabolism of glucose ..... 3
216 ATP balance for these pathways ..... 3
217 photosynthesis (products only) ..... 2
218 light and dark reaction ..... 3
219 detailed Calvin cycle ..... 3
KREBS CYCLE AND RESPIRATION CHAIN
220 formation of $\mathrm{CO}_{2}$ in the cycle (no details) ..... 3
221 intermediate compounds in the cycle ..... 3
222 formation of water and ATP (no details) ..... 3
223 FMN and cytochromes ..... 3
224 calculation of ATP amount for 1 mol glucose ..... 3
NUCLEIC ACIDS AND PROTEIN SYNTHESES
225 pyrimidine, purine ..... 2
226 nucleosides, nucleotides ..... 3
227 formulas of all pyrimidine and purine bases ..... 3333

205 general properties, active centres
2
OTHER BIOCHEMISTRY
241 hormones, regulation ..... 3
242 hormone feedback ..... 3
243 insulin, glucagon, adrenaline ..... 3
244 mineral metabolism (no details) ..... 3
245 ions in blood ..... 3
246 buffers in blood ..... 3
247 haemoglobin: function \& skeleton ..... 3
248 - diagram of oxygen absorption ..... 3
249 steps of clotting the blood ..... 3
250 antigens and antibodies ..... 3
251 blood groups ..... 3
252 acetyl choline structure and functions ..... 3

## INSTRUMENTAL METHODS OF DETERMINING STRUCTURE

## UV-VIS SPECTROSCOPY

253 identification of aromatic compound
254 identification of chromophore

## MASS SPECTRA

255 recognition of: - molecular ion
256 - fragments with a help of a table
257 - typical isotope distribution

## IR

258 interpretation using a table of group frequencies
259 recognition of hydrogen bonds 3
260 Raman spectroscopy

## NMR

261 interpret. of simple spectrum (like ethanol) 3
262 spin-spin coupling
263 coupling constants

264 identification of o - and p - substituted
benzene
$265{ }^{13} \mathrm{C}-\mathrm{NMR}$

## X-RAYS

266 Bragg law
267 electron density diagrams 3
268 coordination number 3
269 unit cell
structures of:
$270-\mathrm{NaCl}$
$271-\mathrm{CsCl}$
272 - close-packed (2 types)

273 determining of the Avogadro constant
from X-ray data

## POLARIMETRY

274 calculation of specific rotation angle 3

## PHYSICAL CHEMISTRY

CHEMICAL EQUILIBRIA
275 dynamical model of chemical equilibrium 1 chemical equilibrium expressed in terms of
276 - relative concentration 1
277 - relative partial pressures

278 the relationship between equilibrium
constant for

ideal gases expressed in different ways
(concentrations, pressures, mole fractions) 2
279 relation of equilibrium constant and standard Gibbs energy ..... 3
IONIC EQUILIBRIA
280 Arrhenius theory of acids and bases ..... 1
281 Broensted-Lowry theory, conjugated acids \& bases ..... 1
282 definition of pH ..... 1
283 ionic product of water ..... 1
284 relation between K , and Kb for conjugateacids \& bases1
285 hydrolysis of salts ..... 1
286 solubility product - definition ..... 1
287 calculation of solubility (in water) from solubility product ..... 1
288 calculation of pH for weak acid from $\mathrm{K}_{\mathrm{a}}$ ..... 1
289 calculation of pH for $10^{-7} \mathrm{~mol} / \mathrm{dm}^{3} \mathrm{HCI}$ ..... 2
290 calculation of pH for multiprotic acids ..... 2
291 definition of activity coefficient ..... 2
292 definition of ionic strength ..... 3
293 Debye-Hueckel formula ..... 3
ELECTRODE EQUILIBRIA
294 electromotive force (definition) ..... 1
295 first kind electrodes ..... 1
296 standard electrode potential ..... 1
297 Nernst equation ..... 2
298 second kind electrodes ..... 2
299 relation between $\Delta \mathrm{G}$ and electromotive force ..... 3
KINETICS OF HOMEGENOUS REACTION
300 factors influencing reaction rate ..... 1
301 rate equation ..... 1
302 rate constant ..... 1
303 order of reaction ..... 2
304 1st order reactions: time dependence of concentration ..... 2
305 - half life ..... 2
306 - relation between half-life and rate constant ..... 2
307 rate-determining step ..... 2
308 molecularity ..... 2
309 Arrhenius equation, activation energy (defin.) ..... 2
310 calculation of rate constant for $1^{\text {st }}$ orderreactions2
311 calculation of rate constant for 2,3 orderreactions3
312 calculation of activation energy from experimental. data ..... 3
313 basic concepts of collision theory ..... 3
314 basic concepts of transition state theory ..... 3
315 opposing, parallel and consecutive reactions ..... 3
THERMODYNAMICS
316 system and its surroundings ..... 2
317 energy, heat and work ..... 2
318 relation between enthalpy and energy ..... 2
319 heat capacity - definition ..... 2
320 difference between $\mathrm{C}_{\mathrm{p}}$ and $\mathrm{C}_{\mathrm{V}}$ ..... 3
321 Hess' law ..... 2
322 Born-Herbier cycle for ionic compounds ..... 3
323 lattice energies - approximate calculations (e.g.Kapustinski equation) ..... 3
324 use of standard formation enthalpies ..... 2
325 heats of solution and solvation ..... 2
326 bond energies - definition and uses ..... 2
SECOND LAW
327 Entropy - definition (q/T) ..... 2
328 entropy and disorder ..... 2
329 relation $\mathrm{S}=\mathrm{k} \ln \mathrm{W}$ ..... 3
330 relation $\mathrm{G}=\mathrm{H}-\mathrm{T} \mathrm{S}$ ..... 2
$331 \Delta \mathrm{G}$ and directionality of changes ..... 2
PHASE SYSTEMS
332 ideal gas law1
333 van der Waals gas law ..... 3
334 definition of partial pressure ..... 1
335 Temp. dependence of the vapour pressure of liquid ..... 2
336 Clausius-Clapeyron equation ..... 3
337 reading phase diagram: triple point ..... 3338 - critical temperature339 liquid-vapour system (diagram)3340 - ideal and nonideal systems3
341 - use in fractional distillation ..... 33
342 Henry's law ..... 2
343 Raoult's law ..... 2
344 deviations from Raoult's law ..... 3
345 Boiling point elevation law ..... 2
346 freezing-point depression, determination. of molar mass ..... 2
347 osmotic pressure ..... 2
348 partition coefficient ..... 3
349 solvent extraction ..... 2
350 basic principles of chromatography ..... 2
OTHER PROBLEMS
ANALYTICAL CHEMISTRY
351 using pipette ..... 1
352 using burette ..... 1
353 choice of indicators for acidimetry ..... 1
354 titration curve: pH (strong AND weak acid) ..... 2
355 - EMF (redox titration) ..... 2
356 calculation of pH of simple buffer solution 2357 identification of: $\mathrm{Ag}^{+}, \mathrm{Ba}^{2+}, \mathrm{Cl}^{-}, \mathrm{SO}_{4}{ }^{2-}$ions1
$358-$ of $\mathrm{Al}^{3+}, \mathrm{NO}_{2}{ }^{-}, \mathrm{NO}_{3}{ }^{-}, \mathrm{Bi}^{3+}$ ions ..... 2
359 - of $\mathrm{VO}_{3}^{-}, \mathrm{ClO}_{3}^{-}, \mathrm{Ti}^{4+}$ ions ..... 3
360 - using flame test for $\mathrm{K}, \mathrm{Ca}, \mathrm{Sr}$ ..... 1
361 Lambert-Beer-Law ..... 2
COMPLEXES
362 writing down complexation reactions ..... 1
363 complex formation constants (definition) ..... 2
$364 \mathrm{E}_{\mathrm{g}}$ and $\mathrm{T}_{2 \mathrm{~g}}$ terms: high and low spin octahedral c ..... 3
365 calculation of solubility of AgCl in $\mathrm{NH}_{3}$ (from $\mathrm{K}_{\mathrm{s}}$ and $\mathrm{B}^{\prime} \mathrm{s}$ ) ..... 3
366 cis and trans forms ..... 3
THEORETICAL CHEMISTRY
367 n , 1 , m quantum numbers ..... 2
368 energy levels of hydrogen atom (formula) ..... 2
369 shape of p-orbitals ..... 2
370 d orbital stereoconfiguration ..... 3
371 molecular orbital diagram: $\mathrm{H}_{2}$ molecule ..... 3
$372-\mathrm{N}_{2}$ or $\mathrm{O}_{2}$ molecule ..... 3
373 bond orders in $\mathrm{O}_{2}$ or $\mathrm{O}_{2}^{+}$or $\mathrm{O}_{2}^{-}$ ..... 3
374 Hueckel theory for aromatic compounds ..... 3
375 Lewis acids and bases ..... 2
376 hard and soft Lewis acids ..... 3
377 unpaired electrons and paramagnetism ..... 2
378 square of the wave function and probability ..... 3
379 understanding the simplest Schroedinger equation ..... 3

## PROBLEM 1.

Hydrocarbons with the empirical formula $(\mathrm{CH})_{\mathrm{n}}$ have a particular fascination for many chemists. Such compounds inevitably feature multiple C-C bonds and/or cyclization in order to achieve valence satisfaction of all atoms. Notable instances of $(\mathrm{CH})_{\mathrm{n}}$ hydrocarbons include:
$\mathrm{n}=2$ : acetylene (ethyne)
$\mathrm{n}=6$ : benzene
$\mathrm{n}=8$ : cubane

$\mathrm{n}=20$ : dodecahedrane


Focussing now on examples with $\mathrm{n}=4$, consider two such compounds: cyclobutadiene and butatriene.
a). Draw the structures of these two $\mathrm{C}_{4} \mathrm{H}_{4}$ isomers.
b). The central $\mathrm{C}=\mathrm{C}$ bond in butatriene is different in length to the other two $\mathrm{C}=\mathrm{C}$ bonds in this molecule. Why is this? (Hint: consider the hybridization at each atom). Is the central $\mathrm{C}=\mathrm{C}$ bond shorter, or longer, than the other $\mathrm{C}=\mathrm{C}$ bonds in butatriene?
c). All four carbon atoms in cyclobutadiene are equivalent. There is one other possible valence-satisfied $\mathrm{C}_{4} \mathrm{H}_{4}$ hydrocarbon for which all four C atoms are equivalent: this compound has not been isolated in the laboratory, despite intense effort by a number of research groups. Draw its structure, and by analogy with some of the other $(\mathrm{CH})_{\mathrm{n}}$ hydrocarbons identified above, suggest a feasible trivial name for this compound.
d). How many different chloro-monosubstituted forms (ie $\mathrm{C}_{4} \mathrm{H}_{3} \mathrm{Cl}$ ) exist, of i). cyclobutadiene
ii). butatriene
iii). the compound identified in part c)?
e). How many different chloro-disubstituted forms (ie $\mathrm{C}_{4} \mathrm{H}_{2} \mathrm{Cl}_{2}$ ) exist, of
i). cyclobutadiene
ii). butatriene
iii). the compound identified in part c)?
f). How could the isomers of dichlorobutatriene be distinguished, on the basis of melting points?

## PROBLEM 2.

a). Draw an energy-level diagram that shows how the 1 s atomic orbitals of two hydrogen atoms combine to form the molecular orbitals of $\mathrm{H}_{2}$.
b). Describe the MOs of $\mathrm{H}_{2}$ and their relationship to their parent atomic orbitals.
c). Why is the higher energy MO in $\mathrm{H}_{2}$ called an antibonding orbital?
d). In a similar way, we may combine the atomic orbitals of more complicated atoms to form molecular orbitals. Consider the oxygen molecule, $\mathrm{O}_{2}$. Arrange the oxygen atoms as follows (along the $y$ axis) and assume that there are $1 \mathrm{~s}, 2 \mathrm{~s}, 2 \mathrm{p}_{\mathrm{x}}$, $2 p_{y}$ and $2 p_{z}$ orbitals on each atom.


Now, construct the molecular orbitals arising from the interaction of the $2 \mathrm{~s}, 2 \mathrm{px}$, 2 py and 2 pz atomic orbitals on two oxygen atoms and fill them in on the diagram below:

$2 \mathrm{p}_{\mathrm{y}}\left\{\begin{array}{lll}\square & \sigma^{*} & \mathrm{~h} \\ \square & \sigma & \mathrm{~g}\end{array}\right.$

$2 \mathrm{~s}\left\{\begin{array}{lll}\square & \sigma * & d \\ & \sigma & c\end{array}\right.$
1s

$\mathrm{O}_{2}$
e) We may rearrange these molecular orbitals in order of increasing energy in a molecular orbital diagram:


Why is the energy of orbital $g$ lower than e or $i$, and similarly, why is the energy of orbital h higher than $f$ or $j$ ?
f) Why do orbitals e and i have the same energy?
g) If we were to stretch the $\mathrm{O}_{2}$ molecule (i.e. make the $\mathrm{O}-\mathrm{O}$ distance bigger) how would the energy of orbital j change? Would this change be more or less than the change in energy of orbital h ?

## PROBLEM 3.

Molecular orbital theory can be applied to determine the orbital occupancy of CN , NN , and NO.
a). What is the bond order for each of these molecules?
b). Which of $\mathrm{CN}, \mathrm{N}_{2}$, and NO has the highest IE (ionization energy)? Which has the lowest IE? $\quad\left[\operatorname{IE}(\mathrm{X})=\Delta \mathrm{H}^{\circ}{ }_{\mathrm{f}}\left(\mathrm{X}^{+}\right)-\Delta \mathrm{H}_{\mathrm{f}}^{\circ}(\mathrm{X})\right]$
c). Which has the highest electron affinity? (The electron affinity is the energy released upon attachment of an electron to a species, and is positive when electron attachment is exothermic).
d). Addition or subtraction of electrons from CN or NO produces species which are formally isoelectronic with $\mathrm{N}_{2}$. Would you expect these isoelectronic analogues to have as high a bond strength as $\mathrm{N}_{2}$ itself? If so, why? If not, why not?

## PROBLEM 4.

The noble gases were once thought to be completely inert and incapable of chemical bond formation. It is now known that this is not the case, and most general chemistry textbooks now describe some of the krypton- and xenoncontaining compounds which have been isolated.
a). Using valence-bond theory, predict the geometries possible for $\mathrm{XeF}_{2}$ and $\mathrm{XeF}_{4}$.
b). What is the oxidation number of Xe in each of these compounds? Would you expect them to behave as oxidizing or as reducing agents?
c). Helium is widely known as the most inert of all the elements; yet even helium's 'inertness' is strictly only applicable to its interactions with other neutral atoms and molecules. Compounds of helium, involving formal chemical bonds between helium and other atoms, can exist when the overall entity bears a (generally positive) charge. For example, the helium atom can form observable (though not necessarily long-lived) compounds with $\mathrm{H}^{+}$, with $\mathrm{He}^{+}$, and with $\mathrm{He}^{2+}$. Use MO theory to determine the bond order for each of these cases.
d). Stable diatomic dications of the formula $\mathrm{XHe}^{2+}$ are generally only possible when $\operatorname{IE}\left(\mathrm{X}^{+}\right)<\operatorname{IE}(\mathrm{He})$ : that is, when the energy required to further ionize $\mathrm{X}^{+}$is less than that needed to ionize He. Without recourse to a table of successive ionization energies, identify which element (called 'Z'), from H to Ar , is most likely to fulfil this criterion.
e). Which of the immediate neighbours of your identified element $Z$ (ie those elements either 1 left, 1 right, 1 above, or 1 below it in the periodic table) is most likely to also form a stable dication with He? Which of Z's neighbours is least likely to form such a dication?

## PROBLEM 5.

Benzene is the prototypical aromatic hydrocarbon. Larger hydrocarbons, consisting of a network of benzenoid rings (somewhat like a small section of a graphitic sheet) can also possess aromatic character and are known as 'polycyclic aromatic hydrocarbons' or PAHs. Many structural features of PAHs can be understood by considering them to be comprised of $6 \pi$ 'benzenoid' aromatic rings (although larger delocalized systems, such as $10 \pi$ and $14 \pi$ systems, should also be considered for completeness). In this question, we shall assume that $6 \pi$ delocalized orbitals are sufficient to explain the structural features of PAHs. The simplest PAH is naphthalene, $\mathrm{C}_{10} \mathrm{H}_{8}$ :


Note that, although naphthalene is generally drawn with both rings fully delocalized, we can expect it to be less aromatic than two separate benzene rings. This is because delocalization in one ring places constraints on the bonding in the other ring:


Here, delocalization in the ring shown in bold is only possible if the other ring exhibits a formal alternation of single and double C-C bonds. Obviously in a symmetrical molecule such as naphthalene we should not expect the two rings to exhibit different bonding patterns, and instead we should say that each ring has
some aromatic character (but not as much as a benzene ring) and some tendency to alternation of single and double bonds. If we draw naphthalene like this:

then we can see that bonds 'a' and 'c' have significant single-bond character, while bonds ' b ' have substantial double-bond character (and this will also hold true for the analogous bonds on the other ring).

Now consider the carbon skeletons of the following three PAHs:


Phenanthrene


Triphenylene


Pyrene
a). Using $\bigcirc$ to denote rings having aromatic character, and showing other $\mathrm{C}-\mathrm{C}$ bonds as formal single or double bonds, show the most aromatic resonance forms possible for each of the above three PAH skeletons. The most aromatic resonance form possible is that having the greatest number of aromatic rings; for naphthalene, this is

b). Identify, using the letters 'L' and 'S' respectively, the longest and shortest carboncarbon bonds in each of phenanthrene, triphenylene, and pyrene. (If a PAH does not feature 'unusually' long or 'unusually' short bonds - i.e. significantly different from the benzene C-C bond length - then do not attempt to label it).
c). Compare the number of 'fully-aromatic' rings, for the resonance forms obtained in a), to the total number of rings in each PAH. Which is the most aromatic of these PAHs, on this basis? Which is the least aromatic?
d). Now compare the number of 'fully-aromatic' rings to the number of carbon atoms in each PAH. Which is the most aromatic PAH, and which is the least, on this basis? Is the ordering different from that in c)?
e). Now consider a sheet of graphite:

i). What is the average bond order per $\mathrm{C}-\mathrm{C}$ bond?
ii). Is each C-C bond longer, or shorter, than in benzene?
iii). Is graphite more, or less, aromatic (per carbon atom) than benzene?


## PROBLEM 6.

A PhD student has received a consignment of all six $\mathrm{C}_{4} \mathrm{H}_{8}$ isomers (which are gases at room temperature). Unfortunately, during shipping the labels have become detached from the gas cylinders and she cannot correctly identify them. She labels the cylinders as 'A' to ' F ' and sets about trying to deduce the contents of each cylinder. She makes the following observations:
i). A, B, C, and D are seen to decolourise bromine rapidly (even in darkness), while $E$ and $F$ do not.
ii). The products of the reactions of B and C with $\mathrm{Br}_{2}$ are found to be stereoisomers of each other.
iii). A, B, and C all give an identical product when reacted with $\mathrm{H}_{2}$ over a Pd catalyst.
iv). E has a higher boiling point than F .
v). C has a higher boiling point than B .

Identify the contents of the six cylinders.

## PROBLEM 7.

One of the most durable general rules in chemistry is that virtually all general rules are violated by some compound or other! For example, $\mathrm{O}_{2}$ breaks the electron-pairing rule, and $\mathrm{PF}_{5}$ disobeys the octet rule. Another rule for which
'loopholes' exist is the often-stated requirement for optical isomerism in organic compounds: these compounds must contain an $\mathrm{sp}^{3}$ hybridized, asymmetric carbon atom which is bonded to four different atoms or groups. It is now known that some of the larger fullerenes, for example some of the $\mathrm{C}_{76}$ isomers, are optically active: these are molecules which formally contain only $\mathrm{sp}^{2}$ hybridized C atoms, and in which each carbon atom is therefore directly bonded to only three other atoms. Here the chirality arises from the fullerene lattice's curvature, and from the asymmetrical pattern of 5-and 6-membered rings which comprise it.

Much simpler organic molecules can also provide unexpected instances of stereoisomerism:
a). How many different isomers exist of dichloroethylene? Identify any pairs of stereoisomers. Which category of stereoisomerism is exhibited here?
b). How many different dichloropropadiene (dichloroallene) isomers exist? Identify any pairs of stereoisomers. Which category of stereoisomerism is exhibited here?
c). For compounds of the general formula $\mathrm{ClHC}=(\mathrm{C}=)_{\mathrm{n}} \mathrm{CHCl}$, formulate a rule which indicates the dependence of isomerism upon $n$. What is the underlying geometrical basis behind this rule?

## PROBLEM 8.

A sample of dichloropropadiene is analyzed in a mass spectrometer. A strong signal is observed in the mass spectrum at a mass-to-charge ( $\mathrm{m} / \mathrm{z}$ ) ratio of 75 , and another at $\mathrm{m} / \mathrm{z} 77$. Under certain operating conditions, these are the only two signals seen in the mass spectrum. Under different conditions, the same sample gives rise to a number of different signals, including $\mathrm{m} / \mathrm{z} 82$ (but not 83 ) and $\mathrm{m} / \mathrm{z}$ 28 (but not 27). Regardless of the operating conditions, it is found that the signal at $\mathrm{m} / \mathrm{z} 77$ is always $60 \%$ of the intensity of the peak at $\mathrm{m} / \mathrm{z} 75$.

You can assume the following:

- Observed ions are all singly-charged positive ions and arise directly by dissociative ionization of the dichloropropadiene, without any rearrangement occurring during fragmentation.
- The dichloropropadiene has been prepared from elemental carbon, hydrogen, and chlorine in some unspecified fashion: the elemental feedstocks used are known to contain isotopic abundance ratios different from those conventionally observed for hydrogen, carbon, and chlorine, but contain only stable isotopes. Furthermore, no effort has been made to label specific atoms within the molecule with any particular isotope.
a). What are the chemical formulae of the ions detected at $\mathrm{m} / \mathrm{z} 75$ and 77 ?
b). What is the isotopic distribution seen in the dichloropropadiene sample? Calculate the percentage of each isotopomer of dichloropropadiene. [Isotopomers are molecules which have identical chemical formulae but which differ in their constituent isotopes.]
c). What is the molar mass of the sample? Assume, for simplicity, that the atomic mass of each nucleus is exactly equal to its mass number.
d). Can you identify the isomer of dichloropropadiene studied here?

A recent development of traditional mass spectrometry is Electrospray Mass Spectrometry (ESMS). ESMS differs from conventional mass spectrometry only in the fact that solutions are injected into the mass spectrometer and there is no ionising source. This technique detects only those ions which already pre-exist in solution.

For example, a sample of tetrabutyl ammonium bromide (in an inert solvent) injected into an ESMS gives a peak at $\mathrm{m} / \mathrm{z}=242$ as the most intense signal in the positve ion detection mode. There are two major signals, of approximately equal instensity, at $\mathrm{m} / \mathrm{z}=79$ and $\mathrm{m} / \mathrm{z}=81$ in the negative ion mode.
e). what ion(s) give rise to these three signals?

A sample of isopropanol (propan-2-ol) injected into an ESMS instrument shows a peak at $\mathrm{m} / \mathrm{z}=61$ as the most intense signal in the positive ion detection mode. The most intense signal in the negative ion detection mode is at $\mathrm{m} / \mathrm{z}=59$.
f). what ion(s) give rise to these two signals?

## PROBLEM 9.

Dilithium, a substance which is crucial to the propulsion system of the Federation starship 'Enterprise', is actually a known species (though it does not exhibit all of the properties which Roddenberry et al. ${ }^{t}$ have ascribed to it!). Dilithium is formed by the adhesion of two lithium atoms in the gas phase:

$$
\begin{equation*}
\mathrm{Li}_{(\mathrm{g})}+\mathrm{Li}_{(\mathrm{g})} \quad \rightleftharpoons \operatorname{Li}_{2(\mathrm{~g})} \tag{1}
\end{equation*}
$$

a). The enthalpy of formation of dilithium is not easily measurable by direct means. However, the following thermochemical parameters are known:

[^0]$\Delta \mathrm{H}^{\circ}{ }_{\mathrm{f}}\left(\mathrm{Li}_{(\mathrm{g})}\right)=159.4 \mathrm{~kJ} \mathrm{~mol}^{-1}$
$\operatorname{IE}\left(\mathrm{Li}_{(\mathrm{g})}\right)=5.392 \mathrm{eV}\left[1 \mathrm{eV}=96.486 \mathrm{~kJ} \mathrm{~mol}^{-1}\right]$
$\mathrm{D}^{0}\left(\mathrm{Li}_{2}{ }^{+}(\mathrm{g})\right)=129.8 \mathrm{~kJ} \mathrm{~mol}^{-1}\left[\mathrm{D}^{0}\left(\mathrm{Li}_{2}{ }^{+}(\mathrm{g})\right)\right.$ is the bond strength of $\left.\mathrm{Li}_{2}{ }^{+}(\mathrm{g})\right]$
$\operatorname{IE}\left(\operatorname{Li}_{2(\mathrm{~g})}\right)=5.113 \mathrm{eV}$
Using these values, determine $\Delta \mathrm{H}^{\circ}\left(\mathrm{Li}_{2(\mathrm{~g})}\right)$ and $\mathrm{D}^{0}\left(\mathrm{Li}_{2(\mathrm{~g})}\right)$.
b). The chief warp plasma chemist on the Enterprise is testing the performance of the warp nacelles. He transports 122.045 g of pure lithium into the evacuated reaction chamber within the port warp nacelle. The reaction chamber has a volume of $5.9474 \times 10^{5} \mathrm{~m}^{3}$, and is maintained at an operating temperature of 610.25 K . A highly sensitive pressure monitor indicates that the pressure within the reaction chamber stabilizes at $9.462 \times 10^{-4}$ Torr ( 1 Torr $=0.133322 \mathrm{kPa}$ ); a spectrophotojargonometric analysis of the inner surface of the reaction chamber shows that all of the lithium has vaporized. (The reaction chamber, of course, is made from a duranium alloy which has zero vapour pressure at 610.25 K .) What are the concentrations of gaseous lithium and dilithium in the reaction chamber? What is the equilibrium constant, $\mathrm{K}_{\mathrm{c}}$, for reaction (1) at this temperature?
$$
[\mathrm{R}=8.31441 \mathrm{~J} \text { K-1 mol-1; } \mathrm{Mr}(\mathrm{Li})=6.9410 \mathrm{~g} \text { mol- } 1]
$$
c). Next, 265.384 g of lithium is transported into an identical, evacuated reaction chamber (also at 610.25 K ) within the starboard warp nacelle. The pressure gauge on this chamber stabilizes at $1.0455 \times 10^{-3}$ Torr. What is the vapour pressure of dilithium at 610.25 K ?
d). Assuming that the reaction $2 \mathrm{Li}_{(\mathrm{g})} \rightarrow \mathrm{Li}_{2(\mathrm{~g})}$ is the sole source of propulsive energy for the starship Enterprise, calculate the minimum mass of lithium which must be carried as fuel if the Enterprise is to accelerate from rest to a velocity of half lightspeed. The total mass of the Enterprise, which is a large spaceship with a complement of several hundred crew members, is $3.586 \times 10^{6} \mathrm{~kg}$ (excluding fuel).
To simplify your calculation, you can assume the following:

- relativistic effects can be ignored
- the reaction chambers can be maintained indefinitely at 610.25 K without any energy cost
- solid lithium, transported into the reaction chamber, can be vaporized to lithium atoms without any energy cost (conversely, the reverse process does not release any energy)
- the Li-Li bond enthalpy can be converted with $100 \%$ efficiency into the starship's kinetic energy
- the lithium carried as fuel need not be included in the effective mass of the Enterprise.
[Clearly, some of these assumptions are not physically reasonable, but that need not concern us here. We are dealing with science fiction!]
e). Finally, comment on the apparent suitability (or otherwise) of dilithium formation as a technique for near-lightspeed travel. Would formation of diberyllium, $\mathrm{Be}_{2(\mathrm{~g})}$, offer a better alternative?


## PROBLEM 10.

Elemental analysis of an organic substance, $\mathbf{X}$, has indicated its composition as $\mathbf{C}$ ( $40.02 \%$ by mass) and H ( $6.75 \%$ by mass). It does not contain detectable quantities of N or S , and it is presumed that the remaining fraction of its composition is oxygen, which cannot be reliably analyzed by direct methods.
a). What is the empirical formula of $\mathbf{X}$ ?
b). $\quad \mathbf{X}$ is a liquid at room temperature. 10 mL of $\mathbf{X}\left(\right.$ density $\left.=1.044 \mathrm{~g} \mathrm{~mL}^{-1}\right)$ is added to cyclohexane to a total volume of 500 mL . The density of this solution is determined to be $0.777 \mathrm{~g} \mathrm{~mL}^{-1}$. The solution is found to possess a freezing point of $+2.02{ }^{\circ} \mathrm{C} . \mathrm{T}_{\mathrm{f}}\left(\mathrm{c}-\mathrm{C}_{6} \mathrm{H}_{12}\right)=6.60{ }^{\circ} \mathrm{C} ; \mathrm{K}_{\mathrm{f}}\left(\mathrm{c}-\mathrm{C}_{6} \mathrm{H}_{12}\right)=20.0^{\circ} \mathrm{C} \mathrm{kg} \mathrm{mol}{ }^{-1}$. What is the molecular weight and formula of $\mathbf{X}$, from the above measurements?
c). $\mathbf{X}$ is also readily miscible in water. 50 mL of $\mathbf{X}$ is added to ultrapure water, again to a total volume of 500 mL . This solution has a density of $1.005 \mathrm{~g} \mathrm{~mL}^{-1}$, and a freezing point of $-3.54{ }^{\circ} \mathrm{C} . \mathrm{K}_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}\right)=1.86^{\circ} \mathrm{C} \mathrm{kg} \mathrm{mol}{ }^{-1}$. What is the apparent molecular weight of $\mathbf{X}$ from the above data?
d). In aqueous solution, $\mathbf{X}$ is found to react with added base. When 25.00 mL of the aqueous solution of $\mathbf{X}$, prepared in c), is titrated against $1.247 \mathrm{~mol} \mathrm{~L}^{-1}$ aqueous NaOH , the endpoint as determined by a pH meter is obtained at 33.60 mL of the hydroxide solution. The titrated system, at endpoint, has a volume of 58.50 mL and a density of $1.003 \mathrm{~g} \mathrm{~mL}^{-1}$. It is found to freeze at $-2.78{ }^{\circ} \mathrm{C}$. What is the structure of the product, $\left(\mathrm{Na}^{+}\right)_{i} \mathbf{Y}^{\mathbf{i}-}$, which results from the reaction of $\mathbf{X}$ with aqueous NaOH ?
e). What is the structure of compound $\mathbf{X}$ ? Comment on any apparent discrepancy in your answers to parts b), c), and d).

## PROBLEM 11.

It is often considered that two isotopes will have identical chemical reactivity: however, this is not precisely true. The differing reactivity of different isotopes
arises via the dependence of vibrational energy spacings, in molecules, on the masses of the molecule's constituent atomic nuclei. While the details of this mechanism need not concern us here, it is useful to note that compounds featuring light isotopes (eg. ${ }^{1} \mathrm{H}^{19} \mathrm{~F}$ ) have slightly lower bond strengths than analogous compounds featuring heavier isotopes (e.g. ${ }^{2} \mathrm{H}^{19} \mathrm{~F}$ ).

This "isotope effect" is often of little or no importance at room temperature, but it can be crucial in the chemistry of low-temperature regions. One type of widelystudied environment which is characterized by very low temperatures (typically $10 \mathrm{~K}-20 \mathrm{~K}$ ) is that of the dense interstellar clouds, which are the large clouds of gas and dust from which stars ultimately form. Deuterium fractionation in cold interstellar clouds occurs by a variety of processes, including the following mechanism:

$$
\begin{array}{lll}
\mathrm{H}_{2}+\mathrm{D} & \rightarrow & \mathrm{HD}+\mathrm{H} \\
\mathrm{HD}+\mathrm{D} & \rightarrow & \mathrm{D}_{2}+\mathrm{H} \tag{2}
\end{array}
$$

Thermochemical parameters relevant to reaction (1) are:

$$
\begin{array}{ll}
\Delta \mathrm{H}_{\mathrm{f}}^{\circ}\left(\mathrm{H}_{2(\mathrm{~g})}\right)=0 \mathrm{~kJ} \mathrm{~mol}^{-1} & \mathrm{~S}^{\circ}\left(\mathrm{H}_{2(\mathrm{~g})}\right)=130.57 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1} \\
\Delta \mathrm{H}_{\mathrm{f}}^{\circ}\left(\mathrm{HD}_{(\mathrm{g})}\right)=0.33 \mathrm{~kJ} \mathrm{~mol}^{-1} & \mathrm{~S}^{\circ}\left(\mathrm{HD}_{(\mathrm{g})}\right)=143.69 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1} \\
\Delta \mathrm{H}_{\mathrm{f}}^{\circ}\left(\mathrm{H}_{(\mathrm{g})}\right)=216.00 \mathrm{~kJ} \mathrm{~mol}^{-1} & \mathrm{~S}^{\circ}\left(\mathrm{H}_{(\mathrm{g})}\right)=114.60 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1} \\
\Delta \mathrm{H}_{\mathrm{f}}^{\circ}\left(\mathrm{D}_{(\mathrm{g})}\right)=219.76 \mathrm{~kJ} \mathrm{~mol}^{-1} & \mathrm{~S}^{\circ}\left(\mathrm{D}_{(\mathrm{g})}\right)=123.24 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}
\end{array}
$$

[Enthalpies of formation are zero Kelvin values (more appropriate to interstellar temperatures than would be 298 K measurements); entropies are 298 K values, but for our purposes can be assumed temperature-independent].
a). Determine the free-energy change $\Delta \mathrm{G}^{\circ}$ for reaction (1), at $\mathrm{T}=20 \mathrm{~K}$ and at $\mathrm{T}=$ 1000 K . In which direction is this reaction spontaneous, if the initial concentrations of all reactants and products are equal?
b). What does the sign of $\Delta \mathrm{H}^{\circ}$ (i.e., positive or negative) tell us about the respective bond strengths of $\mathrm{H}_{2}$ and HD? What does the sign of $\Delta \mathrm{S}^{\circ}$ tell us about reaction (1) in the forward direction, and what is the physical basis for the sign of $\Delta \mathrm{S}^{\circ}$ ?
c). Now consider reaction (2). What is the sign of $\Delta \mathrm{H}^{\circ}$, and of $\Delta \mathrm{S}^{\circ}$, for reaction in the forward direction? If you assume that the enthalpy and entropy changes are equal in magnitude to those found in a), calculate the free energy change and predict the direction of spontaneous reaction at 20 K , and at 1000 K .
d). Molecular hydrogen (in its various isotopic forms) is present in much higher concentrations than atomic hydrogen (and atomic deuterium) in interstellar
clouds. Predict the dominant form of deuterium (ie $\mathrm{D}, \mathrm{HD}$ or $\mathrm{D}_{2}$ ) in interstellar clouds, assuming a temperature of 20 K :
i). when the cosmic abundance $n(D) \ll n(H)$ [that is, when the total number of deuterium nuclei, in whatever chemical form, is very much less than the total number of hydrogen nuclei], and
ii). when $n(D)=n(H)$. What will be the dominant form of hydrogen under these conditions?

Scenario i) is that which applies in the real universe.

## PROBLEM 12.

Helium is the only member of the periodic table to have been detected within an extraterrestrial object (the solar corona) prior to its isolation within the laboratory. We now know much of the physical and chemical properties of helium; but for almost thirty years, from 1868, the solar spectrum was the sole source of information on this novel element.
a). With our current understanding of quantum theory, this spectrum contains much useful data to analyze. For example, the visible spectrum features a series of absorption lines at wavelengths of $4338,4540,4858,5410$ and $6558 \AA(1 \AA=$ $10^{-10} \mathrm{~m}$ ). The spacing of these lines indicates that the absorption is due to excitation of a 'hydrogen-like' atom or ion (i.e., one with an electron configuration equivalent to H ). Is this species $\mathrm{He}, \mathrm{He}^{+}$, or $\mathrm{He}^{2+}$ ?
b). It can be shown that the energy level common to all of the transitions involved in these absorption lines is the lower energy state $n_{i}=4$. To what upper energy states $n_{f}$ do the respective absorption features lead to? What is the Rydberg-like constant [i.e., the constant analogous to $\mathrm{R}_{\mathrm{H}}$ in the atomic hydrogen spectrum] for the absorbing species $\left(\mathrm{He}^{\mathrm{i}+}\right)$ which exhibits these transitions?
c). The ionization energy (IE) of a species is often measured in electronvolts (eV). What is $\operatorname{IE}\left(\mathrm{He}^{\mathrm{i}+}\right)$ ?
d). From atomic spectroscopy, it is now known that $\operatorname{IE}\left(\mathrm{He}^{+}\right) / \mathrm{IE}(\mathrm{He})=2.180$. The sum of these two ionization energies gives the appearance energy, $\mathrm{AE}\left(\mathrm{He}^{2+}\right)$, for production of $\mathrm{He}^{2+}$ from He . The quantity $\mathrm{AE}\left(\mathrm{He}^{2+}\right)$ is the minimum quantum of energy which must be deposited into He in order to remove both of its electrons. Calculate the frequency and wavelength of the least energetic photon capable of effecting the double ionization of helium. Is sunlight, at the Earth's surface, an efficient source of such photons?

Useful constants:

$$
\begin{aligned}
& \mathrm{c}=2.997925 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-1} \\
& \mathrm{~h}=6.62618 \times 10^{-34} \mathrm{~J} \mathrm{~s}^{-1} \\
& 1 \mathrm{eV}=96.486 \mathrm{~kJ} \mathrm{~mol}^{-1}=2.4180 \times 10^{14} \mathrm{~Hz}
\end{aligned}
$$

## PROBLEM 13.

A student (the same unfortunate soul to have featured in Question 6) has received a consignment of alkali halides, but - you guessed it - the labels have come off all but one of the containers: the identified container is potassium bromide. The laboratory in which she works does not have access to any spectroscopic instruments: therefore, in an attempt to identify the unknown alkali halide samples, she uses an ion-exchange column. The ion-exchange resin she selects is a cross-linked polystyrene resin of the strong acid type, containing sulfonic acid groups $\left(-\mathrm{SO}_{3} \mathrm{H}\right)$ from which only the protons can be exchanged. She analyzes the six unknown alkali halide samples (and the KBr , as a test of the validity of the method) in the following manner:

She weighs out $5.00 \pm 0.01 \mathrm{~g}$ of each sample, which is dissolved in distilled water in a 100 mL volumetric flask. 40 mL of each solution is passed through the column; the eluant is collected in a 250 mL volumetric flask, and the column is washed through twice with distilled water; the eluant sample is then made up to 250 mL . Before the next sample is run through the column, she recharges the column resin by washing it with sufficient 1 M HCl , and then with distilled water. She titrates 50 mL aliquots of each eluant sample, in triplicate, against sodium hydroxide solution (nominal concentration $=3.26 \times 10^{-2} \mathrm{~mol} \mathrm{~L}^{-1}$ ) using phenolphthalein as an indicator, obtaining the following results:

| Sample | Mean titre volume |
| :--- | :--- |
| A | $21.15 \pm 0.1 \mathrm{~mL}$ |
| B | $29.30 \pm 0.1 \mathrm{~mL}$ |
| C | $7.40 \pm 0.1 \mathrm{~mL}$ |
| D | $21.20 \pm 0.1 \mathrm{~mL}$ |
| E | $10.30 \pm 0.1 \mathrm{~mL}$ |
| F | $29.15 \pm 0.1 \mathrm{~mL}$ |
| KBr | $10.25 \pm 0.1 \mathrm{~mL}$ |

In analyzing these results, you can assume that

- each sample is of $>99 \%$ purity
- each container is both water- and air-tight
- no two containers contain the same alkali halide; the consignment included fluorides, chlorides, bromides and iodides, but no astatine compounds.
a). What is the reasoning behind the student's use of the above procedure? Write chemical reaction equations for any reactions occurring.
b). Which of the samples can be positively identified from this analysis? Which of the samples can only be narrowed down to two or three possibilities?
c). Using available equipment in the lab - including a watchglass, a roll of litmus paper, an acidified solution of sodium persulfate $\left(\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{8}\right)$ and a dropper bottle of starch solution - the student was able to identify each of the six unknown samples. Without knowing the results of her tests using these reagents, explain how the above materials would suffice to identify all of the samples not conclusively identified from b).
d). What property of the alkali halides prevents the unambiguous identification of some of the unknowns by the ion exchange technique used here? Would you expect a similar effect to be as great a problem in, for example, a similar attempt to identify a number of alkaline earth halides $\mathrm{MX}_{2}$ ?


## PROBLEM 14.

Chemistry can sometimes give rise to 'optical illusions' when three-dimensional structures are considered. For example:

a). How many $\mathrm{C}_{4}$ rings does cubane possess?
b). For a valence-satisfied hydrocarbon $\mathrm{C}_{\boldsymbol{n}} \mathrm{H}_{\boldsymbol{m}}$, how is $\boldsymbol{m}$, the number of hydrogen atoms, related to $\mathbf{n}$, the number of carbon atoms, to $\mathbf{r}$, the number of rings and to d, the number of double bonds?
c). According to the answer given in a), what is the formula for cubane? Is this formula correct?
d). Now for a temporary diversion. Two polycyclic aromatic hydrocarbons (PAHs) are known as coronene and corannulene. They have, respectively, the following carbon skeletons:



Both PAHs have fully conjugated carbon-carbon bonding: redraw coronene and corannulene, ensuring that your drawings have as many $\mathrm{C}=\mathrm{C}$ bonds as is consistent with complete conjugation (including conjugation of each carbon atom on the central polygon). Now, from the number of C atoms, rings, and double bonds, predict the number of hydrogens on each molecule, and draw in the hydrogen atoms to satisfy any valence-unsatisfied C atoms. Does the number of H atoms added tally with the prediction of the formula derived in b )?
e). The two PAHs drawn above are shown as though they were both flat: in fact, one is flat, while one is not [though it is not very severely distorted from planarity]. Which PAH is not flat, and why?
f). Now, using your flat drawing of a non-flat PAH as inspiration, draw cubane as thought it were flat: do not attempt to introduce any perspective, but preserve the integrity of all C-C and C-H bonds which cubane possesses. The drawing which you produce may well look quite distorted [and so it should - you are drawing a highly 3-dimensional structure as though it occupied only two dimensions!], and it should not feature any instances of bonds crossing other bonds. From your flat drawing of cubane, tally the number of rings present in this molecule. Does this agree with your answer in a)? Does it agree with b)?
g). A further check: determine the maximum number of C-C bonds which may be broken in each of coronene and corannulene before the molecule must fall into two fragments ie. without fragmenting the carbon skeleton. [Do not make any distinction between double bonds and single bonds in doing this.] Redraw the carbon skeletons of these PAHs, minus these bonds, to ensure that all carbon atoms are still connected. Is there a relationship between the number of bonds which may be broken and the number of rings (and if so, what is the relationship)?
h). How many bonds in cubane can be broken without fragmenting the carbon skeleton? Does this give a ring number, $\mathbf{r}$, in agreement with a), c), and f)?
i). Now consider dodecahedrane, $\mathrm{C}_{20} \mathrm{H}_{20}$ :


Draw a flat version of this molecule, by analogy with cubane in f). How many rings does this 12 -faceted molecule possess? Is this number in agreement with the formula from b )?
j). Finally we consider buckminsterfullerene, $\mathrm{C}_{60}$ :


For this, you need not attempt a flat drawing [sighs of relief all round], but some calculation is required. Each C atom in $\mathrm{C}_{60}$ has three nearest neighbours. How many carbon-carbon bonds are present? [If you have trouble here, refer back to cubane where each C atom also has three nearest neighbour carbons.] How many of these bonds must be double bonds, in order to satisfy valence requirements? From the formula found in b , how many rings does $\mathrm{C}_{60}$ possess? A geometrical proof, derived by Euler, indicates that a closed network comprised only of pentagons and hexagons must contain exactly twelve pentagons regardless of the number of hexagons. Can you state unambiguously how many of $\mathrm{C}_{60}$ 's rings are pentagons, and how many are hexagons?

## PROBLEM 15.

The acidity of a water sample is influenced by gas absorption. The most important gas, in this respect, is generally carbon dioxide.
a). Give a set of three reaction equations which demonstrate the effect of atmospheric $\mathrm{CO}_{2}$ upon water acidity.
b). Arrange the following gas mixtures in order of their tendency for $\mathrm{CO}_{2}$ (g) to dissolve in aqueous solution (percentages given are mole \%):
i). $\quad 90 \% \mathrm{Ar}, 10 \% \mathrm{CO}_{2}$
ii). $\quad 80 \% \mathrm{Ar}, 10 \% \mathrm{CO}_{2}, 10 \% \mathrm{NH}_{3}$
iii). $\quad 80 \% \mathrm{Ar}, 10 \% \mathrm{CO}_{2}, 10 \% \mathrm{Cl}_{2}$

Write equations for any chemical reactions occurring in aqueous solution on exposure to these gas mixtures.
c). Arrange the following aqueous systems in order of their ability to dissolve $\mathrm{CO}_{2}$. Assume that, prior to exposure to $10 \% \mathrm{CO}_{2}$ in Ar , they have been allowed to equilibrate with air:
i). distilled water
ii). $\quad 1 \mathrm{M} \mathrm{HCl}$ solution
iii). $\quad 1 \mathrm{M}$ sodium acetate solution
d). Assuming an atmospheric content of 350 ppm CO 2 (by volume), and assuming that equilibration has been reached between gaseous and aqueous $\mathrm{CO}_{2}$, calculate the pH of a raindrop at atmospheric pressure. Appropriate constants at $25^{\circ} \mathrm{C}$ are: $\mathrm{K}_{\mathrm{H}}\left(\mathrm{CO}_{2}\right)=3.39 \times 10^{-2} \mathrm{~mol} \mathrm{~L}^{-1} \mathrm{~atm}^{-1}, \mathrm{~K}_{\mathrm{b}}\left(\mathrm{HCO}_{3}^{-}\right)=2.24 \times 10^{-8}, \mathrm{~K}_{\mathrm{b}}\left(\mathrm{CO}_{3}{ }^{2-}\right)=2.14$ $\times 10^{-4}$.
e). Calculate the pH of a bottle of carbonated water $\left(\mathrm{P}\left(\mathrm{CO}_{2(\mathrm{~g})}\right)=1 \mathrm{~atm}\right)$.
f). A 100 mL sample of rainwater is titrated against $1.00 \times 10^{-4} \mathrm{~mol} \mathrm{~L}^{-1} \mathrm{NaOH}$ (in uncarbonated, distilled water) under experimental conditions which prevent further gas exchange. Sketch the pH curve for this titration. Your graph must indicate the expected pH at the start of the titration; at 7.1 mL ; and at 21.2 mL of added NaOH solution.

## PROBLEM 16.

a). How many carboxylic acids exist, which satisfy the overall formula $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{2}$ ? Draw and name all such compounds. [Do not name optical isomers, nor draw enantiomers separately, but indicate, with asterisks at chiral carbons, which structures are optically active.]
b). Rank the above carboxylic acids in decreasing order of their expected $\mathrm{K}_{\mathrm{a}}$ values in aqueous solution. Explain your reasoning for this ordering.
c). How many structural isomers of the formula $\mathrm{R}-\mathrm{COOH}$, where $\mathrm{R}=\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{~F}$, exhibit optical activity? Draw these structural isomers (identifying chiral atoms as in a)), and predict the most acidic and the least acidic species amongst those which you have drawn. Justify your assignments of relative acidity for these species.
d). What organic product is expected from the reaction of a carboxylic acid with an alcohol under acidic conditions? Write a generalized equation for such a reaction, showing reactants and products.
e). If ${ }^{18} \mathrm{O}$-labelled 1-propanol is reacted with acidified, unlabelled ethanoic acid, the isotopic label is found to reside entirely within the organic product. Draw this product, and write a generalized mechanism for the carboxylic acid/alcohol reaction.
f). If, instead, the reaction employs unlabelled propanol and labelled ethanoic acid $\left(\mathrm{CH}_{3} \mathrm{C}-\mathrm{OH}\right)$, show the products expected:
i). for reaction occurring in $1 \mathrm{~mol} \mathrm{~L}^{-1} \mathrm{HCl}$, and
ii). for reaction initially in $1 \mathrm{~mol} \mathrm{~L}^{-1} \mathrm{NaOH}$, followed by acidification with 1 mol $\mathrm{L}^{-1} \mathrm{DCl}$.

## PROBLEM 17.

The noble gases, helium in particular, are not generally thought of in terms of solid-phase chemistry. Nevertheless, several different types of material are known to contain embedded or trapped helium atoms. Molecules which possess the ability to incarcerate noble-gas atoms are known as 'clathrates'. Such compounds are present in meteorites, which are seen to release minute quantities of noble gases upon heating. Comparison of the thermal response of the (currently unidentified) noble-gas-containing phase of meteoritic material, with that of the species $\mathrm{He} @ \mathrm{C}_{60}$ (the '@' indicates that the helium is contained within, but is not chemically bonded to, the fullerene $\mathrm{C}_{60}$ cage), has led to the recent suggestion that fullerenes in meteorites may be responsible for the embedded noble gases in these materials.
a). The diameter of the $\mathrm{C}_{60}$ fullerene cage is $7.0 \AA\left(1 \AA=10^{-10} \mathrm{~m}\right)$. Calculate the interior volume of $\mathrm{C}_{60}$; also determine the 'pressure' within the cage, in the species He@C60, at 298 K .
b). In 1994, an analysis was reported of the fullerene content of material from an ancient meteorite impact site ( 1.85 billion years old), in Sudbury, Ontario. It was hypothesized that the $\mathrm{C}_{60}$ found amongst the impact ejecta may have arisen as a result of shock-induced chemistry associated with the impact. In 1996 it was reported that some of the fullerenes extracted from the material contained helium, with the following results being obtained:

- release of $1.15 \times 10^{-7} \mathrm{~cm}^{3}{ }^{3} \mathrm{He}(\mathrm{STP})$ per g C $\mathrm{C}_{60}$
- release of $2.09 \times 10^{-4} \mathrm{~cm}^{3}{ }^{4} \mathrm{He}(\mathrm{STP})$ per $\mathrm{g} \mathrm{C}_{60}$

What fraction of the $\mathrm{C}_{60}$ molecules in the sample contain a ${ }^{3} \mathrm{He}$ atom? What are the effective mean partial pressures, of ${ }^{3} \mathrm{He}$ and ${ }^{4} \mathrm{He}$ respectively, within the $\mathrm{C}_{60}$ sample?
c). The content of ${ }^{4} \mathrm{He}$ within Earth's atmosphere is currently $5.240 \pm 0.004 \mathrm{ppm}$ by volume. If it is assumed that the partial pressure of ${ }^{4} \mathrm{He}$ within the $\mathrm{C}_{60}$ sample reflects the helium partial pressure in the atmosphere in which the fullerene was formed, and if it is also assumed that the terrestrial atmosphere's helium content has remained essentially unchanged over 2 billion years, is the ${ }^{4} \mathrm{He}$-release data for the sample consistent with a terrestrial origin of the fullerene cage?
d). The ${ }^{3} \mathrm{He} /{ }^{4} \mathrm{He}$ ratio in the Earth's atmosphere is $1.3 \times 10^{-6}: 1$; values for this parameter in material from the Earth's crust are typically lower still. Is the observed ${ }^{3} \mathrm{He} /{ }^{4} \mathrm{He}$ ratio in the fullerene sample consistent with a terrestrial origin?
e). Now for a change of pace. Consider a (purely hypothetical) fullerene with the formula $\mathrm{C}_{5.0 \times 10^{9}}$, consisting of a single-layer, spherical, carbon shell, and internally pressurized with 120 kPa of helium. Assuming that the carbon-carbon bond distance is $1.42 \AA$, and that the surface structure is entirely consistent with a single graphitic sheet, calculate:
i). the surface area, diameter, and interior volume of this giant fullerene,
ii). the density of the helium-filled fullerene, and
iii). the density of air at STP (assume $\left.\mathrm{M}_{\mathrm{r}}(\mathrm{air})=29.0 \mathrm{~g} \mathrm{~mol}^{-1}\right)$.
iv) Comment on the implications of ii) and iii) for the physical properties of the fullerene.

## PROBLEM 18.

The uses of radioisotopes in nuclear medicine are twofold. Radiotherapy involves targetting of sites of active cell division by radionuclides to induce cell death. Nuclear imaging employs radioisotopes to reveal metabolic details of an organ. One such technique involves determination of a patient's blood volume.
a). Three radiopharmaceutical compounds contain, respectively, the radioisotopes ${ }^{71} \mathrm{Zn}\left(\mathrm{t}_{1 / 2}=2.4\right.$ minutes), ${ }^{67} \mathrm{Ga}$ ( $\mathrm{t}_{1 / 2}=78.25$ hours), and ${ }^{68} \mathrm{Ge}$ ( $\mathrm{t}_{1 / 2}=287$ days ), each with activities of $7.0 \times 10^{7} \mathrm{~Bq}$ per mL . For each of these compounds
i). calculate the activity per mL after 30 minutes have elapsed, and
ii). calculate the activity per mL after 30 minutes and after dilution of 10 mL of the radiopharmaceutical to 25 L .
b). Ignoring chemical effects, what advantages does ${ }^{67} \mathrm{Ga}$ have over the other two radioisotopes for determination of a patient's blood volume?
c). The modes of decay for these three isotopes are $\beta$-particle emission $\left({ }^{71} \mathrm{Zn}\right)$ and electron capture $\left({ }^{67} \mathrm{Ga}\right.$ and $\left.{ }^{68} \mathrm{Ge}\right)$. What are the products of these decay processes?
d). A pharmacist prepares gallium citrate $\left(\mathrm{GaC}_{6} \mathrm{H}_{5} \mathrm{O}_{6} \cdot 3 \mathrm{H}_{2} \mathrm{O}\right)$ from a sample of ${ }^{67} \mathrm{Ga}$ enriched gallium ( $5.0 \times 10^{-5} \mathrm{~mole} \%{ }^{67} \mathrm{Ga} ; 10.25 \mathrm{mg} \mathrm{Ga}$ in total). The synthesis of gallium citrate is quantitative; following synthesis, the radiopharmaceutical is dissolved in 100 mL of water. Eight hours after the ${ }^{67} \mathrm{Ga}$ is first produced, 1 mL of the solution is administered intravenously to a patient, and one hour later a 1 mL blood sample is taken from the patient.
i). Calculate the activity, in Bq , of the 1 mL dose of gallium citrate solution.
ii). If the blood sample has an activity of 105.6 Bq , what is the patient's blood volume?

## PROBLEM 19.

The following half-reactions relate to the speciation of uranium in aqueous solutions:

| $\mathrm{U}^{3+}+3 \mathrm{e}$ | $\rightarrow$ | U | $\mathrm{E}^{\circ}=-1.798 \mathrm{~V}$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{U}^{4+}+\mathrm{e}$ | $\rightarrow$ | $\mathrm{U}^{3+}$ | $\mathrm{E}=-0.607 \mathrm{~V}$ |
| $\mathrm{UO}_{2}{ }^{2+}+\mathrm{e}$ | $\rightarrow$ | $\mathrm{UO}_{2}^{+}$ | $\mathrm{E}^{\circ}=+0.062 \mathrm{~V}$ |
| $\mathrm{UO}_{2}{ }^{2+}+4 \mathrm{H}^{+}+2 \mathrm{e}$ | $\rightarrow$ | $\mathrm{U}^{4+}+2 \mathrm{H}_{2} \mathrm{O}$ | $\mathrm{E}^{\circ}=+0.327 \mathrm{~V}$ |
| $\mathrm{UO}_{2}{ }^{2+}+4 \mathrm{H}^{+}+6 \mathrm{e}$ | $\rightarrow$ | $\mathrm{U}+2 \mathrm{H}_{2} \mathrm{O}$ | $\mathrm{E}^{\circ}=-1.444 \mathrm{~V}$ |
| $\mathrm{UO}_{2}^{+}+4 \mathrm{H}^{+}+\mathrm{e}$ | $\rightarrow$ | $\mathrm{U}^{4+}+2 \mathrm{H}_{2} \mathrm{O}$ | $\mathrm{E}^{\circ}=+0.620 \mathrm{~V}$ |

a). Assign oxidation states to the various uranium-containing species appearing in the above half-reactions.
b). By analysis of the above half-reactions, determine the ultimate chemical fate of a small piece of solid uranium placed in contact with a 1 molar solution of a strong, monoprotic acid HX, and in the presence of 1 atm of hydrogen, all at $25^{\circ} \mathrm{C}$. Provide balanced reactions and electrode potentials for all reactions. [It can be assumed that the conjugate base $\mathrm{X}^{-}$does not react perceptibly with uranium or with its compounds].
c). What is the most stable uranium-containing species at $\mathrm{pH}=6$ (and under otherwise standard conditions)?
d). Determine the pH range, for acidic or neutral solutions, under which a 1 molar solution of $\mathrm{UO}_{2}{ }^{+}$would be stable:
i). under otherwise standard conditions (i.e. $\mathrm{P}\left(\mathrm{H}_{2}\right)=1$, concentrations of other uranium-containing species $=1$ )
ii). with $\mathrm{P}\left(\mathrm{H}_{2}\right)=1.0 \times 10^{-6} \mathrm{~atm}$, and with conditions otherwise standard.

Which set of conditions is more relevant to the speciation of uranium in natural waterways?

## PROBLEM 20.

A sealed glass vessel, fitted with two tungsten filaments separated by a 5 mm gap, is filled with clean, dry air at standard temperature and pressure. An electrical discharge is established between the two filaments. Over the next several minutes, the gas within the vessel is seen to take on a distinct brownish tinge.
a). What species is responsible for the observed coloration? Estimate an upper limit to its concentration within the vessel.
b). The same brown colour is seen to develop spontaneously when oxygen and nitric oxide are introduced into an evacuated glass bulb. Write an overall equation for the reaction in the bulb.
c). The following measurements were obtained from several experiments, performed at a temperature of $25^{\circ} \mathrm{C}$ :

| $[\mathrm{NO}]$ <br> $\left(\mathrm{mol} \mathrm{L}^{-1}\right)$ | $\left[\mathrm{O}_{2}\right]$ <br> $\left(\mathrm{mol} \mathrm{L}^{-1}\right)$ | initial rate <br> $\left(\mathrm{mol} \mathrm{L}^{-1} \mathrm{~s}^{-1}\right)$ | $\mathrm{A}_{\infty}$ <br> $(\lambda=400 \mathrm{~nm})$ |
| :---: | :---: | :---: | :---: |
| $1.16 \times 10^{-4}$ | $1.21 \times 10^{-4}$ | $1.15 \times 10^{-8}$ | 0.341 |
| $1.15 \times 10^{-4}$ | $2.41 \times 10^{-4}$ | $2.28 \times 10^{-8}$ | 0.331 |
| $1.18 \times 10^{-4}$ | $6.26 \times 10^{-5}$ | $6.24 \times 10^{-9}$ | 0.335 |
| $2.31 \times 10^{-4}$ | $2.42 \times 10^{-4}$ | $9.19 \times 10^{-8}$ | 0.656 |
| $5.75 \times 10^{-5}$ | $2.44 \times 10^{-5}$ | $5.78 \times 10^{-9}$ | 0.166 |

i). Determine the reaction order in $\mathrm{O}_{2}$, in NO, and overall.
ii). Determine the reaction rate constant at 298 K .
d). The column on the far right of the above table shows the absorbance at 400 nm (path length $=10 \mathrm{~cm}$ ) after sufficient time has elapsed for the reaction mixture to have reached equilibrium.
i). Does the reaction go essentially to completion, or not?
ii). Determine the molar absorption coefficient $\varepsilon$ at the stated wavelength.
iii). Is the (visible) wavelength of maximum absorbance likely to be closest to 400,500 , or 600 nm ?
e). If the brown gas obtained in this reaction is isolated in an apparatus whose volume can be modified by a piston, the following results are obtained:

| $\mathrm{V}(\mathrm{mL})$ | $\mathrm{P}_{\text {tot }}(\mathrm{atm})$ |
| :---: | :---: |
| 1000 | $2.49 \times 10^{-3}$ |
| 500 | $4.90 \times 10^{-3}$ |
| 200 | $1.18 \times 10^{-2}$ |
| 100 | $2.25 \times 10^{-2}$ |
| 50 | $4.23 \times 10^{-2}$ |
| 20 | $9.60 \times 10^{-2}$ |
| 10 | $1.78 \times 10^{-1}$ |

The temperature of the apparatus is maintained at $25{ }^{\circ} \mathrm{C}$ for all of the above measurements. Provide a reaction equation which accounts for the dependence of pressure upon volume, and determine the appropriate equilibrium constant.
f). If the system detailed in e) is subjected to yet greater compression, the following data are obtained:

| $\mathrm{V}(\mathrm{mL})$ | $\mathrm{P}_{\text {tot }}(\mathrm{atm})$ |
| :---: | :---: |
| 10 | 0.178 |
| 5 | 0.331 |
| 2 | 0.765 |
| 1 | 1.215 |
| 0.5 | 1.215 |
| 0.2 | 1.215 |

Why does the pressure not continue to increase at volumes of 1 mL and less? Provide equations for any chemical reactions occurring, and calculate the partial pressures of any gas-phase species at $\mathrm{V}=1 \mathrm{~mL}$. What is the equilibrium constant for the process responsible for the "pressure cap" of 1.215 atm ?

## PROBLEM 21.

Investigation of the complexation reactions of transition metal ions

$$
\mathrm{M}^{\mathrm{n}+}+\mathrm{mL}^{-} \quad \rightleftharpoons \quad \mathrm{ML}_{\mathrm{m}}{ }^{(\mathrm{n}-\mathrm{m})^{+}}
$$

is often complicated by the existence of competing equilibrium processes: for example, very often the ligand $\mathrm{L}^{-}$is the conjugate base of a weak acid, and so its concentration in solution is highly pH dependent. In such circumstances it is common to reframe the transition metal complex's formation constant, $\beta_{\mathrm{m}}$ :

$$
\beta_{\mathrm{m}}=\frac{\left[\mathrm{ML}_{m}{ }^{(n-m)+}\right]}{\left[\mathrm{M}^{n+}\right]\left[\mathrm{L}^{-}\right]^{m}}
$$

by substituting, for $\left[\mathrm{L}^{-}\right]$, the parameter $\alpha_{\mathrm{L}^{-}} \mathrm{C}_{\mathrm{T}}(\mathrm{L})$, where $\mathrm{C}_{\mathrm{T}}(\mathrm{L})$ indicates the total concentration of L in all forms in solution [whether as HL or as $\mathrm{L}^{-}$or as $\mathrm{ML}_{\mathrm{i}}{ }^{(\mathrm{n}-\mathrm{i})^{+}}$] and $\alpha_{L^{-}}$is that fraction of 'total $\mathrm{L}^{\prime}$ which is in the appropriate form of $\mathrm{L}^{-}$. Such an approach is often used, for example, in titrimetric analysis involving EDTA, since EDTA ( $\mathrm{H}_{4} \mathrm{Y}$ ") is a weak tetraprotic acid which is capable of effective complexation reactions only in its fully deprotonated form, $\mathrm{Y}^{4}$. It can be shown that $\alpha_{Y^{4}}$ has the form

$$
\begin{gathered}
\alpha_{\mathrm{Y}^{4}}= \\
K_{\mathrm{a}, 1} K_{\mathrm{a}, 2} K_{\mathrm{a}, 3} K_{\mathrm{a}, 4}
\end{gathered}
$$

$$
\left[\mathrm{H}^{+}\right]^{4}+K_{\mathrm{a}, 1}\left[\mathrm{H}^{+}\right]^{3}+K_{\mathrm{a}, 1} K_{\mathrm{a}, 2}\left[\mathrm{H}^{+}\right]^{2}+K_{\mathrm{a}, 1} K_{\mathrm{a}, 2} K_{\mathrm{a}, 3}\left[\mathrm{H}^{+}\right]+K_{\mathrm{a}, 1} K_{\mathrm{a}, 2} K_{\mathrm{a}, 3} K_{\mathrm{a}, 4}
$$

where $\mathrm{K}_{\mathrm{a}, \mathrm{i}}$ is the ith acid dissociation constant of EDTA (values are, respectively, $1.02 \times 10^{-2}, 2.14 \times 10^{-3}, 6.92 \times 10^{-7}$, and $5.50 \times 10^{-11}$ ).
a). Determine values for the parameter $\alpha_{\mathrm{Y}^{4}}$ at pH 's of, respectively, 2, 6, and 10 . What is the concentration of the fully deprotonated anion $\mathrm{Y}^{4}$, in a 500 mL solution containing 3.252 g of EDTA at each of these pH values?
b). The complex formation constant $\mathrm{K}_{\mathrm{Y}}$, for complexation of $\mathrm{M}^{\mathrm{n}+}$ with $\mathrm{Y}^{4-}$, has values of $6.3 \times 10^{21}\left(\mathrm{Hg}^{2+}\right), 2.1 \times 10^{14}\left(\mathrm{Fe}^{2+}\right)$, and $5.0 \times 10^{10}\left(\mathrm{Ca}^{2+}\right)$. Which of these metal ions will form EDTA complexes at better than $99.9 \%$ yield, in a solution containing $5.00 \times 10^{-3} \mathrm{~mol} \mathrm{~L}^{-1}$ total EDTA buffered to a pH of
i). 2
ii). 6
iii). 10 ?
c). The mercuric ion, $\mathrm{Hg}^{2+}$, has a high affinity for chloride:

$$
\mathrm{Hg}^{2+}+4 \mathrm{Cl}^{-} \quad \rightleftharpoons \mathrm{HgCl}_{4}^{2-}
$$

for which the formation constant is $\beta_{\mathrm{Cl}}=3.98 \times 10^{15}$. For a solution containing $0.5 \mathrm{~mol} \mathrm{~L}^{-1}$ total chloride and $5.00 \times 10^{-3} \mathrm{~mol} \mathrm{~L}^{-1}$ total EDTA, determine the fraction of Hg existing as the free ion, as the tetrachloride anion, and as the EDTA complex, at a pH of
i). 2
ii). 6
iii). 10
[You should assume that the total metal ion concentration is much less than 0.05 $\mathrm{mol} \mathrm{L}{ }^{-1}$.]
d). An amalgam is known to contain only mercury, sodium, and calcium. 5.218 grams of the sample is treated with an appropriate oxidizing agent, and made up to 500 mL .25 mL aliquots of this solution, buffered to $\mathrm{pH}=2.6$, are titrated against a $0.0122 \mathrm{~mol} \mathrm{~L}^{-1} \mathrm{MgY}^{2-}$ solution: the mean titre value obtained is 44.19 $\mathrm{mol} \mathrm{L}{ }^{-1}$. When 10 mL aliquots are buffered to a pH of 9.5 , a titre value of 57.43 $\mathrm{mol} \mathrm{L}{ }^{-1}$ is obtained. Determine the percentage by mass of the mercury, sodium, and calcium in the amalgam.

## PROBLEM 22.

Greenhouse gas emissions are a topic of global environmental concern. The increase in atmospheric concentration of one greenhouse gas, $\mathrm{CO}_{2}$, has been welldocumented over the past several decades.
a). Let us approximate the distribution of greenhouse gases in the Earth's atmosphere by assuming that these gases $\left(\mathrm{CO}_{2}, \mathrm{H}_{2} \mathrm{O}\right.$ vapour etc) are localized within a layer between the altitudes of 10 and 11 km . [Such a description is not accurate, but serves to illustrate some concepts.] What is the effect of such a greenhouse-gas layer upon the temperature of the atmosphere at an altitude of 5 km ?
b). What is the layer's effect on atmospheric temperature at 15 km ? Explain, qualitatively, this 'side-effect' of the Greenhouse layer.
c). How does temperature change in the lower atmosphere influence the equilibria of $\mathrm{CO}_{2}$ and of $\mathrm{H}_{2} \mathrm{O}$ between the gaseous and aqueous phases? Will a shift in the positions of equilibrium for these species have any effect, itself, upon the temperature of the lower atmosphere?
d). Now we climb above the greenhouse layer to the ozone layer. Ozone is both produced and destroyed photochemically. Devise a mechanism which accounts for ozone production and destruction in a pure-oxygen atmosphere.
e). The enthalpies of formation of O and $\mathrm{O}_{3}$ are $\Delta \mathrm{H}_{\mathrm{f}}{ }_{\mathrm{f}}(\mathrm{O})=249 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and $\Delta \mathrm{H}^{\circ}{ }_{\mathrm{f}}\left(\mathrm{O}_{3}\right)=143 \mathrm{~kJ} \mathrm{~mol}^{-1}$. Determine the longest-wavelength photons capable of oxygen and ozone photolysis, respectively.
f). In polar regions, severe depletion of stratospheric ozone is seen during springtime. It is thought that conditions are 'set up' for this catastrophic depletion (known as the 'ozone hole') by several factors, including the following equilibria:

$$
\begin{array}{lll}
\mathrm{HCl}_{(\mathrm{g})}+\mathrm{PSC} & \varlimsup & \mathrm{HCl} \cdot \mathrm{PSC} \\
\mathrm{ClONO}_{2(\mathrm{~g})}+\mathrm{PSC} & \rightleftharpoons & \mathrm{ClONO}_{2} \cdot \mathrm{PSC} \\
\mathrm{ClO}_{(\mathrm{g})}+\mathrm{ClO}_{(\mathrm{g})} & = & \mathrm{ClOOCl}_{(\mathrm{g})} \tag{3}
\end{array}
$$

Here PSC denotes a 'polar stratospheric cloud', resulting from condensation of water vapour and other volatiles at elevated altitudes. PSC formation is common in the Antarctic stratosphere during winter and early spring, but less so in the Arctic where temperatures are not quite so low. It is known that ozone depletion is more severe the further the above equilibria lie to the right hand side. Bearing in mind that bond formation is generally exothermic, how will the above equilibria be affected by temperature?
g). Ozone hole formation in the Arctic stratosphere is a recently-noted phenomenon: it was originally expected that the Arctic would be 'immune' to ozone hole formation, but this is evidently not the case. Based on information supplied above, suggest which of the following strategies could conceivably account for the development of the Arctic ozone hole:
i). Northern hemisphere levels of stratospheric CFC have only very recently risen to levels which the Antarctic stratosphere had already experienced a decade ago; or
ii). The continued influx of greenhouse gases into the lower atmosphere is continuing to reduce the temperature of the Arctic stratosphere; or
iii). An increase in the concentration of water vapour in the Arctic stratosphere makes PSC formation more favourable than was previously the case; or
iv). An increase in the amount of IR radiation reaching the Arctic stratosphere is causing increased photolysis of the Arctic ozone.

## PROBLEM 23.

"Queenbee substance" $\mathbf{Q}$ contains $65.2 \%$ carbon and $8.75 \%$ hydrogen and no other element except oxygen. $\mathbf{Q}$ is known to be acidic and titration of 43.7 mg of this compound required 23.7 mL of 0.0100 M aqueous sodium hydroxide to reach the equivalence point. The molecular weight of $\mathbf{Q}$ was determined to be less than 200.
a). What is the molecular formula of $\mathbf{Q}$ and what functional groups might be responsible for the acidity of this compound?

Q reacts with hydrogen in the presence of finely divided platinum metal to afford a new compound $\mathbf{A}$. Further reduction of $\mathbf{A}$ with sodium borohydride in ethanol gives substance B. Compound $\mathbf{B}$ was readily dehydrated upon warming with strong sulfuric acid to afford an alkene $\mathbf{C}$. The ${ }^{13} \mathrm{C} \mathrm{nmr}$ of $\mathbf{C}$ revealed amongst other features the presence of a methyl group attached to a double bond.
b). What functional groups are consistent with the above reactions?

Ozonolysis of $\mathbf{C}$ followed by an oxidative work up gave only two fragments, ethanoic acid and a straight chain dicarboxylic acid $\mathbf{D}$. Similar cleavage of $\mathbf{Q}$ itself yielded oxalic acid (ethanedioic acid) and a substance $\mathbf{E}$ which contained a carboxylic acid group.
c). Deduce the structures for $\mathbf{D}$ and $\mathbf{E}$ and hence give the possible structures for $\mathbf{Q}$.

## PROBLEM 24.

Chrysophanic acid is a naturally occurring anthraquinone pigment isolated from the rhubarb root and has the structure shown below. One rather elegant synthesis of this molecule originated in the Research School of Chemistry at the Australian National University.


3-Methylanisole (3-methyl-methoxybenzene) was reduced with lithium metal in a mixture of liquefied anhydrous ammonia, tetrahydrofuran and $t$-butanol to afford B. $\left(\mathrm{C}_{8} \mathrm{H}_{12} \mathrm{O}\right)$. Treatment of $\mathbf{B}$ with potassium amide in anhydrous liquid ammonia followed by aqueous work up resulted in its isomerisation to $\mathbf{C}$.
a). Draw all three possible structures for $\mathbf{C}$.

The ${ }^{1} \mathrm{H} \mathrm{nmr}$ spectrum of $\mathbf{C}$ revealed amongst other features two olefinic protons which were not adjacent to one another. In addition it revealed two vicinal methylene groups one of which was adjacent to an olefinic proton.
b). Draw the structures of $\mathbf{C}$ which fit this information.

Reaction of $\mathbf{C}$ with 5-hydroxy-naphthalene-1,4-dione afforded the Diels Alder adduct $\mathbf{D}\left(\mathrm{C}_{18} \mathrm{H}_{18} \mathrm{O}_{4}\right)$. The ${ }^{1} \mathrm{H}$ nmr. spectrum of $\mathbf{D}$ exhibited amongst other features a resonance $\delta 10.5$ integrating for 1 proton and indicative of an intramolecularly bonded hydroxyl group.
c). Suggest three possible structures for compound $\mathbf{D}$.

Enolisation of $\mathbf{D}$ by treatment with potassium carbonate in hot methanol followed by oxidation with the potassium nitrosodisulfonate (Fremy's salt) yielded a yellow orange coloured quinonoid product $\mathbf{E}$. $\left(\mathrm{C}_{18} \mathrm{H}_{16} \mathrm{O}_{4}\right)$. The ${ }^{13} \mathrm{C} \mathrm{nmr}$. spectrum of $\mathbf{E}$ contained a total of 9 resonances attributable to quaternary carbons. Pyrolysis of $\mathbf{E}$ at $180^{\circ}$ for 15 minutes resulted in the extrusion of ethene via a retro-Diels Alder reaction resulting in the formation of $\mathbf{F}\left(\mathrm{C}_{16} \mathrm{H}_{12} \mathrm{O}_{4}\right)$. The ${ }^{1} \mathrm{H} \mathrm{nmr}$. spectrum of $\mathbf{F}$ exhibited amongst other features 3 singlets each integrating for 1 proton (the lowest of these was at $\delta 11.00$ ) and two 3 proton singlets, one at $\delta 4.01$ and one at $\delta 2.25 \mathrm{ppm}$.
d). Based on this evidence suggest possible structures for compounds $\mathbf{E}$ and $\mathbf{F}$.

When $\mathbf{F}$ was treated with boron trichloride in dichloromethane at $-10^{\circ}$, it afforded, after work up, an orange coloured solid, the mass spectrum of which gave a molecular ion at $\mathrm{m} / \mathrm{e} 254$. This was found to be identical with natural chrysophanic acid.
e). Using the work you have done above draw a complete set of structures tracing out the total synthesis of chrysophanic acid.

## PROBLEM 25.

The so called Claisen type rearrangements provide versatile tools to the synthetic organic chemist. To the student however these reactions are often difficult to recognise and require some thought to understand. A practical example of this reaction is shown below. Study this for a moment and then try the following problem which involves amongst other things an example of this reaction.


In 1977 a sesquiterpene furan (K)was isolated from an Australian soft coral Sinularia gonatodes. This compound was found to inactivate bee venom and the fact that such a simple compound might act as an anti-inflammatory agent prompted considerable interest from synthetic chemists. One such synthesis is described below.

The $\operatorname{acid}(\mathbf{A})$ was esterified with 2-(trimethylsilyl)ethanol $\left[\mathrm{Me}_{3} \mathrm{Si} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{OH}\right]$ and the resulting keto-ester selectively reduced at the ketone carbonyl with $\mathrm{NaBH}_{4} / \mathrm{CeCl}_{3}$ to afford a compound $\mathbf{B}\left(\mathrm{C}_{14} \mathrm{H}_{22} \mathrm{O}_{4} \mathrm{Si}\right)$.


A

Treatment of B with 1,1,1-trimethoxyethane in the presence of a trace of anhydrous acid afforded an intermediate compound which underwent a Claisen like rearrangement on heating to afford $\mathbf{C}$. Spectroscopic examination of $\mathbf{C}$ revealed the presence of a trimethylsilylethyl ester and a methyl ester.
a). Deduce the structures of compounds $\mathbf{B}$ and $\mathbf{C}$ and the intermediate which leads to C.

Reduction of $\mathbf{C}$ with lithium borohydride yielded a primary alcohol D $\left(\mathrm{C}_{16} \mathrm{H}_{26} \mathrm{O}_{4} \mathrm{Si}\right)$ which could be oxidised with pyridinium chlorochromate to yield $\mathbf{F}$ Reaction of $\mathbf{F}$ with the Wittig reagent $\mathbf{G}$ yielded two isomers $\mathbf{H}$ and $\mathbf{I}$. the major product $\mathbf{H}$ had the (E)-stereochemistry.


G
b). Give structures for the compounds D - I, being careful to show the correct stereochemistry for isomer $\mathbf{H}$ and $\mathbf{I}$.

A final Wittig reaction with the ylid derived from methyl triphenylphosphonium iodide afforded $\mathbf{J}$ which after cleavage of the trimethylsilylethyl ester with tetra-nbutyl ammonium fluoride yielded the desired compound $\mathbf{K}$.
c). Give structures to complete the synthetic sequence.

## PROBLEM 26.

Mentors Note: The following reactions are those which fall outside "normal" high school level chemistry, and may be useful in any of the tasks of the 30th IChO. Whilst an understanding of mechanism may help the student, mechanisms are not considered essential for the tasks. However it is anticipated that students will be aware of stereo and regiochemical outcomes associated with these reactions.

REDUCTIONS (Assume a standard aqueous or pH adjusted work up in each case)
(i)

(ii)

(iii)

(iv)

(v)

(vi)


(note: diimide $\mathrm{NH}=\mathrm{NH}$ is generated by oxidation of hydrazine)
(vii)



## OXIDATIONS

(ix)

(x)

(xi)

(xii)


(xiii)

(i) $\mathrm{O}_{3}$
(ii) $\mathrm{KMnO}_{4}$
(xiv)


(xv)

(xvi)


## OTHER REACTIONS

(xvii)

(xviii)

(xix)

(xx)

(xxi)


(xxiii)


(xxiv)

(xxv)

(xxvi)
 PhS ${ }^{-}$


Additional Notes: With the exception of (xiii), (xvi) it is expected that students could derive an IUPAC name for the starting materials. With the exception of (xiv), (xiii), (xx), (xxii), (xxiii), (xvii) a similar expectation would hold true for naming products.

## PROBLEM 27-EXPERIMENTAL

## Synethsis of $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Cl}\right] \mathrm{Cl}_{2}$ and of the linkage isomers $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{ONO}\right] \mathrm{Cl}_{2}$ and $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{NO}_{2}\right] \mathrm{Cl}_{2}$.

## a). Preparation of $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Cl}\right] \mathrm{Cl}_{2}$

Dissolve 10.0 g of ammonium chloride in 60 mL of concentrated aqueous ammonia (CARE!) in a 500 mL Erlenmeyer flask. While continuously agitating the solution with a magnetic stirrer, add 20 g of finely powdered cobalt chloride 6-hydrate in small portions (CAUTION: avoid exposure to this powder. Grind with care in a fumehood).

With continued stirring of the resultant brown slurry, slowly add 16 mL of $30 \%$ hydrogen peroxide (CARE!) from a dropping funnel. When the effervescence has ceased, slowly add 60 mL of concentrated HCl .

Continue stirring on a hot plate, holding the temperature at about $85^{\circ} \mathrm{C}$ for 20 min ; then cool the mixture to room temperature and filter off the precipitated $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Cl}\right] \mathrm{Cl}_{2}$. Wash with 40 mL of ice water in several portions, followed by 40 mL of cold 6 M HCl . Dry the product in an oven at $100^{\circ} \mathrm{C}$ for several hours. The yield is about 18 g of purple product.

This complex can be recrystallised from boiling water to provide small dark purple crystal;s in high yield, but this is not necessary for the following sysnthesis.

## b). Preparation of $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{ONO}\right] \mathrm{Cl}_{2}$ and $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{NO}_{2}\right] \mathrm{Cl}_{2}$

Dissolve 10 g of $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Cl}\right] \mathrm{Cl}_{2}$ in a solution of 15 mL of concentrated aqueous ammonia (CARE!) in 160 mL of water while stirring and heating. Filter off any slight precipitate of cobalt oxide that may form, and cool the filtrate to about $10^{\circ} \mathrm{C}$.

Titrate the solution, with continuous cooling, with 2 M HCl until it is just neutral to litmus. The solution will change colour to wine-red.

Dissolve 10.0 g sodium nitrite in the solution, then add 10 mL of 6 M HCl . Allow the solution to stand in an ice bath for an hour or two, and filter off the precipitated pink crystals of $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{ONO}\right] \mathrm{Cl}_{2}$. Wash with 50 mL of ice water, followed by 50 mL of ethanol, and air dry at room temperature. The yield is about 9 g .

Store cool and in the dark. Upon standing, isomerisation to the nitrito isomer to the nitro isomer slowly occurs.

To prepare a pure sample of the nitro isomer, dissolve 4.0 g of $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{ONO}\right] \mathrm{Cl}_{2}$ in 40 mL of hot water containing a few drops of aqueous ammonia, and then add, while cooling, 40 mL of concentrated HCl . Cool the solution in an ice bath and filter off the orange $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{NO}_{2}\right] \mathrm{Cl}_{2}$. Wash the product with 25 mL of ethanol and air dry at room temperature. The yield is about 3.5 g of orange-yellow product.

## PROBLEM 28 - EXPERIMENTAL

Anion exchange chromatography separation of cobalt and nickel followed by EDTA titration of the metals using back-titration.

Cobalt and nickel are separated on a strong-base anion exchange column (chloride form) by eluting with 9 M HCl and 3 M HCl , respectively. In 9 M HCl , the nickel does not form an anionic chloro complex while the cobalt does; hence, the former will elute. In 3 M HCl , the blue, anionic cobalt chloro complex is dissociated to form the pink aquated cobalt cation, which elutes. Following separation, the metals are titrated indirectly with standard EDTA for quantitation; excess EDTA is added and the unreacted EDTA is back-titrated with a standard zinc solution in slightly acid solution, using xylenol orange indicator.
Separation:

$$
\begin{aligned}
& \mathrm{Ni}^{2+}+\mathrm{Cl}^{-} \rightarrow \mathrm{NiCl}^{+} \\
& \mathrm{Co}^{2+}+4 \mathrm{Cl}^{-} \rightarrow \mathrm{CoCl}_{4}^{2-}
\end{aligned}
$$

Titration:

$$
\begin{aligned}
& \mathrm{Co}^{2+}+\mathrm{H}_{2} \mathrm{Y}^{2-} \rightarrow \mathrm{CoY}^{2-}+2 \mathrm{H}^{+} \\
& \mathrm{Ni}^{2-}+\mathrm{H}_{2} \mathrm{Y}^{2-} \rightarrow \mathrm{NiY}^{2-}+2 \mathrm{H}^{+} \\
& \mathrm{H}_{2} \mathrm{Y}^{2-}+\mathrm{Zn}^{2+} \rightarrow \mathrm{ZnY}^{2-}+2 \mathrm{H}^{+}(\text {back-titration })
\end{aligned}
$$

End point:

$$
\begin{array}{ll}
\mathrm{H}_{4} \mathrm{In}+\mathrm{Zn}^{2+} \rightleftharpoons & \mathrm{ZnIn}^{2-}+4 \mathrm{H}^{+} \\
\text {yellow-green } & \text { red-violet }
\end{array}
$$

## Solutions and Chemicals Required

Miscellaneous. $3 \mathrm{M} \mathrm{NaOH}, 9 \mathrm{M} \mathrm{HCl}, 3 \mathrm{M} \mathrm{HCl}, 0.5 \%$ (wt/vol) xylenol orange indicator in $10 \%$ ethanol ( 0.5 g dissolved in 10 mL ethanol and diluted to 100 mL with water-must be fresh), zinc granules, $0.2 \%$ phenolphthalein in $90 \%$ ethanol, hexamine (hexamethylenetetramine), Dowex 1-X8 anion exchange resin (chloride form) or equivalent.

Standard 0.01 M EDTA solution. Prepare from $\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{Y} 2 \mathrm{H}_{2} \mathrm{O}$ dried at $80^{\circ} \mathrm{C}$ for 2 hours and cooled in a desiccator by accurately weighing about 1.9 g (to the nearest milligram), dissolving in distilled deionized water, and diluting to 500.0 mL in a volumetric flask. Calculate the molarity.

Standard 0.01 M zinc solution. Accurately weigh approximately 0.33 g pure zinc granules (to the nearest 0.1 mg ) and transfer to a $400-\mathrm{mL}$ beaker. Do not use zinc dust. For highest accuracy, the zinc granules should be treated with 2 M HCl to remove any zinc oxide coating. Decant the acid and wash the zinc repeatedly with water. Then, wash several times with ethanol and finally with ether in the fume hood (FIRE HAZARD). Dry the granules before weighing. Dissolve with the minimum amount of HCl required. Heat on a steam bath to aid dissolution. Cover with a watch glass during dissolution. After the zinc is in solution, wash the droplets of water on the watch glass with distilled water into the beaker, wash down the sides of the beaker and quantitatively transfer the solution to a $500-\mathrm{mL}$ volumetric flask. Dilute to volume with distilled water. Calculate the molarity of the solution.

## Procedure

1. Preparation of the ion exchange column. Prepare a column using a $50-\mathrm{mL}$ burette with glass wool in the bottom to hold the resin. Add a slurry of Dowex 1-X8 anion exchange resin (in the chloride form) in 9 M HCl to the burette until
the height of the resin column is about $15-20 \mathrm{~cm}$. Do not allow the liquid level to drop below the resin level. Keep about 2 mL of liquid above the resin.

Wash the column with two $10-\mathrm{mL}$ portions of 9 M HCl using a flow rate of 2 or 3 mL per minute. The column will darken somewhat when treated with HCl , but it will return to normal colour if washed with water. Leave $2-3 \mathrm{~cm}$ of HCl above the resin level.
2. Separation of the unknown mixture. Obtain an unknown from your instructor in a $50-\mathrm{mL}$ volumetric flask. Dilute to volume with 9 M HCl . The unknown will contain 5 mmol or less each of nickel(II) and cobalt(II) in 9 M HCl .

Add with a pipette 2 mL of the unknown solution onto the column. Elute the nickel with about 75 mL 9 M HCl added in $15-\mathrm{mL}$ portions, using a flow rate of $1-2 \mathrm{~mL}$ per minute. Collect in a $250-\mathrm{mL}$ Erlenmeyer flask. The pale yellow-green $\mathrm{NiCl}^{+}$complex will flow through the column and may darken the resin. The blue cobalt band (appears green due to yellow resin) will move partway down the column. While the sample is being eluted, it is advisable to perform a practice titration as described below.

After all the nickel is eluted but before the cobalt band reaches the end of the column, stop the flow and replace the collection flask with a clean one. Elute the cobalt with about five $10-\mathrm{mL}$ portions of 3 M HCl , at a flow rate of 1 mL per minute. As the HCl is diluted on the column, the $\mathrm{CoCl}_{4}{ }^{2-}$ complex should dissociate to the pink coloured $\mathrm{Co}^{2+}$. After the cobalt is seen to be eluted, stop the flow and proceed to titrate the separated metals. (Final elution with water may be used to assure complete removal of the cobalt.)
3. Titration of the nickel and cobalt. Carefully evaporate the collected samples to near dryness on a hot plate (FUME HOOD). Cool and dilute with 50 mL distilled deionized water. Before titrating your unknown samples, and while they are evaporating, perform a practice titration or two using a prepared cobalt or nickel solution. Titrate the nickel and cobalt solutions indirectly as follows. Neutralize each solution to a phenolphthalein end point with 3 M NaOH , avoiding excess NaOH . Add 6 M HCl dropwise to just remove the red indicator colour. Add 25.00 mL standard 0.01 M EDTA to the flasks, and add five drops $9 \mathrm{M} \mathrm{HCl}, 1 \mathrm{~g}$ hexamine, and four drops xylenol orange indicator solution. The hexamine buffers the solution at $\mathrm{pH} 5-6$. If the solution is red-violet, warm and add another 10.00 mL EDTA. Back-titrate with standard 0.01 M zinc solution until the indicator changes from yellow-green to red-violet.

## Calculations

From the millimoles EDTA taken and the number of millimoles excess EDTA found in the back-titration, calculate and report the number of millimoles nickel and cobalt in your unknown.

## PROBLEM 29 - EXPERIMENTAL

## Determination of copper and barium in a mixture of chlorides.

Copper and barium are common components in high temperature superconductors. They are easily separated by removing barium as its insoluble sulfate which is determined gravimetrically. The soluble copper can be determined volumetrically by reaction with excess iodide ion and subsequent estimation of liberated iodine with standardized thiosulfate.

Separation

$$
\mathrm{Ba}^{2+}+\mathrm{SO}_{4}{ }^{=} \rightarrow \mathrm{BaSO}_{4} \downarrow
$$

Titration

$$
\begin{aligned}
& 2 \mathrm{Cu}^{2+}+4 \mathrm{I}^{-} \rightarrow 2 \mathrm{CuI}+\mathrm{I}_{2} \\
& \mathrm{I}_{2}+\mathrm{S}_{2} \mathrm{O}_{3}{ }^{=} \rightarrow 2 \mathrm{I}^{-}+\mathrm{S}_{4} \mathrm{O}_{6}=
\end{aligned}
$$

## Solutions and Chemicals Required

Miscellaneous: $10 \% \mathrm{KI}$ solution, $10 \% \mathrm{KSCN}$ (or $\mathrm{NH}_{4} \mathrm{SCN}$ ). Starch indicator, saturated $\mathrm{K}_{2} \mathrm{SO}_{4}$.

Standard 0.1 M Na $\mathbf{N}_{2} \mathbf{S}_{2} \mathbf{O}_{3}$. This is made by dissolving 25.0 g of AR $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3} .5 \mathrm{H}_{2} \mathrm{O}$ in 1 L of "boiled out" distilled water in a volumetric flask. Solutions are best used fresh unless stabilised.

Standardise your sodium thiosulphate against either potassium iodate or potassium bromate as primary standards. This can be found in any text on volumetric or quantitative analysis.

## Procedure

1. Accurately weigh approximately 3 g of your "unknown" sample (The "unknown" should contain $\mathrm{CuCl}_{2}$ and $\mathrm{BaCl}_{2}$ in a ratio between $3: 1$ and $8: 3$ ). Using a 400 mL beaker, dissolve the solid in 180 mL of water. (Do note use more as your final volume will be 250 mL - see later).
2. Precipitation. Heat the solution nearly to boiling and keep the solution just below the boiling point. Add slowly from a Pasteur pipette 10 mL of saturated $\mathrm{K}_{2} \mathrm{SO}_{4}$ solution; stir vigorously throughout the addition. Let the precipitate settle, then test for complete precipitation by adding a few drops of potassium sulfate without stirring. If additional precipitate forms, add slowly, with stirring, 5 mL more potassium sulfate; let settle, and test again. Repeat this operation until precipitation is complete. Leave the stirring rods in the beakers, cover with watch glasses, and digest on the steam bath until the supernatant liquid is clear. (The initial precipitate is fine particles. During digestion, the particles grow to filterable size.) This will require $30-60$ minutes or longer. Add more distilled water if the volume falls below 200 mL .
3. Filtration and washing of the precipitate. Prepare an $11-\mathrm{cm}$ No. 42 Whatman hardened, ashless filter paper or equivalent for filtration; the paper should be well fitted to the funnel so that the long stem of the funnel remains filled with distilled water, or the filtration will be very slow. Filter the solutions while hot; be careful not to fill the paper too full, as the barium sulfate has a tendency to "creep" above the edge of the paper. Wash the precipitate into the filter with hot distilled water, clean the adhering precipitate from the stirring rod and beaker with the rubber "policeman" (!), and again rinse the contents of the beaker into the filter. Examine the beaker very carefully for particles of precipitate that may have escaped transfer. Wash the precipitate and the filter paper with hot distilled water until no turbidity appears when a few millilitres of the washings, acidified with a few drops of concentrated nitric acid (CARE!), are tested for chloride with silver nitrate solution. During the washing, rinse the precipitate down into the cone of the filter as much as possible. Examine the filtrate for any precipitate that may have run through the filter. When the precipitate has been thoroughly washed you should test one drop with concentrated ammonia solution (CARE!) on a white tile. The absence of any visible blue colour shows that all the copper has been removed from the precipitate. If a blue colour appears, the washing and testing should be repeated.

Quantitatively transfer the cool filtrate to a 250 mL volumetric flask and make up to volume. Mix thoroughly.
4. Titration: Pipette 50.0 mL of this solution into a 250 mL conical flask, add 2 drops of glacial acetic acid (CARE!) followed by 15 mL of $10 \% \mathrm{KI}$. Titrate the liberated iodine with standard 0.1 M thiosulfate until the brown iodine colour just fades. Then add 2 mL of starch indicator and continue the titration until the blue colour commences to fade. At this point add $\sim 10 \mathrm{~mL}$ of $10 \%$ potassium (or ammonium) thiocyanate whereupon the blue colour will intensify. Complete the
titration as quickly as possible. When the blue colour has gone, a pale coloured precipitate should remain. A distinct and readily determined endpoint is easily achieved.

Repeat on two further aliquots or until agreement is reached.
You can, if you wish, determine the barium by gravimetric analysis as follows.
5 Ignition and weighing of the precipitate. Loosen the filter paper in the funnels and allow to drain for a few minutes. Fold each filter into a package enclosing the precipitate, with the triple thickness of paper on top. Place into weighed porcelain crucibles and gently press down into the bottom. Inspect the funnels for traces of precipitate; if any precipitate is found, wipe it off with a small piece of moist ashless filter paper and add to the crucible. Place each crucible on a triangle on a tripod or ring stand, in an inclined position with the cover displaced slightly. Heat gently with a small flame from a gas burner (CARE!) until all the moisture has been driven off and the paper begins to smoke and char. Adjust the burner so that the paper continues to char without catching fire. If the paper inflames, cover the crucible to smother the fire, and lower the burner flame. When the paper has completely carbonised and no smoke is given off, gradually raise the temperature enough to burn off the carbon completely. A red glowing of the carbon as it burns is normal, but there should be no flame. The precipitate should finally be white with no black particles. Allow to cool. Place the crucible in a vertical position in the triangle, and moisten the precipitate with three or four drops of dilute (1:4) sulfuric acid. Heat very gently until the acid has fumed off. (This treatment converts any precipitate that has been reduced to barium sulfide by the hot carbon black to barium sulfate.) Then, cover the crucibles and heat to dull redness in the full flame of the burner for 15 minutes.

Allow the covered crucibles to cool in a desiccator for at least one hour and then weigh them. Heat again to redness for 10-15 minutes, cool in the desiccator, and weigh again. Repeat until two successive weighings agree within 0.3-0.4 mg.

## Calculation

Copper. From the volume of standard thiosulfate used, calculate the millimoles of iodine and hence copper present in the 50.0 mL aliquot. Since the sample was taken from a total of 250.0 mL the total copper in millimoles will be 5 times that estimated in the titration.

Barium. The total barium in millimoles follow directly from the mass of barium sulfate.

Report your result as a ratio of $\mathrm{Cu}: \mathrm{Ba}$.

## PROBLEM 30 - EXPERIMENTAL

## Preparation and analysis of potassium trisoxalatoferrate(III) trihydrate, $\mathbf{K}_{3}\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right] \cdot \mathbf{3} \mathbf{H}_{2} \mathrm{O}$

## Introduction

In this experiment, you will prepare the complex trisoxalatoferrate(III) $\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right) 3^{3-}$ anion and isolate it as its hydrated potassium salt, $\mathrm{K}_{3}\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}$. This trihydrate is a green crystalline salt, soluble in hot water but rather insoluble when cold. The complex anion is photo-sensitive. This means that upon exposure to light of an appropriate wavelength ( $<450 \mathrm{~nm}$ in this case) the $\left.\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$ undergoes an intramolecular redox reaction in which the Fe (III) atom is reduced to $\mathrm{Fe}(\mathrm{II})$ while one of the oxalate groups is oxidised to $\mathrm{CO}_{2}$. You will be carrying out such a photo reduction on your sample, as well as applying the photo reaction to make a "blueprint".

Finally, you will also analyse your product for water of crystallisation, oxalate and iron.

WARNING: Oxalate ion is toxic and the analysis procedure for iron uses zinc that has been amalgamated with mercury. Be sure to discard any residues that contain or mercury in a responsible manner!.

## Preparation of $\mathrm{K}_{3}\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{\mathbf{4}}\right)_{3}\right] \cdot \mathbf{3} \mathbf{H}_{2} \mathrm{O}$

Weigh approximately 9.0 g of hydrated potassium oxalate $\left(\mathrm{K}_{2} \mathrm{C}_{2} \mathrm{O}_{4} \cdot \mathrm{H}_{2} \mathrm{O}\right)$ into a 250 mL beaker; add 30 mL of distilled water and heat to dissolve (do not boil).

In a second small beaker dissolve 4.4 g of $\mathrm{FeCl}_{3} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ in the minimum amount of cold water $(10-15 \mathrm{~mL})$. Add the $\mathrm{FeCl}_{3} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ solution to the warm oxalate solution and stir with a glass rod. Allow the product to crystallise (away from strong sunlight) by cooling the solution in an ice-water mixture.

Collect the crystalline product by vacuum filtration (discard the filtrate in an appropriate residue bottle). Wash the crystals with about 10 mL acetone and continue suction for a few more minutes until dry.

Recrysallisation: Weigh 5.0 g of your $\mathrm{K}_{3}\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}$ into a small beaker. Add 13 mL of distilled water and warm the mixture on a hot plate until the solid dissolves. Filter the solution quickly by vacuum filtration, wash the filter with no more than 2 mL hot distilled water and immediately transfer the hot filtrate to a clean beaker. Cool the solution in an icebath and when crystallization is complete, filter the crystals and wash twice with 5 mL quantities of ice-cold
distilled water. Dry the crystals by suction. Transfer them to a preweighed container and dry at $50^{\circ} \mathrm{C}$ for about thirty minutes. Weigh the purified product.

## Photochemical Reaction of $\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right) 3^{3-}$

As mentioned above, light causes an internal electron-transfer reaction to occur in the $\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}{ }^{3-}$ ion, producing $\mathrm{CO}_{2}$ and $\mathrm{Fe}^{2+}$ ions. The $\mathrm{Fe}^{2+}$ that is produced can readily be detected by adding a solution of potassium ferricyanide $\mathrm{K}_{3} \mathrm{Fe}(\mathrm{CN})_{6}$ ( 0.1 M ) whereupon a deep blue colour should result, due to the formation of the complex ferroferricyanide (Turnbull's blue). For this exercise you will need a bright light source (CAUTION!) such as a 150W spot lamp. Bright sunlight may suffice but the photochemical reactions will be significantly slower.

CAUTION must be exercised in using the ferricyanide solution. Avoid contact with your skin and collect all residues for disposal or recovery. Thoroughly was your hands following handling.

Dissolve 0.7 g of your complex (it doesn't have to have been recrystallized) in 100 mL of distilled water in a conical flask. Add 3 mL of $2 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ and swirl the mixture. To each of three labelled test tubes, add 10 mL of this solution.

Keep one tube away from the light source as the control and irradiate the remaining two tubes with the light source for 1 and 5 minutes, respectively.

To all 3 tubes now add 1 mL of the potassium ferricyanide solution $\left(\mathrm{K}_{3} \mathrm{Fe}(\mathrm{CN})_{6}\right)$.
Record and explain your observations. To convince yourself it is $\mathrm{Fe}^{2+}$ that is being detected, add a few drops of ferricyanide solution to a test tube containing 5 mL of iron(II) sulfate $\left(\mathrm{FeSO}_{4}\right)$ solution.

## Blueprinting

Pour about 25 mL of the $\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}{ }^{3-}$ solution you have prepared previously into a petri-dish. Thoroughly soak a $5 \mathrm{~cm} \times 5 \mathrm{~cm}$ piece of filter paper in this solution. Using plastic tongs, remove the filter paper and allow to drip dry in a fume cupboard with the light out.

When the treated paper is dry, lay it flat about 75 mm below the lamp and place some small opaque objects (coins, keys, etc.) on the paper.

Irradiate for a few minutes and dip the paper into another petri-dish containing about 25 mL of potassium ferricyanide solution (CAUTION!), using the plastic tongs. Remove the developed "blueprint" and dip in a beaker of distilled water to wash off excess ferricyanide solution.. Explain your observations.

## Analysis of the Complex for Oxalate

Preparation of $\mathbf{0 . 0 4 M} \mathbf{K M n O}_{4}$ solution: Dissolve 6.3 g A.R. $\mathrm{KMnO}_{4}$ in 1 L of distilled water. If the solution is not to be used immediately, gently boil it for about 1 hour. Cover and let stand overnight. Remove any precipitated $\mathrm{MnO}_{2}$ by filtration through a fine porosity filtering crucible or sintered glass funnel. The solution should be stored in the dark when not in use.

Standardization of $\mathbf{0 . 0 4 M} \mathbf{K M n O}_{4}$ solution: Accurately weigh approx. 3.2 g of finely powdered A.R. sodium oxalate $\left(\mathrm{Na}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right)$ into a 250 mL beaker. Dissolve the sodium oxalate completely in the minimum amount of warm distilled water (about 100 mL ). Quantitatively transfer the solution to a 250 mL volumetric flask, and make up to the mark with distilled water.

Pipette 25.0 mL of this solution into a clean 250 mL conical flask and add 25.0 mL of 1 M sulfuric acid. Warm the solution to about $60^{\circ} \mathrm{C}$ (as a rough guide, 60 ${ }^{\circ} \mathrm{C}$ is the temperature at which the flask is just a little too hot to hold in the hand comfortably (CAUTION!). Titrate the warm solution with the $0.04 \mathrm{M} \mathrm{KMnO}_{4}$ until a faint pink colour persists after 30 seconds.

Repeat the determination until triplicate titrations agree to better than 0.1 mL . Average your results and calculate the molarity of the $\mathrm{KMnO}_{4}$ solution.

Analysis for water: Clean and dry a small Petri dish or watchglass. Place the dish in a microwave oven on high for about one minute. CAUTION: The microwave oven should contain some "ballast" to prevent damage to the oven eg a beaker of sand or silica gel. A conventional oven, set to $110^{\circ} \mathrm{C}$ will of course do as well - the drying process just takes a little longer. Cool in a desiccator and accurately weigh the dish or watchglass.

Accurately weigh approximately 1.0 g of recrystallized complex into the dish and heat in the microwave oven on high for 5 minutes. Cool and weigh. Repeat this process until the sample has come to constant weight. The loss of weight is due to removal of lattice water (water of crystallization). Calculate the percentage of lattice water in your sample of complex.

## Analysis for oxalate and iron:

The oxalate ligands in the tris(oxalato)ferrate(III) complex are oxidized by titration with permanganate:
$5 \mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}{ }^{3-}+2 \mathrm{MnO}_{4}^{-} \rightarrow 5 \mathrm{Fe}^{3+}+2 \mathrm{Mn}^{2+}+10 \mathrm{CO}_{2}+8 \mathrm{H}_{2} \mathrm{O}$
The iron(III) is reduced with an excess of zinc-amalgam (zinc metal coated with metallic mercury) to Fe(II):

$$
2 \mathrm{Fe}^{3+}+\mathrm{Zn}(\mathrm{Hg}) \rightarrow 2 \mathrm{Fe}^{2+}+\mathrm{Zn}^{2+}+\mathrm{Hg}
$$

The $\mathrm{Fe}^{2+}$ that is formed is quantitatively reoxidized to iron(III) by titration with standard permanganate:
$5 \mathrm{Fe}^{3+}+\mathrm{MnO}_{4}^{-}+8 \mathrm{H}^{+} \rightarrow 5 \mathrm{Fe}^{3+}+\mathrm{Mn}^{2+}+4 \mathrm{H}_{2} \mathrm{O}$
Note that any iron(II) impurity in your sample would also be titrated in this step.
In summary, on a weighed sample of your complex:

1. oxalate is firstly determined by permanganate titration,
2. the Fe (III) in the resulting titration solution is reduced to Fe (II) by excess zinc-amalgam, and finally,
3. $\mathrm{Fe}(\mathrm{II})$ is determined by permanganate titration.

## Procedure

Accurately weigh approximately 0.40 g of recrystallized complex and dissolve the sample in 25 mL of 1 M sulfuric acid in a 100 mL conical flask. Warm the solution to $60^{\circ} \mathrm{C}$ and determine the amount of oxalate in the solution by titration with standardized $0.04 \mathrm{M} \mathrm{KMnO}_{4}$ as previously. Do not titrate past the endpoint! Cool the titration solution and quantitatively transfer it into a bottle containing zinc amalgam. Shake the bottle for two minutes and carefully decant the reduced solution into a 250 mL conical flask. Wash the amalgam thoroughly by shaking it with three successive 30 mL portions of a mixture of equal volumes of distilled water and $1 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$. Add the washings to the conical flask and determine the amount of iron(II) in the solution by titration with standardized $\mathrm{KMnO}_{4}$ at room temperature.

Calculate the percentages of iron and oxalate in your sample.

## Worked solutions to the problems

## PROBLEM 1.

a).


Cyclobutadiene


Butatriene
b). The hybridization at each carbon atom is as below:


The central $\mathrm{C}=\mathrm{C}$ bond is between two carbons of $s p$ hybridization; other $\mathrm{C}=\mathrm{C}$ bonds are between an $s p$-hybridized and an $s p^{2}$-hybridized C atom. The greater the proportion of $s$-character in the hybridized orbital, the more 'squat' is the orbital and hence the shorter the $\sigma$-bond which results. Therefore the central $\mathrm{C}=\mathrm{C}$ bond is shorter than the other two.
c).


Tetrahedrane
d). (i) one
(ii) one
(iii) one
e). (i) Arguably three:


I


II


III

Since cyclobutadiene is not aromatic, I and II aren't properly different canonical forms but are distinct isomers (nevertheless, they may not exist separately).
(ii) Three:

I

II

III
(iii) One:

f). The melting points of the isomers should correlate with their dipole moments. By symmetry, II has zero dipole moment and so has the lowest melting point. Of the other two, III will have a larger dipole moment than I (because the dipole in III lies along the long horizontal axis, whereas that in I lies along the short vertical axis) So III will have the highest melting point.

## PROBLEM 2.


b). The molecular orbitals of $\mathrm{H}_{2}$ are formed by combining, in equal amounts, the 1s atomic orbitals on each of the hydrogen atoms. Two molecular orbitals are formed: one lying higher in energy than the 1 s atomic orbitals, and the other lying lower in energy. The lower MO is formed from the in-phase combination of the 1 s atomic orbitals on each hydrogen atom. The higher MO is formed from the out-of-phase combination. With reference to the above diagram we may write:

$$
\sigma=\phi_{1}+\phi_{2} \quad \text { and } \quad \sigma^{*}=\phi_{1}-\phi_{2}
$$

c). It is called an antibonding molecular orbital because it results in a net decrease in electron density between the atoms.
d).
$2 \mathrm{p}_{\mathrm{z}}$

$\pi^{*} \quad$ j
j
i
h
g

$2 \mathrm{~s} \begin{cases}\mathrm{O} & \mathrm{O} \\ \mathrm{O} & \mathrm{O}\end{cases}$ $\sigma^{*} \quad \mathrm{~d}$
$\sigma \quad \mathrm{c}$

1s

$\sigma *$
$\sigma$
$\mathrm{O}_{2}$
e). The end-on overlap of two p atomic orbitals in g is much better than the side-on overlap in e or i . Thus the amount of bonding character in g is larger and hence the energy of the orbital is lower.

A similar reason explains the energy of $h$ vs $f$ and $j$. The overlap in $h$ is again better than in $f$ or $j$. Thus the amount of anti-bonding character in $h$ is larger and hence the energy of the orbital is higher.
$\mathrm{f})$. Orbitals e and i both arise from the side-on overlap of p atomic orbitals. The p orbitals in the x direction are, of course, identical to those in the z direction ( x and z are completely arbitrary designations on our part) and so the resulting molecular orbitals are identical.
g). As we stretch the $\mathrm{O}_{2}$ molecule the overlap between the atomic orbitals on one oxygen and those on the other atom decreases. Thus the anti-bonding character in molecular orbital j decreases and hence its energy is lowered.

Because the end-on overlap in orbital h is greater to begin with than the side-on overlap in j , the overlap will decrease faster in h as the $\mathrm{O}_{2}$ molecule is stretched. Thus the anti-bonding character decreases more rapidly, and hence the energy of $h$ is lowered much f .

## PROBLEM 3.

a). We can construct MO diagrams as follows:



These diagrams ignore differences in energy levels between different nuclei, but give the correct qualitative trends for determination of bond orders.

Molecular orbitals arising from the $1 s$ and $2 s$ atomic orbitals are filled in all cases, and give rise to no net bonding character. Bond order is found from the difference in occupancy of bonding and antibonding orbitals arising from the $2 p$ atomic orbitals. CN has 5 electrons in the $\sigma$ and $\pi$ bonding orbitals derived from the $2 p$ orbitals, and none in the corresponding antibonding orbitals, and therefore has a bond order of 2.5. $\mathrm{N}_{2}$ has an excess of six electrons in bonding orbitals, so bond order $=3$. NO has five more electrons in bonding orbitals than in antibonding orbitals, so its bond order is 2.5 .
b). Here we need to consider the electronic configuration arising from electron loss. For $\mathrm{CN}^{+}$, the new electron configuration will be


For $\mathrm{N}_{2}{ }^{+}$, an electron is removed from one of the $\pi$ bonding orbitals of $\mathrm{N}_{2}$, while for $\mathrm{NO}^{+}$the electron in the $\pi^{*}$ antibonding orbital of NO is removed. Removal of an antibonding electron will convey some stabilization on $\mathrm{NO}^{+}$: electrons removed for the other species are from bonding orbitals, so NO will have the lowest ionization energy. Ionization of each of CN and $\mathrm{N}_{2}$ requires removal of
one electron from an electron pair in a bonding orbital, so $\operatorname{IE}(\mathrm{CN})$ and $\operatorname{IE}\left(\mathrm{N}_{2}\right)$ should be similar. We would expect that $\operatorname{IE}\left(\mathrm{N}_{2}\right)$ should be somewhat higher than IE(CN), however, because the overlap between atomic orbitals on two N atoms will be better than that between atomic orbitals on C and on N , so $\mathrm{N}_{2}$ should have the highest ionization energy. Literature values for these quantities $(\operatorname{IE}(\mathrm{CN})=$ $1359 \mathrm{~kJ} \mathrm{~mol}^{-1}, \operatorname{IE}\left(\mathrm{~N}_{2}\right)=1503 \mathrm{~kJ} \mathrm{~mol}^{-1}, \operatorname{IE}(\mathrm{NO})=894 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ) support these expectations. Note that $\operatorname{IE}(\mathrm{NO})$ is much lower than the other two ionization energies, indicating the greater ease of removing an electron from an antibonding orbital rather than a bonding one.
c). Formation of $\mathrm{N}_{2}{ }^{-}$or $\mathrm{NO}^{-}$involves addition of an electron to an antibonding orbital in each case. In contrast, formation of $\mathrm{CN}^{-}$involves placing the additional electron in the $\pi$ bonding orbital (which also achieves an electronic structure isoelectronic with that of $\mathrm{N}_{2}$ ). Thus we would expect CN to have the highest electron affinity, and this is borne out by the literature values $(\mathrm{EA}(\mathrm{CN})=369 \mathrm{~kJ}$ $\mathrm{mol}^{-1}, \mathrm{EA}\left(\mathrm{N}_{2}\right) \sim 0 \mathrm{~kJ} \mathrm{~mol}^{-1}, \mathrm{EA}(\mathrm{NO}) \sim 9 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ).
d). There are two competing effects here. Firstly, overlap will generally be strongest between atomic orbitals of identical nuclei; thus we would expect $\mathrm{N}_{2}$ to have the highest bond strength. However, the comparison is more complex because $\mathrm{NO}^{+}$ and $\mathrm{CN}^{-}$are charged species: the dissociation processes are, respectively,

$$
\mathrm{CN}^{-} \quad \rightarrow \quad \mathrm{C}^{-}+\mathrm{N}
$$

(since C turns out to have a higher electron affinity than N ),

$$
\begin{array}{clll} 
& \mathrm{N}_{2} & \rightarrow & \mathrm{~N}+\mathrm{N} \\
\text { and } & \mathrm{NO}^{+} & \rightarrow & \mathrm{N}+\mathrm{O}^{+}
\end{array}
$$

(since O happens to have a lower ionization energy than N ).
Bond formation tends to stabilize a charge, whether positive or negative, and so despite the inherently better overlap in $\mathrm{N}_{2}$, it will not necessarily be $\mathrm{N}_{2}$ which has the highest bond strength of the three isoelectronic species. In the absence of further information, the question can't be answered with confidence.
(For the record, current literature values yield $D\left[(\mathrm{C}-\mathrm{N})^{-}\right]=994 \mathrm{~kJ} \mathrm{~mol}^{-1} ; D(\mathrm{~N}-\mathrm{N})$ $=946 \mathrm{~kJ} \mathrm{~mol}^{-1}$; and $D\left[(\mathrm{~N}-\mathrm{O})^{+}\right]=1051 \mathrm{~kJ} \mathrm{~mol}^{-1}$. So charge delocalization wins out over better $\mathrm{N}-\mathrm{N}$ overlap in both cases.)

## PROBLEM 4.

a).

$\mathrm{XeF}_{2}$ has 5 electron pairs on Xe , so the structure will be based on a trigonal bipyramidal electron configuration. Of the three possibilities,


$\mathrm{F}-\mathrm{Xe}-\mathrm{F}$,
the linear structure minimizes the repulsion between the lone pairs (which will be held closer to Xe than the electrons involved in Xe-F bonds) and so the linear geometry is favoured.
$\mathrm{XeF}_{4}$ has 6 electron pairs on Xe , so the structure will be based on a octahedral configuration. Of the two possibilities,



The planar structure minimizes the lone-pair repulsion and is consequently favoured.
b). F always has an oxidation number of -1 . Therefore the oxidation numbers of Xe are $+2\left(\mathrm{XeF}_{2}\right)$ and $+4\left(\mathrm{XeF}_{4}\right)$. These species are powerful oxidizing agents!
c). Ignoring energy level differences for H and He , we can draw the following MO diagrams:




From these diagrams, we can see that $\mathrm{HeH}^{+}$and $\mathrm{He}_{2}{ }^{2+}$ both have a bond order of 1, while $\mathrm{He}_{2}{ }^{+}$has a bond order of 0.5 .
d). Group II elements will have low second ionization energies (because $\mathrm{Be}^{+} \rightarrow \mathrm{Be}^{2+}$ or $\mathrm{Mg}^{+} \rightarrow \mathrm{Mg}^{2+}$ yields a closed-shell, $1 s^{2}$ or $1 s^{2} 2 s^{2} 2 p^{6}$ 'noble gas' configuration). $\mathrm{Mg}^{2+}$ has better shielding than $\mathrm{Be}^{2+}$, so $\mathrm{IE}\left(\mathrm{Mg}^{+}\right)<\mathrm{IE}\left(\mathrm{Be}^{+}\right)$. Therefore Mg is the best candidate for ' $Z$ '.
e). Of Mg's neighbours: Ca will have the lowest second ionization energy of $\{\mathrm{Be}, \mathrm{Na}$, $\mathrm{Al}, \mathrm{Ca}\}$ for reasons analogous to those above. So Ca is most likely to form a stable dication with He .
$\mathrm{Na}^{+}$is already closed-shell, so $\mathrm{Na}^{+} \rightarrow \mathrm{Na}^{2+}$ is very unfavourable. Therefore, Na is least likely to form a dication with He.

## PROBLEM 5.

a). The structures are shown in b). below.
b).


Phenanthrene


Triphenylene


Pyrene
c). Phenanthrene possesses two aromatic rings out of three (67\%). Triphenylene has three aromatic rings out of four (75\%). Pyrene has two aromatic rings out of four $(50 \%)$. Therefore, triphenylene is the most aromatic of these PAHs; pyrene is the least aromatic.
d). Phenanthrene possesses 2 aromatic rings for 14 C atoms (1:7). Triphenylene has 3 aromatic rings for 18 C atoms (1:6). Pyrene has 2 aromatic rings for 16 C atoms (1:8). Triphenylene is still the most aromatic of these PAHs, with pyrene still the least aromatic.
e). (i) Average bond order $=4 / 3$. In any canonical form, one of every three C-C bonds must be a double bond, while two are single. Alternatively (see resonance structure below) two of every three $\mathrm{C}-\mathrm{C}$ bonds have $3 / 2$ bond order, while one out of three is formally single: again, an average order of $4 / 3$ results.
(ii) Bond order in benzene $=3 / 2$. Benzene's C-C bonds have more double-bond character than graphite: therefore graphite's bonds are longer.
(iii) Only one in every three of graphite's rings is aromatic in any given canonical form. However, there is one ring per two C atoms in graphite, versus one ring per six C atoms in benzene. By this token, therefore, graphite and benzene are equally aromatic on a per-carbon-atom basis. (If larger $\pi$-delocalized systems are also considered, for example 10 -electron systems, then graphite is more aromatic because such systems cannot feature in benzene's resonance stabilization).

## PROBLEM 6.

- The six isomers of $\mathrm{C}_{4} \mathrm{H}_{8}$ are 1-butene, cis-2-butene, trans-2-butene, methyl propene, cyclobutane, and methyl cyclopropane.
- A, B, C, and D, decolourize bromine in the absence of light: therefore this process is bromine addition to an alkene: therefore $\mathrm{A}-\mathrm{D}$ are the four alkenes, and E and F are the two cycloalkanes.
- Methyl cyclopropane possesses a dipole moment, while the dipole moment of cyclobutane is zero. Therefore, the boiling point of methyl cyclopropane will be higher than that of cyclobutane. Since $\operatorname{bpt}(\mathrm{E})>\operatorname{bpt}(\mathrm{F}), \mathrm{E}$ is methyl cyclopropane and F is cyclobutane.
- Hydrogenation of 1-butene, or of either isomer of 2-butene, yields n-butane. This accounts for the same product arising from hydrogenation of $\mathrm{A}, \mathrm{B}$, and C . The "odd one out" is D, which must therefore be methyl propene.
- Bromine addition to cis-2-butene produces the meso form of 2,3 dibromopropane, while addition to trans-2-butene yields the R,R and S,S enantiomers. This
accounts for the observation that B and C produce stereoisomeric products with bromine. By elimination (the deductive process, NOT the organic reaction mechanism!), A is 1-butene.
- Cis-2-butene should have a higher boiling point than trans-2-butene by virtue of the latter's zero dipole moment. Since $\operatorname{bpt}(\mathrm{C})>\operatorname{bpt}(\mathrm{B}), \underline{\mathrm{C} \text { is cis-2-butene }}$ and $\underline{\mathrm{B}}$ is trans-2-butene.


## PROBLEM 7.

a). Three isomers:



II

III

I and II are geometric isomers.
b).


I


II


III

I and II are optical isomers.
c). Geometric isomers arise if $\mathrm{n}=$ even. Optical isomerism requires $\mathrm{n}=$ odd.

This distinction arises from the planarity of even- $n$ structures, which must therefore all possess a plane of symmetry and which therefore must all be superimposable upon their mirror images. Odd- $n$ structures aren't planar because the two terminal $\mathrm{C}=\mathrm{C}$ bonds have $\pi$ clouds which are orthogonal to each other: these structures will not possess planes of symmetry and can therefore possess non-superimposable mirror images (which is the true basis of optical isomerism).

## PROBLEM 8.

a). The ion at $\mathrm{m} / \mathrm{z} 82$ must be ${ }^{12} \mathrm{C}^{35} \mathrm{Cl}^{35} \mathrm{Cl}$. The absence of $\mathrm{m} / \mathrm{z} 83$ requires an absence of ${ }^{13} \mathrm{C}$ in the sample.

The ion at $\mathrm{m} / \mathrm{z} 28$ must therefore be ${ }^{12} \mathrm{C}^{12} \mathrm{C}^{2} \mathrm{H}^{2} \mathrm{H}$. The absence of $\mathrm{m} / \mathrm{z} 27$ requires an absence of ${ }^{1} \mathrm{H}$.

Therefore, the ion at $\mathrm{m} / \mathrm{z} 75$ must be ${ }^{35} \mathrm{Cl}^{12} \mathrm{C}_{3}{ }^{2} \mathrm{H}_{2}$, and $\mathrm{m} / \mathrm{z} 77$ is the ${ }^{37} \mathrm{Cl}-$ isotopomer of this species.
b). $\quad \mathrm{I}(\mathrm{m} / \mathrm{z} 77)=0.6 \mathrm{I}(\mathrm{m} / \mathrm{z} 75)$

$$
\begin{array}{ll}
\therefore & n\left({ }^{37} \mathrm{Cl}\right)=0.6 n\left({ }^{35} \mathrm{Cl}\right) \\
\therefore & \%\left({ }^{37} \mathrm{Cl}\right)=[0.6 /(1+0.6)] \times 100 \%=37.5 \% \\
\therefore & \%\left({ }^{35} \mathrm{Cl}\right)=62.5 \%
\end{array}
$$

There are three isotopomers of dichloropropadiene:
$\%\left[\mathrm{C}_{3} \mathrm{D}_{2}\left({ }^{35} \mathrm{Cl}\right)_{2}\right]=(62.5 \%)^{2}=39.06 \%$
$\%\left[\mathrm{C}_{3} \mathrm{D}_{2}{ }^{35} \mathrm{Cl}^{37} \mathrm{Cl}\right]=2 \times 62.5 \% \times 37.5 \%=46.88 \%$
$\%\left[\mathrm{C}_{3} \mathrm{D}_{2}\left({ }^{37} \mathrm{Cl}\right)_{2}\right]=(37.5 \%)^{2}=14.06 \%$
c). 1 mole corresponds to:
0.3906 mole $\times 110.0 \mathrm{~g} \mathrm{~mol}^{-1}+0.4688$ mole $\times 112.0 \mathrm{~g} \mathrm{~mol}^{-1}+0.1406$ mole $\times$ $114.0 \mathrm{~g} \mathrm{~mol}^{-1}$
i.e., a molar mass of $111.50 \mathrm{~g} \mathrm{~mol}^{-1}$.
d). $\mathrm{CCl}_{2}{ }^{+}$and $\mathrm{CCD}_{2}{ }^{+}$can only arise if the dichloropropadiene structure is
fragmentation here gives either ion

e). The peak at $\mathrm{m} / \mathrm{z}=242$ in positive ion detection mode is due to the species $\left(\mathrm{C}_{4} \mathrm{H}_{9}\right)_{4} \mathrm{~N}^{+}\left(\mathrm{C}_{16} \mathrm{H}_{36} \mathrm{~N}=242.4 \mathrm{amu}\right)$ which is the only positive species in solution. In negative ion detection mode, peaks due to ${ }^{79} \mathrm{Br}^{-}$and ${ }^{81} \mathrm{Br}^{-}$are observed. The natural abundances of ${ }^{79} \mathrm{Br}$ and ${ }^{81} \mathrm{Br}$ are $50.7 \%$ and $49.3 \%$ respectively, so these two peaks are essentially of equal height.
f). These spectra are consistent with the self ionisation:

$$
\begin{array}{ccc}
\mathrm{C}_{3} \mathrm{H}_{7} \mathrm{OH}
\end{array} \rightarrow \quad \begin{gathered}
\mathrm{C}_{3} \mathrm{H}_{7} \mathrm{O}^{-} \\
\mathrm{m} / \mathrm{z}=59.1
\end{gathered}+\quad \begin{aligned}
& \mathrm{C}_{3} \mathrm{H}_{7} \mathrm{OH}_{2}^{+} \\
& \mathrm{m} / \mathrm{z}=61.1
\end{aligned}
$$

## PROBLEM 9.

a). We can construct a thermochemical cycle where the known quantities are

$$
\begin{aligned}
& \mathrm{A}=2 \Delta \mathrm{H}_{\mathrm{f}}^{\circ}\left(\mathrm{Li}_{(\mathrm{g})}\right)=318.8 \mathrm{~kJ} \mathrm{~mol}^{-1} \\
& \mathrm{~B}=\mathrm{IE}\left(\mathrm{Li}_{(\mathrm{g})}\right)=520.3 \mathrm{~kJ} \mathrm{~mol}^{-1} \\
& \mathrm{C}=-D^{\circ}\left(\mathrm{Li}_{2}{ }^{+}(\mathrm{g})\right)=-129.8 \mathrm{~kJ} \mathrm{~mol}^{-1} \\
& \mathrm{D}=-\mathrm{IE}\left(\mathrm{Li}_{2}(\mathrm{~g})\right)=-493.3 \mathrm{~kJ} \mathrm{~mol}^{-1}
\end{aligned}
$$


and the unknowns are

$$
\mathrm{E}=\mathrm{A}+\mathrm{B}+\mathrm{C}+\mathrm{D}=\Delta \mathrm{H}_{\mathrm{f}}^{\circ}\left(\mathrm{Li}_{2(\mathrm{~g})}\right)
$$

and $\quad \mathrm{F}=\mathrm{A}-\mathrm{E}=D^{\circ}\left(\mathrm{Li}_{2(g)}\right)$.
Thus, we obtain $\Delta \mathrm{H}^{\circ}\left(\operatorname{Li}_{2(g)}\right)=216.0 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and $D^{\circ}\left(\operatorname{Li}_{2(g)}\right)=102.8 \mathrm{~kJ} \mathrm{~mol}^{-1}$.
b). The number of moles of Li in the sample is $\left(122.045 \mathrm{~g} / 6.9410 \mathrm{~g} \mathrm{~mol}^{-1}\right)$
$=17.583$ moles.
We can calculate the expected pressure if only $\mathrm{Li}_{(\mathrm{g})}$ is present, from $\mathrm{PV}=\mathrm{nRT}$ :
$\mathrm{P}=\mathrm{nRT} / \mathrm{V}$
i.e. $\mathrm{P}=17.583 \mathrm{~mol} \times 8.31441 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1} \times 610.25 \mathrm{~K} /\left(5.9474 \times 10^{5} \mathrm{~m}^{3}\right)$,
yielding $\mathrm{P}_{\text {expected }}=0.15000 \mathrm{~Pa}$ (i.e. $1.1251 \times 10^{-3}$ Torr) .
Now, from the equilibrium reaction
$\mathrm{Li}_{(\mathrm{g})}+\mathrm{Li}_{(\mathrm{g})} \quad \mp \quad \mathrm{Li}_{2(\mathrm{~g})}$,
we can see that 2 moles of $\operatorname{Li}_{(\mathrm{g})}$ produce 1 mole of $\mathrm{Li}_{2(\mathrm{~g})}$, and so the dilithium partial pressure must equal the difference between the 'expected' pressure for atomic lithium vapour and the observed total pressure:
$\mathrm{P}\left(\mathrm{Li}_{2(\mathrm{~g})}\right)=1.1251 \times 10^{-3}$ Torr $-9.462 \times 10^{-4}$ Torr $=1.789 \times 10^{-4}$ Torr.
Similarly, $\mathrm{P}\left(\mathrm{Li}_{(\mathrm{g})}\right)=$ Ptotal $-\mathrm{P}\left(\mathrm{Li}_{2(\mathrm{~g})}\right)=9.462 \times 10^{-4}-1.789 \times 10^{-4}$ Torr
i.e. $\mathrm{P}\left(\mathrm{Li}_{(\mathrm{g})}\right)=7.673 \times 10^{-4}$ Torr.

To determine $K_{\mathrm{c}}$, we must convert partial pressures into concentrations. Manipulation of $\mathrm{PV}=\mathrm{nRT}$ and of the various conversion constants indicates that, at 610.25 K , we can convert from Torr to $\mathrm{mol} \mathrm{L}^{-1}$ by multiplying by $2.6276 \times 10^{-5}$ $\mathrm{mol} \mathrm{L}{ }^{-1} \mathrm{Torr}^{-1}$, yielding $\left[\mathrm{Li}_{2(\mathrm{~g})}\right]=4.701 \times 10^{-9} \mathrm{~mol} \mathrm{~L}^{-1}$ and $\left[\mathrm{Li}_{(\mathrm{g})}\right]=2.016 \times 10^{-8}$ $\mathrm{mol} \mathrm{L}{ }^{-1}$. Now, with $K_{\mathrm{c}}$ defined as

$$
K_{\mathrm{c}}=\frac{\left[\mathrm{Li}_{2(g)}\right]}{\left[\mathrm{Li}_{(\mathrm{g})}\right]^{2}}
$$

we obtain a value of $K_{\mathrm{c}}=1.156 \times 10^{7}$.
c). In this reaction chamber, moles $\mathrm{Li}=265.384 \mathrm{~g} / 6.9410 \mathrm{~g} \mathrm{~mol}^{-1}=38.234$ moles. We can determine that not all of the lithium is in the vapour phase:

If all $\mathrm{Li}_{(s)}$ were converted to $\mathrm{Li}_{2(g)}$, then there would be 38.234 moles in a volume of $5.9474 \times 10^{8}$ litres, corresponding to $\left[\mathrm{Li}_{2(g)}\right]=3.2143 \times 10^{-8} \mathrm{~mol} \mathrm{~L}^{-1}$, or a total pressure of $1.2233 \times 10^{-3}$ Torr. This is higher than the observed pressure; furthermore, since much of the lithium vapour will be atomic rather than diatomic, the total pressure should be significantly higher than $1.2233 \times 10^{-3}$ Torr if all the lithium is vaporized. We can conclude, since the pressure has stabilized, that the vapour is in equilibrium with solid or liquid lithium: thus the observed pressure corresponds to the vapour pressure of lithium. The vapour pressure of dilithium can be defined as the partial pressure of $\mathrm{Li}_{2(\mathrm{~g})}$ in the gas phase under these conditions.

We can solve this from $K_{\mathrm{c}}$, by substituting in $\left[\mathrm{Li}_{(g)}\right]+\left[\mathrm{Li}_{2(g)}\right]=2.7472 \times 10^{-8} \mathrm{~mol}$ $\mathrm{L}^{-1}$ (from the observed pressure, and using the Torr $\rightarrow \mathrm{mol} \mathrm{L}^{-1}$ conversion factor found in b)), from which we find $\left[\mathrm{Li}_{2(g)}\right]=5.553 \times 10^{-9} \mathrm{~mol} \mathrm{~L}^{-1}$, corresponding to $\mathrm{P}_{\text {vap }}\left(\mathrm{Li}_{2(g)}\right)=2.113 \times 10^{-4}$ Torr at 610.25 K .
d). First, we need to determine the energy necessary to accelerate the Enterprise to half lightspeed. The kinetic energy is $\mathrm{E}=\mathrm{mv}^{2} / 2$, and with $\mathrm{m}=3.586 \times 10^{6} \mathrm{~kg}$ and $\mathrm{v}=1.49896 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-1}$, we find $\mathrm{E}=4.0286 \times 10^{19} \mathrm{~kJ}$. Since the bond enthalpy of $\mathrm{Li}_{2(\mathrm{~g})}$ is $102.8 \mathrm{~kJ} \mathrm{~mol}^{-1}$ (determined in a)), we require $3.919 \times 10^{17}$ moles of dilithium - i.e., $5.44 \times 10^{15} \mathrm{~kg}$ of dilithium! (To be pedantic, we would need even more lithium than this because of the equilibrium between gaseous lithium and dilithium ...)
e). The calculations in d) indicate that dilithium is not so efficacious a propellant as some researchers have suggested. ${ }^{\dagger}$ However, diberyllium would be even worse:

[^1]MO theory shows that $\mathrm{Li}_{2(\mathrm{~g})}$ has a bond order of 1 , while $\mathrm{Be}_{2(\mathrm{~g})}$ has no net bonding character.

## PROBLEM 10.

a). In a 100 g sample:
40.02 g is C : this is equivalent to $(40.02 / 12.011)=3.332$ moles of C atoms
6.75 g is H : equivalent to $(6.75 / 1.00797)=6.697$ moles of H atoms
53.23 g is O : equivalent to $(53.23 / 15.9994)=3.327$ moles of O

Ratio $(\mathrm{C}: \mathrm{H}: \mathrm{O})=1.001: 2.013: 1$, therefore the empirical formula is $\mathrm{CH}_{2} \mathrm{O}$.
b). $\Delta \mathrm{T}_{\mathrm{f}}=\mathrm{K}_{\mathrm{f}} M$, where $\Delta \mathrm{T}_{\mathrm{f}}$ is the freezing-point depression and $M$ is the molality of the solution. First step is to determine the solution's molality:
$\Delta \mathrm{T}_{\mathrm{f}}=6.60-2.02=+4.58^{\circ} \mathrm{C}$
$M=\Delta \mathrm{T}_{\mathrm{f}} / \mathrm{K}_{\mathrm{f}}$, so $M=0.229 \mathrm{~mol} \mathrm{~kg}^{-1}$.
Next step is to determine the solvent mass:
Mass of solution $=$ density $\times \mathrm{vol}=0.777 \mathrm{~g} \mathrm{~mL}^{-1} \times 500 \mathrm{~mL} \times 10^{-3} \mathrm{~kg} \mathrm{~g}^{-1}=0.3885$ kg

Mass of solute $=$ density $\times \mathrm{vol}=10.44 \mathrm{~g}$ ( or 0.01044 kg$)$
Mass of solvent $=0.3885-0.01044 \mathrm{~kg}=0.3781 \mathrm{~kg}$
Molality is defined as the moles of solute divided by the mass of solvent, so:
moles $(\mathbf{X})=0.229 \mathrm{~mol} \mathrm{~kg}^{-1} \times 0.3781 \mathrm{~kg}=8.66 \times 10^{-2}$ moles
Mass $(\mathbf{X})$ divided by moles $(\mathbf{X})$ yields the molar mass:
$\mathrm{M}_{\mathrm{r}}(\mathbf{X})=10.44 \mathrm{~g} / 8.66 \times 10^{-2}$ moles $=120.6 \mathrm{~g} \mathrm{~mol}^{-1}$.
Now, using the molar mass of the 'formula unit' $\mathrm{CH}_{2} \mathrm{O}$ as $30.03 \mathrm{~g} \mathrm{~mol}^{-1}$, we obtain a formula for $\mathbf{X}$ of $\left(\mathrm{CH}_{2} \mathrm{O}\right)_{4.02}$, i.e. $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{4}$.
c). Solution to this problem is largely analogous to that for $b$ ): the chief difference is that, in a polar solvent such as water, ionization might be expected. This possibility (of dissociation into ions) necessitates the use of the formula $\Delta \mathrm{T}_{\mathrm{f}}=\mathbf{i} \mathrm{K}_{\mathrm{f}}$ $M$, where the factor $\mathbf{i}$ indicates the mean number of dissociated fragments produced per solute molecule.
$\Delta \mathrm{T}_{\mathrm{f}}=0.0-3.54=+3.54^{\circ} \mathrm{C}$
i $M=\Delta \mathrm{T}_{\mathrm{f}} / \mathrm{K}_{\mathrm{f}}=3.54 / 1.86=1.903 \mathrm{~mol} \mathrm{~kg}^{-1}$.
Mass of solvent $=\left(500 \mathrm{~mL} \times 1.005 \mathrm{~g} \mathrm{~mL}^{-1}\right)-\left(50 \mathrm{~mL} \times 1.044 \mathrm{~g} \mathrm{~mL}^{-1}\right)=450.3 \mathrm{~g}$

Using $\mathrm{M}_{\mathrm{r}}(\mathbf{X})$ obtained in b ), we determine that 50 mL of $\mathbf{X}$ is equivalent to 0.433 moles.
$M=0.433$ moles $/ 0.4503 \mathrm{~kg}=0.961 \mathrm{~mol} \mathrm{~kg}^{-1}$.
We can now evaluate the 'dissociation factor' i:
$\mathbf{i}=1.903 / 0.961=1.980$.
Thus, the dissociation of $\mathbf{X}$ into two fragments appears virtually quantitative in aqueous solution. Alternatively, if we assume that $\mathbf{i}=1$, we can say that the molar mass of $\mathbf{X}$ obtained by this method is $120.6 \mathrm{~g} \mathrm{~mol}^{-1} / 1.980=60.9 \mathrm{~g} \mathrm{~mol}^{-1}$.
d). First, calculate the number of moles of hydroxide consumed by this reaction:

Moles $\left(\mathrm{OH}^{-}\right)=1.247 \mathrm{~mol} \mathrm{~L}^{-1} \times 33.60 \times 10^{-3} \mathrm{~L}=4.190 \times 10^{-2}$ moles.
Now, since the reaction is monitored by pH , we can assume that this is in some sense an acid-base titration. Therefore, the number of moles of $\mathrm{OH}^{-}$have reacted with an equal quantity of $\mathrm{H}^{+}$, yielding water. (This argument is necessary to help determine the mass of solvent):

Mass of solution $=$ vol. $\times$ density $=58.50 \mathrm{~mL} \times 1.003 \mathrm{~g} \mathrm{~mL}^{-1}=58.68 \mathrm{~g}$
Mass of solute $=\left(\right.$ mass of $\left.\mathbf{Y}^{i-}\right)+\left(\right.$ mass of $\left.\mathrm{Na}^{+}\right)$
Mass of $\mathbf{Y}^{i-}=$ mass $(\mathbf{X})-\operatorname{mass}\left(\mathrm{H}^{+}\right) \times$moles $\left(\mathrm{OH}^{-}\right)$

$$
=\left(25.00 \mathrm{~mL} \times 1.044 \mathrm{~g} \mathrm{~mL}^{-1} \times 0.1^{*}\right)-1.00797 \mathrm{~g} \mathrm{~mol}^{-1} \times 0.0419 \mathrm{moles}=2.57 \mathrm{~g}
$$

Mass of $\mathrm{Na}^{+}=22.990 \times 0.0419$ moles $=0.96 \mathrm{~g}$
So mass of solvent $=58.68 \mathrm{~g}-(2.57 \mathrm{~g}+0.96 \mathrm{~g})=55.15 \mathrm{~g}$.
Now, using i $M=\Delta \mathrm{T}_{\mathrm{f}} / \mathrm{K}_{\mathrm{f}}$, we obtain:
i $M=2.78^{\circ} \mathrm{C} / 1.86^{\circ} \mathrm{C} \mathrm{kg} \mathrm{mol}^{-1}=1.495 \mathrm{~mol} \mathrm{~kg}^{-1}$.
The parameter i $M$ represents the number of moles of dissolved species per kg of water. These dissolved species are $\mathrm{Na}^{+}$and $\mathbf{Y}^{i-}$. By multiplying through by the mass of solvent, we obtain
moles $\left(\mathrm{Na}^{+}\right)+\operatorname{moles}\left(\mathbf{Y}^{i-}\right)=1.495 \mathrm{~mol} \mathrm{~kg}{ }^{-1} \times 5.515 \times 10^{-2} \mathrm{~kg}=8.24 \times 10^{-2}$ moles.

We have already determined moles $\left(\mathrm{Na}^{+}\right)=$moles $\left(\mathrm{OH}^{-}\right)$consumed, so moles $\left(\mathbf{Y}^{i-}\right)=8.24 \times 10^{-2}$ moles $-4.19 \times 10^{-2}$ moles $=4.05 \times 10^{-2}$ moles .

Since moles $\left(\mathbf{Y}^{i-}\right):\left(\mathrm{Na}^{+}\right)=1: 1.03$, we determine from the freezing-point analysis that the salt formed has the formula $\mathrm{Na}^{+} \mathrm{Y}^{-}$. By comparing the mass of $\mathbf{Y}^{i-}$ (found

[^2]above) with moles $\left(\mathbf{Y}^{i-}\right)$, we obtain $\operatorname{Mr}\left(\mathbf{Y}^{i-}\right)=64.4 \mathrm{~g} \mathrm{~mol}^{-1}$ which compares with $\mathrm{Mr}\left(\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-}\right)=59.0 \mathrm{~g} \mathrm{~mol}^{-1}$.

We can conclude that the salt formed is $\mathrm{Na}^{+} \mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}{ }^{-}$.
Note that if, as suggested from b), the formula of $\mathbf{X}$ is $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{4}$, there should be $\left(25.00 \mathrm{~mL} \times 1.044 \mathrm{~g} \mathrm{~mL}^{-1} \times 0.1 / 120.6 \mathrm{~g} \mathrm{~mol}^{-1}=\right) 2.16 \times 10^{-2}$ moles of $\mathbf{X}$ present.

Therefore, conversion of $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{4}$ into $2\left(\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}{ }^{-}\right)$is essentially quantitative.
e). The results of b) and c) appear in disagreement: cyclohexane suggests a molecular mass twice that obtained when water is the solvent. This could be resolved if $\mathbf{X}$ were to dissociate fully into two ions in aqueous solution: so perhaps $\mathbf{X}$ is a strong acid. However, strong acids are relatively rare in organic chemistry. Furthermore, we would not expect a strong acid to dissolve readily in a nonpolar solvent such as cyclohexane! The results of d) suggest a further problem: both of the 'dissociation products' of $\mathbf{X}$, in aqueous solution, are apparently converted into $\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}{ }^{-}$. How is this possible, if the two products are oppositely-charged ions?

An alternative explanation, and that which offers a better account of the chemistry occurring, is that the 'dissociated form' of $\mathbf{X}$ in $\mathrm{H}_{2} \mathrm{O}$, in part c), is a neutral species which is capable of reacting as an acid (as in d)). The calculated molar mass of this "dissociated neutral" species is $60.9 \mathrm{~g} \mathrm{~mol}^{-1}$, which compares with 60.1 g $\mathrm{mol}^{-1}$ expected for $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}_{2}$. There are few isomers of $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}_{2}$, and the one which is most capable of acting as an acid is acetic acid (ethanoic acid), $\mathrm{CH}_{3} \mathrm{COOH}$.

So why does $\mathbf{X}$ apparently give 2 molecules of acetic acid in aqueous solution? This is best answered by considering that $\mathbf{X}$ doesn't dissociate in aqueous solution: rather, it dimerizes in cyclohexane. The hydrogen-bonded acetic acid dimer

is symmetrical and therefore non-polar, and therefore soluble in a non-polar solvent such as cyclohexane.

## PROBLEM 11.

a). The free-energy change is obtained using $\Delta \mathrm{G}^{\circ}=\Delta \mathrm{H}^{\circ}-\mathrm{T} \Delta \mathrm{S}^{\circ}$.

$$
\begin{aligned}
& \Delta \mathrm{H}^{\circ}=\Delta \mathrm{H}_{\mathrm{f}}^{\circ}(\mathrm{H})+\Delta \mathrm{H}_{\mathrm{f}}^{\circ}(\mathrm{HD})-\Delta \mathrm{H}_{\mathrm{f}}^{\circ}\left(\mathrm{H}_{2}\right)-\Delta \mathrm{H}_{\mathrm{f}}^{\circ}(\mathrm{D})=-3.43 \mathrm{~kJ} \mathrm{~mol}^{-1} \\
& \Delta \mathrm{~S}^{\circ}=\mathrm{S}^{\circ}(\mathrm{H})+\mathrm{S}^{\circ}(\mathrm{HD})-\mathrm{S}^{\circ}\left(\mathrm{H}_{2}\right)-\mathrm{S}^{\circ}(\mathrm{D})=+4.48 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}
\end{aligned}
$$

so at $20 \mathrm{~K}, \Delta \mathrm{G}^{\circ}=-3.52 \mathrm{~kJ} \mathrm{~mol}^{-1}$; at $1000 \mathrm{~K}, \Delta \mathrm{G}^{\circ}=-7.91 \mathrm{~kJ} \mathrm{~mol}^{-1}$.
The reaction is spontaneous in the forward direction at both temperatures. [In fact, since $\Delta \mathrm{H}^{\circ}$ is negative and $\Delta \mathrm{S}^{\circ}$ is positive, the forward reaction should be spontaneous at all temperatures.]
b). $\Delta \mathrm{H}^{\circ}$ is negative in the forward direction: thus the bond strength of HD exceeds that of $\mathrm{H}_{2}$. This is in accordance with the general trend, mentioned above, for light-isotope species to have slightly weaker bonds.
$\Delta \mathrm{S}^{\circ}$ is positive in the forward direction, indicating that the products are less ordered than the reactants. The increase in disorder can be understood as arising from the possibility of forming either of two identical HD molecules (involving one or other of the two identical H atoms) from the one possible $\mathrm{H}_{2}$ molecule.
c). The conversion of HD to $\mathrm{D}_{2}$ should be associated with a negative enthalpy change, since the bond strength of $\mathrm{D}_{2}$ should exceed that of HD (heavier isotopes give stronger bonds). The entropy change in the forward direction will also be negative, since (by analogy with the arguments raised above) HD is more disordered than $D_{2}$. Assuming the magnitudes of $\Delta \mathrm{H}^{\circ}$ and $\Delta \mathrm{S}^{\circ}$ are equal to those in a) $\left[\right.$ i.e. $\left.\Delta \mathrm{H}^{\circ}=-3.43 \mathrm{~kJ} \mathrm{~mol}^{-1} ; \Delta \mathrm{S}^{\circ}=-4.48 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}\right]$, we get
$\Delta \mathrm{G}^{\circ}=-3.34 \mathrm{~kJ} \mathrm{~mol}^{-1}$ at $20 \mathrm{~K}, \Delta \mathrm{G}^{\circ}=+1.05 \mathrm{~kJ} \mathrm{~mol}^{-1}$ at 1000 K .
Thus the forward reaction is spontaneous at 20 K , but the reverse reaction becomes spontaneous at 1000 K .
d). I). Since equilibrium (1) always lies towards the right hand side regardless of temperature, it is plain that atomic D cannot be the most abundant form of deuterium. Intuition would suggest that HD will predominate over $\mathrm{D}_{2}$ if the overall deuterium abundance is low, but a more rigorous examination is possible:

If the equilibrium (2) is reversed, then in combination with (1) this yields

$$
\mathrm{H}_{2}+\mathrm{D}+\mathrm{D}_{2}+\mathrm{H} \rightleftharpoons 2 \mathrm{HD}+\mathrm{H}+\mathrm{D}
$$

or, with cancellations,

$$
\begin{equation*}
\mathrm{H}_{2}+\mathrm{D}_{2} \rightleftharpoons 2 \mathrm{HD} \tag{3}
\end{equation*}
$$

The free-energy change for this equilibrium is $\Delta \mathrm{G}^{\circ}(3)=\Delta \mathrm{G}^{\circ}(1)-\Delta \mathrm{G}^{\circ}(2)$; from the calculations in a) and c), we can estimate this to be $\Delta G^{\circ}(3)=-0.18 \mathrm{~kJ} \mathrm{~mol}^{-1}$. Since $\Delta \mathrm{G}^{\circ}(3)$ is negative, the equilibrium must lie towards the right-hand side: therefore HD will indeed predominate over $\mathrm{D}_{2}$.
ii). The above argument also applies to the case where $n(\mathrm{D})=n(\mathrm{H})$, so HD will still predominate over $\mathrm{D}_{2}$. Also, since equilibrium (3) lies towards the right-hand side, HD will also be the dominant form of hydrogen.

## PROBLEM 12.

a). Neutral helium has 2 electrons; a 'hydrogen-like' species has only one electron. Therefore, the species in question is $\mathrm{He}^{+}$.
b). The hydrogen spectrum obeys the relation

$$
\Delta \mathrm{E}=\mathrm{R}_{\mathrm{H}}\left(\frac{1}{n_{\mathrm{i}}^{2}}-\frac{1}{n_{\mathrm{f}}^{2}}\right)
$$

and so, in the present case, the $\mathrm{He}^{+}$lines should obey

$$
\Delta \mathrm{E}=\mathrm{R}_{\mathrm{He}^{+}}\left(\frac{1}{4^{2}}-\frac{1}{n_{\mathrm{f}}^{2}}\right)
$$

which, with $\Delta \mathrm{E}=\mathrm{h} \nu=\mathrm{hc} / \lambda$, may be rearranged to yield

$$
\mathrm{R}_{\mathrm{He}^{+}}=(\mathrm{hc} / \lambda)\left(\frac{1}{4^{2}}-\frac{1}{n_{\mathrm{f}}^{2}}\right)^{-1} .
$$

We must now attempt to fit the spectrum to such a relation. Assume that the longest wavelength observed, $6558 \AA$ (which is the least energetic transition) corresponds to $n_{\mathrm{f}}=5$; we obtain
$\qquad$

| $\lambda$ | $n_{\mathrm{f}}$ | $" \mathrm{R}_{\mathrm{He}^{+}} "$ |
| :---: | :---: | :---: |
| $6.558 \times 10^{-7}$ | 5 | $1.35 \times 10^{-17} \mathrm{~J}$ |
| $5.410 \times 10^{-7}$ | 6 | $1.06 \times 10^{-17} \mathrm{~J}$ |
| $4.858 \times 10^{-7}$ | 7 | $0.97 \times 10^{-17} \mathrm{~J}$ |
| $4.540 \times 10^{-7}$ | 8 | $0.93 \times 10^{-17} \mathrm{~J}$ |
| $4.338 \times 10^{-7}$ | 9 | $0.91 \times 10^{-17} \mathrm{~J}$ |

If the assignment is correct, all transitions should yield the same $\mathrm{R}_{\mathrm{He}^{+}}$value.
Clearly, this is not the case: we must try again.
If we choose $n_{\mathrm{f}}=6$ for the $6558 \AA$ transition, we get

| $\lambda$ | $n_{\mathrm{f}}$ | $" \mathrm{R}_{\mathrm{He}^{+}}$ |
| :---: | :---: | :---: |
| $6.558 \times 10^{-7}$ | 6 | $8.72 \times 10^{-18} \mathrm{~J}$ |
| $5.410 \times 10^{-7}$ | 7 | $8.72 \times 10^{-18} \mathrm{~J}$ |
| $4.858 \times 10^{-7}$ | 8 | $8.72 \times 10^{-18} \mathrm{~J}$ |
| $4.540 \times 10^{-7}$ | 9 | $8.72 \times 10^{-18} \mathrm{~J}$ |
| $4.338 \times 10^{-7}$ | 10 | $8.72 \times 10^{-18} \mathrm{~J}$ |

This is the correct assignment, as is evident from the constancy of the $\mathrm{R}_{\mathrm{He}^{+}}$value obtained.
c). $\operatorname{IE}\left(\mathrm{He}^{+}\right)$is equal to $\mathrm{R}_{\mathrm{He}^{+}}$. To convert this into electronvolts, multiply by 6.02205 $\times 10^{23} \mathrm{~mol}^{-1}$ and divide by $96486 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{eV}^{-1}: \operatorname{IE}\left(\mathrm{He}^{+}\right)=54.44 \mathrm{eV}$.
d). $\operatorname{IE}\left(\mathrm{He}^{+}\right) / \mathrm{IE}(\mathrm{He})=2.180$, $\operatorname{so} \mathrm{IE}(\mathrm{He})=24.97 \mathrm{eV}$.

Thus $\operatorname{AE}\left(\mathrm{He}^{2+}\right)=79.41 \mathrm{eV} \equiv 1.272 \times 10^{-17} \mathrm{~J}$.
We can calculate the frequency, $v=\mathrm{E} / \mathrm{h}=1.920 \times 10^{16} \mathrm{~s}^{-1}$, and the wavelength, $\lambda$ $=\mathrm{c} / v=15.61 \mathrm{~nm}$, of the least energetic photon capable of the double-ionization. This is clearly a much shorter wavelength than the visible spectrum ( $300 \mathrm{~nm}<\lambda<$ 700 nm ): the sun isn't a hot enough 'black body' to produce many such photons, and most would be absorbed by the atmosphere before they reached the surface.

## PROBLEM 13.

a). The student is essentially seeking to determine the molar mass of each sample, $M_{\mathrm{r}}(\mathrm{MX})$, by exchanging $\mathrm{M}^{+}$with $\mathrm{H}^{+}$from the ion-exchange column and by determining the quantity of $\mathrm{H}^{+}$by titration.

Reactions involved are:

$$
\begin{array}{lll}
\mathrm{M}^{+}+\left[\mathrm{RSO}_{3} \mathrm{H}\right] & \rightarrow & \mathrm{H}^{+}+\left[\mathrm{RSO}_{3}^{-} \mathrm{M}^{+}\right] \\
\mathrm{H}^{+}+\mathrm{OH}^{-} & \rightarrow & \mathrm{H}_{2} \mathrm{O}
\end{array}
$$

b). Analysis of results:
moles $\mathrm{M}^{+}$in $5 \mathrm{~g}=$ moles $\mathrm{OH}^{-} \times(250 \mathrm{~mL} / 50 \mathrm{~mL}) \times(100 \mathrm{~mL} / 40 \mathrm{~mL})$
$=$ titre volume $\times 0.326 \mathrm{~mol} \mathrm{~L}^{-1} \times 5 \times 2.5$
$M_{\mathrm{r}}(\mathrm{MX})=$ sample mass $(5 \mathrm{~g}) /$ moles $\mathrm{M}^{+}$in 5 g
This yields the following:

| Sample | $\mathrm{M}_{\mathrm{r}} / \mathrm{g} \mathrm{mol}^{-1}$ | Possible MX |
| :---: | :---: | :--- |
| A | 58.01 | $\mathrm{NaCl}(58.44), \mathrm{KF}(58.10)$ |
| B | 41.88 | $\mathrm{LiCl}(42.39), \mathrm{NaF}(41.99)$ |
| C | 165.81 | $\mathrm{KI}(166.00), \mathrm{RbBr}(165.37), \mathrm{CsCl}(168.36)$ |
| D | 57.88 | $\mathrm{NaCl}(58.44), \mathrm{KF}(58.10)$ |
| E | 119.13 | $\mathrm{KBr}(119.00), \mathrm{RbCl}(120.92)$ |
| F | 42.09 | $\mathrm{LiCl}(42.39), \mathrm{NaF}(41.99)$ |
| KBr | 119.71 | $\mathrm{KBr}(119.00), \mathrm{RbCl}(120.92)$ |

A problem should be evident with the above results: some aspect of the experimental technique is apparently too inaccurate to identify the salts
unambiguously. For example, if all the samples are indeed different, and if the sample labelled ' KBr ' is indeed KBr , then sample E must be RbCl . The molar mass of RbCl is significantly above that of KBr , yet sample E has the lower $\mathrm{M}_{\mathrm{r}}$ according to the titration results. Note that the near-coincidences in molar mass for two (or even three) alkali halides precludes positive identification of $\mathrm{A}, \mathrm{B}, \mathrm{C}$, D, or F .
c). Watchglasses: Lithium salts are very hygroscopic, so leaving a small amount of (e.g.) 'B' and ' F ' on adjacent watchglasses should allow identification of the lithium chloride: it'll form a puddle in a short time (unless the laboratory's atmosphere is very dry).

Litmus paper: Fluoride ion is the conjugate base of a weak acid (HF), so fluoride salts form alkaline solutions. Thus, litmus should identify a dilute solution of either ' B ' or ' F ' as NaF , and ' A ' or ' D ' as KF .

Acidified persulfate + starch: Persulfate oxidizes $\mathrm{I}^{-}$to $\mathrm{I}_{2}$, which forms a dark blue complex with starch solution. Thus, if 'C' is KI, it will give a deep blue starch complex. Persulfate will also oxidize $\mathrm{Cl}^{-}$or $\mathrm{Br}^{-}$, but these won't give the characteristic indication with starch: so this reagent won't distinguish RbBr and CsCl . (However, since the student was able to identify ' C ' using the techniques listed, it implies that ' C ' was indeed KI).

There are no tests here for NaCl : by elimination, whichever of ' A ' and ' D ' does not turn litmus blue is the NaCl .
d). The property which precludes unambiguous identification on the basis of ion exchange is the occurrence of near-coincidences in the molar masses of different alkali halides MX. This arises because these compounds are uni-univalent, and also because the alkali metals are only two atomic numbers higher than the preceding halogen atoms: thus, subtracting a filled shell from a metal (e.g. $\mathrm{K} \rightarrow$ Na ) and adding a filled shell to a halogen (e.g. $\mathrm{F} \rightarrow \mathrm{Cl}$ ) yields a compound having a molar mass nearly identical to the initial compound.

Alkaline earth halides won't have this problem (as a general rule), provided both halogen atoms X are the same: subtracting a filled shell from M (e.g. $\mathrm{Ca} \rightarrow \mathrm{Mg}$ ) and adding a filled shell to each $\mathrm{X}(\mathrm{eg} \mathrm{F} \rightarrow \mathrm{Cl})$ gives quite different molar masses ( 78.08 and $95.21 \mathrm{~g} \mathrm{~mol}^{-1}$ respectively, for $\mathrm{CaF}_{2}$ and $\mathrm{MgCl}_{2}$ ).

## PROBLEM 14.

a). Cubane appears to possess six rings, corresponding to the six faces of a cube.
b). $\quad \boldsymbol{m}=2(\boldsymbol{n}+1-\boldsymbol{r}-\boldsymbol{d})$. Cursory inspection of a few simple examples (methane, ethene, ethyne, benzene) should suffice to demonstrate this.
c). For $\boldsymbol{n}=8, \boldsymbol{r}=6$, $\boldsymbol{d}=0$, a value for $\boldsymbol{m}=6$ is returned (i.e. $\mathrm{C}_{8} \mathrm{H}_{6}$ ). However, cubane is clearly $\mathrm{C}_{8} \mathrm{H}_{8}$.
d). Coronene: $\boldsymbol{n}=24, \boldsymbol{r}=7, \boldsymbol{d}=12$, yielding $\boldsymbol{m}=12$ (i.e. $\mathrm{C}_{24} \mathrm{H}_{12}$ )

Corannulene: $\boldsymbol{n}=20, \boldsymbol{r}=6, \boldsymbol{d}=10$, yielding $\boldsymbol{m}=10$ (i.e. $\mathrm{C}_{20} \mathrm{H}_{10}$ ).
These values are consistent with the expected structures:


e). Corannulene $\left(\mathrm{C}_{20} \mathrm{H}_{10}\right)$ is not flat. If you consider the bonds which radiate out from the central pentagon as 'spokes', then the preferred angle between two spokes is $60^{\circ}$ (as dictated by the geometry of a regular hexagon). However, a 'ring' of five regular hexagons

can only subtend an angle of $300^{\circ}$ : five hexagons are insufficient to complete the ring in planar space. Joining the sides labelled ' $a$ ' achieves closure of the corannulene skeleton, but makes the overall molecule somewhat bowl-shaped.
f). Flattened cubane:


Cubane, drawn in this manner, can be seen to contain five rings. Using $r=5$ yields $\mathrm{C}_{8} \mathrm{H}_{8}$, in agreement with b) but in dispute with a).
g). Seven carbon-carbon bonds can be broken in coronene; six in corannulene. The number of bonds which may be broken without fragmenting the molecule is equal to the number of rings.
H H H H H H H
h). Five bonds can be broken in cubane. Therefore cubane has five rings, in agreement with b) and f) but in disagreement with a).

i). Dodecahedrane features 11 rings. This yields the correct chemical formula of $\mathrm{C}_{20} \mathrm{H}_{20}$ upon implementation of $\boldsymbol{m}=2(\boldsymbol{n}+1-\boldsymbol{r}-\boldsymbol{d})$.

j). Sixty C atoms, each with 3 nearest neighbours, yields $90 \mathrm{C}-\mathrm{C}$ bonds ( $60 \times 3$ yields double the number - this effectively counts each bond twice). Each C atom has a valence requirement for 4 bonds - so one bond to each C must be double. Therefore $\boldsymbol{d}=30$ (again, each bond has two ends!). From the formula, we know that $\boldsymbol{n}=60$ (C atoms) and $\boldsymbol{m}=0$ (H atoms), so $\boldsymbol{r}$ (rings) must be 31 .

If 12 rings are pentagons, then 19 rings must be hexagons. However, by analogy with the other cage structures (cubane and dodecahedrane), or by inspection of a soccerball, it can be seen that $\mathrm{C}_{60}$ possesses 32 faces (in a geometric sense), and that 20 of these faces are hexagons. One of the faces on the $\mathrm{C}_{60}$ surface does not correspond to a 'true ring', but any assignment of either a pentagon or a hexagon as the 'illusory' ring is quite arbitrary. We can't state unambiguously how many pentagonal or hexagonal rings are present!

## PROBLEM 15.

a).

$$
\begin{array}{lll}
\mathrm{CO}_{2(\mathrm{~g})} & = & \mathrm{CO}_{2(a q)} \\
\mathrm{CO}_{2(a q)}+\mathrm{H}_{2} \mathrm{O} & = & \mathrm{HCO}_{3^{-}(a q)}+\mathrm{H}^{+}{ }_{(a q)} \\
\mathrm{HCO}_{3^{-}(a q)} & = & \mathrm{CO}_{3^{2-}(a q)}+\mathrm{H}^{+}{ }_{(a q)} \tag{3}
\end{array}
$$

Note that an additional equilibrium

$$
\mathrm{CO}_{2(a q)}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{H}_{2} \mathrm{CO}_{3(a q)}
$$

can be introduced to account for the separate existence of dissolved $\mathrm{CO}_{2}$ and aqueous carbonic acid, but such an equilibrium is not strictly necessary to explain the reaction chemistry of carbonate in water.

Since equilibrium will be established between the left and right hand side of each reaction, and since we are starting from $\mathrm{CO}_{2}(\mathrm{~g})$ and $\mathrm{H}_{2} \mathrm{O}$, the resulting solution will clearly be acidic.
b). $\quad \mathrm{NH}_{3}$ is a basic gas:

so an acid-base reaction will be established, pulling the equilibria (2) and (3) towards the right hand side. This will increase the tendency for atmospheric $\mathrm{CO}_{2}$ to dissolve.
$\mathrm{Cl}_{2}$ is an acidic gas:


The increase in $\left[\mathrm{H}^{+}\right]$engendered by these reactions will drive the equilibria (2) and (3) back towards the left hand side. This will decrease the tendency for atmospheric $\mathrm{CO}_{2}$ to dissolve.

Thus the tendency for $\mathrm{CO}_{2}$ to dissolve is:
mixture ii) > mixture i) > mixture iii).
c). Acetate, $\mathrm{CH}_{3} \mathrm{COO}^{-}$, is the conjugate base of a weak acid:

$$
\mathrm{CH}_{3} \mathrm{COO}^{-}{ }_{(a q)}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{CH}_{3} \mathrm{COOH}_{(a q)}+\mathrm{OH}^{-}{ }_{(a q)} .
$$

The sodium acetate solution is significantly alkaline, and will pull each of the $\mathrm{CO}_{2}$ equilibria towards the right hand side.

The hydrochloric acid solution will drive the $\mathrm{CO}_{2}$ equilibria back towards the left hand side.

Thus the tendency for $\mathrm{CO}_{2}$ to dissolve is:
solution iii) > solution i) > solution ii).
d). The concentration of aqueous $\mathrm{CO}_{2}$ is given by Henry's law:
$\left[\mathrm{CO}_{2}(a q)\right]=K_{\mathrm{H}} \mathrm{P}\left(\mathrm{CO}_{2}\right)=3.39 \times 10^{-2} \mathrm{~mol} \mathrm{~L}^{-1} \mathrm{~atm}^{-1} \times 3.5 \times 10^{-4} \mathrm{~atm}$
$=1.187 \times 10^{-5} \mathrm{~mol} \mathrm{~L}^{-1}$.
It will be helpful to convert $K_{\mathrm{b}}$ values to $K_{\mathrm{a}}$, using $K_{\mathrm{a}}=K_{\mathrm{w}} / K_{\mathrm{b}}$ at $25^{\circ} \mathrm{C}$ :
$K_{\mathrm{a}}\left(\mathrm{CO}_{2(a q)}\right)=4.46 \times 10^{-7}$
$K_{\mathrm{a}}\left(\mathrm{HCO}_{3}{ }^{-}(a q)\right)=4.67 \times 10^{-11}$.
These $K_{\mathrm{a}}$ values are defined as:
$K_{\mathrm{a}}\left(\mathrm{CO}_{2(a q)}\right)=4.46 \times 10^{-7}=\frac{\left[\mathrm{HCO}_{3}^{-}\right]\left[\mathrm{H}^{+}\right]}{\left[\mathrm{CO}_{2(a q)}\right]}$
$K_{\mathrm{a}}\left(\mathrm{HCO}_{3^{-}}{ }^{-}(a q)\right)=4.67 \times 10^{-11}=\frac{\left[\mathrm{CO}_{3}{ }^{2-}\right]\left[\mathrm{H}^{+}\right]}{\left[\mathrm{HCO}_{3}{ }^{-}\right]}$
Since $K_{\mathrm{a}}\left(\mathrm{CO}_{2}(a q)\right) \gg K_{\mathrm{a}}\left(\mathrm{HCO}_{3^{-}}{ }_{(a q)}\right)$, we assume that in acidic solution only the first deprotonation equilibrium is significant (we can test this, once we've found $\left[\mathrm{H}^{+}\right]$). Therefore,
$\left[\mathrm{H}^{+}\right]=\left[\mathrm{HCO}_{3}{ }^{-}\right]=\left(4.46 \times 10^{-7} \times 1.187 \times 10^{-5}\right)^{0.5}=2.30 \times 10^{-6} \mathrm{~mol} \mathrm{~L}^{-1}$.
i.e. $\mathrm{pH}=5.64$.

Now, using $\left[\mathrm{H}^{+}\right]=\left[\mathrm{HCO}_{3}^{-}\right]=2.30 \times 10^{-6} \mathrm{~mol} \mathrm{~L}{ }^{-1}$, we can see $\left[\mathrm{CO}_{3}{ }^{2-}\right] \approx 4.67 \times$ $10^{-11} \mathrm{~mol} \mathrm{~L}{ }^{-1}$. Thus, the degree of dissociation of $\mathrm{HCO}_{3}{ }^{-}$to $\mathrm{H}^{+}$and $\mathrm{CO}_{3}{ }^{2-}$ is very slight, and our assumption (that the second deprotonation equilibrium is insignificant in this case) is correct.
e). It should be intuitively apparent that 1 atm of $\mathrm{CO}_{2}(\mathrm{~g})$ will produce a substantially more acidic solution than will $350 \mathrm{ppm} \mathrm{CO}{ }_{2}(\mathrm{~g})$ : thus, for reasons analogous to those presented in d), we need consider only the equilibria

in solving this problem.
$\left[\mathrm{CO}_{2}(a q)\right]=K_{\mathrm{H}} \mathrm{P}\left(\mathrm{CO}_{2}\right)=3.39 \times 10^{-2} \mathrm{~mol} \mathrm{~L}^{-1}$,
and $\left[\mathrm{H}^{+}\right]=\left[\mathrm{HCO}_{3}^{-}\right]=\left(K_{\mathrm{a}}\left[\mathrm{CO}_{2}(a q)\right]\right)^{0.5}=1.23 \times 10^{-4} \mathrm{~mol} \mathrm{~L}^{-1}$
i.e. $\mathrm{pH}=3.91$.
f). This is a weak (diprotic) acid / strong base titration.

We need, first, to determine the total $\left[\mathrm{CO}_{2(a q)}\right]$ :
Total $\left[\mathrm{CO}_{2(a q)}\right]=\left[\mathrm{CO}_{2(a q)}\right]+\left[\mathrm{HCO}_{3}^{-}\right]+\left[\mathrm{CO}_{3}{ }^{2-}\right]$
$=\left(1.187 \times 10^{-5}\right)+\left(2.30 \times 10^{-6}\right)+\left(4.67 \times 10^{-11}\right) \mathrm{mol} \mathrm{L}^{-1}=1.417 \times 10^{-5} \mathrm{~mol} \mathrm{~L}^{-1}$,
and so the 100 mL aliquot contains $1.417 \times 10^{-6}$ moles of the weak diprotic acid $\mathrm{CO}_{2(a q)}$ and its assorted conjugate bases. This will require $2.834 \times 10^{-6}$ moles of $\mathrm{OH}^{-}$for complete neutralization, i.e. 28.34 mL of $1.00 \times 10^{-4} \mathrm{~mol} \mathrm{~L}^{-1} \mathrm{NaOH}$.

At the start of the titration, $\mathrm{pH}=5.64$ from d).

At 7.1 mL (the first half-equivalence point), $\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}\left(\mathrm{CO}_{2}(a q)\right)=6.35$
At 21.2 mL (the half-equivalence point for the second deprotonation), $\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}\left(\mathrm{HCO}_{3}{ }^{-}\right)=10.33$.


## PROBLEM 16.

a). There are four different structural isomers:

pentanoic acid


3-methylbutanoic acid



2-methylbutanoic acid


2,2-dimethylpropanoic acid

2-methylbutanoic acid will be optically active.
b). Acidity involves dissociation to form a carboxylate anion:




The position of the equilibrium thus depends on the stability of the anion $\mathrm{RCOO}^{-}$. Since alkyl groups are inductive donors of electron density, the more branched structures will have the lower $K_{\mathrm{a}}$ values. Expected order of $K_{\mathrm{a}}$ (highest to lowest):
pentanoic acid (no branching on alkyl chain)
3-methylbutanoic acid

2-methylbutanoic acid
(methyl sidechain on $\beta$ carbon; weakly inductively destabilized)
(methyl sidechain on $\alpha$ carbon; more inductively destabilized)

2,2-dimethylpropanoic acid (two methyl sidechains on $\alpha$ carbon; most inductively destabilized)

We can also compare these with the literature values (i.e., are the above arguments valid?). In the acid order given above, pKa values are 4.76, 4.76, (not known), 5.04, essentially in agreement with the results expected from the inductive effect.
c). There are 9 structural isomers of this type (several others are not optically active):

A



E


F


D


C




I


Fluorine is inductively electron withdrawing, and so proximity of the fluorine atom to the carboxylate group will stabilize the conjugate base (and increase the acid's strength).

The most acidic species will be $\mathbf{A}$, which has the fluorine $\alpha$ to the carboxylic acid (maximum stabilization by $F$ ) and has no alkyl sidechains (minimum destabilization by methyl groups).

The least acidic of the optically-active species is $\mathbf{H}$, which has the fluorine $\gamma$ to the COOH group (minimum inductive donation from F to $\mathrm{COO}^{-}$) and which also has a methyl group $\alpha$ to the COOH (maximum inductive withdrawing from $\mathrm{COO}^{-}$).
d). This reaction produces an ester:

$$
\mathrm{R}-\mathrm{COOH}+\mathrm{R}^{\prime}-\mathrm{OH} \quad \rightarrow \quad \mathrm{R}-\mathrm{COO}-\mathrm{R}^{\prime}+\mathrm{H}_{2} \mathrm{O}
$$

e). The labelled ester is:


The reaction occurs as nucleophilic attack of the carboxyl carbon:

f). i). The expected product is

ii) When ethanoic acid is added to the NaOH solution, an acid-base equilibrium is established:

$$
\mathrm{CH}_{3} \mathrm{CO} * \mathrm{OH}+\mathrm{OH}^{-} \rightleftharpoons \mathrm{CH}_{3}\left(\mathrm{COO}^{*}\right)^{-}+\mathrm{H}_{2} \mathrm{O}
$$

The ethanoate anion has two equivalent oxygens. When the solution is reacidified, the label is scrambled:


with the two isotopomers formed in equal amounts (provided that the ethanoic acid / hydroxide system had sufficient time to attain equilibrium). The former isotopomer will yield the same product as i); the latter will give unlabelled propyl ethanoate and labelled water (or, to be more precise, labelled HOD).

## PROBLEM 17.

a). The volume of a sphere is $V=(4 / 3) \pi r^{3}$.
$\boldsymbol{r}=3.5 \times 10^{-10} \mathrm{~m}$, so $\boldsymbol{V}=1.796 \times 10^{-28} \mathrm{~m}^{3}$.
Now for the pressure: $\boldsymbol{P V}=\boldsymbol{n} \boldsymbol{R} \boldsymbol{T}$, so $\boldsymbol{P}=\boldsymbol{n} \boldsymbol{R} \boldsymbol{T} / \boldsymbol{V}$.
$\boldsymbol{n}=1$ atom $=\left(6.02205 \times 10^{23}\right)^{-1}=1.661 \times 10^{-24}$ moles .
so $\boldsymbol{P}=2.2907 \times 10^{4} \mathrm{kPa}$ (i.e. 229 atmospheres)
b). First, we need the number of moles of $\mathrm{C}_{60}$ in 1 gram:
$M_{\mathrm{r}}\left(\mathrm{C}_{60}\right)=60 \times 12.011=720.66 \mathrm{~g} \mathrm{~mol}^{-1}$
so $1 \mathrm{~g} \equiv 1.388 \times 10^{-3}$ moles.
Now, we need the number of moles of ${ }^{3} \mathrm{He}$ from 1 gram of $\mathrm{C}_{60}$ :
$\boldsymbol{n}=\boldsymbol{P V} / \boldsymbol{R} \boldsymbol{T} \quad\left(\boldsymbol{P}=1.00 \times 10^{5} \mathrm{~Pa}, \boldsymbol{T}=298 \mathrm{~K}\right)$
so $\boldsymbol{n}\left({ }^{3} \mathrm{He}\right)=1.00 \times 10^{5} \mathrm{~Pa} \times 1.15 \times 10^{-13} \mathrm{~m}^{3} /\left(8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1} \times 298 \mathrm{~K}\right)$
$\boldsymbol{n}\left({ }^{3} \mathrm{He}\right)=4.642 \times 10^{-12}$ moles $/$ gram $\mathrm{C}_{60}$.
[so only one in every $2.99 \times 10^{8}$ molecules of $\mathrm{C}_{60}$ contains a ${ }^{3} \mathrm{He}$ atom!] We shall denote the fraction of $\mathrm{C}_{60}$ molecules containing ${ }^{3} \mathrm{He}: f\left({ }^{3} \mathrm{He}\right)=3.34 \times 10^{-9}$.

This corresponds to an effective mean partial pressure:

$$
\boldsymbol{P}_{\text {mean }}\left({ }^{3} \mathrm{He}\right)=\boldsymbol{P}\left(\mathrm{He} @ \mathrm{C}_{60}\right) \times f\left({ }^{3} \mathrm{He}\right)=7.66 \times 10^{-5} \mathrm{kPa} .
$$

Similarly for ${ }^{4} \mathrm{He}$, we obtain
$\boldsymbol{n}\left({ }^{4} \mathrm{He}\right)=8.436 \times 10^{-9}$ moles $/$ gram $\mathrm{C}_{60},\left(f\left({ }^{4} \mathrm{He}\right)=6.08 \times 10^{-6}\right)$ and $\boldsymbol{P}_{\text {mean }}\left({ }^{4} \mathrm{He}\right)=0.139 \mathrm{kPa}$.
c). $\quad \boldsymbol{P}_{\text {atm }}=1.00 \times 10^{2} \mathrm{kPa}$.

The atmospheric partial pressure of ${ }^{4} \mathrm{He}$ equals total pressure $\times$ mole fraction $\left({ }^{4} \mathrm{He}\right)$ :
$\boldsymbol{P}\left({ }^{4} \mathrm{He}\right)_{\mathrm{atm}}=1.00 \times 10^{2} \mathrm{kPa} \times 5.24 \times 10^{-6}=5.24 \times 10^{-4} \mathrm{kPa}$.

The ${ }^{4} \mathrm{He}$ partial pressure in Earth's atmosphere is thus more than two orders of magnitude below that in the helium sample. The chemical interaction between ${ }^{4} \mathrm{He}$ and $\mathrm{C}_{60}$ is essentially nonexistent, and so cannot provide a driving force towards helium capture by $\mathrm{C}_{60}$ : it is difficult to understand how the mean ${ }^{4} \mathrm{He}$ pressure within $\mathrm{C}_{60}$ could exceed the ${ }^{4} \mathrm{He}$ partial pressure in the ambient atmosphere. Thus, the ${ }^{4} \mathrm{He}$ content of the sample does not appear to support a terrestrial-atmosphere origin. [The question leaves unmentioned the possibility that Earth's atmospheric pressure was several hundred times higher at some earlier time: with the same helium content, i.e. mole fraction, a terrestrial origin for the caged helium would then be feasible. However, this is not a likely scenario!]
d). The fullerene sample's ${ }^{3} \mathrm{He} /{ }^{4} \mathrm{He}$ ratio is $5.50 \times 10^{-4}: 1$, i.e. more than two orders of magnitude higher than the terrestrial atmospheric value. [Therefore, the ${ }^{3} \mathrm{He}$ partial pressure in the fullerene sample exceeds the current terrestrial atmospheric value by a factor of $1.12 \times 10^{5}$ !] The helium abundance ratio is definitely not in agreement with a terrestrial atmosphere origin for the caged helium in the fullerene. The implication is that the $\mathrm{He} @ \mathrm{C}_{60}$ was pre-existing within the meteorite, and survived the impact.
[As an aside, it is currently thought that the $\mathrm{He} @ \mathrm{C}_{60}$ within the meteorite is not only extraterrestrial in origin, but extrasolar as well: there are no environments in the solar system with a high enough helium pressure that don't also have very high pressures of $\mathrm{H}_{2}$ or other gases which inhibit fullerene formation. The best candidates (refer Science 272 (1996) 249) for the source of the ${\mathrm{He} @ \mathrm{C}_{60} \text { are a }}^{2}$ class of helium- and carbon-rich, hydrogen-poor red giant stars, whose outer envelopes are known to contain soot particles and which are all at least hundreds of light years distant ...]
e). i).To determine the fullerene's surface area, we need to define a two-dimensional graphitic unit cell:


The unit cell has sides of length $\left(\boldsymbol{r}(\mathrm{C}-\mathrm{C}) \times\left[2+2 \sin \left(30^{\circ}\right)\right]\right)$ and $(\boldsymbol{r}(\mathrm{C}-\mathrm{C}) \times$ $2 \cos \left(30^{\circ}\right)$ ), respectively: thus the area of this unit cell is $1.048 \times 10^{-19} \mathrm{~m}^{2}$.

The unit cell contains: 2 complete C atoms (shown in black)
2 half C atoms (grey)

> 4 quarter C atoms (white)
> i.e., 4 complete C atoms in total.

Therefore there is one complete $C$ atom per $2.62 \times 10^{-20} \mathrm{~m}^{2}$; and, since there are $5 \times 10^{9} \mathrm{C}$ atoms, the total surface area of the fullerene is

$$
\boldsymbol{A}=1.31 \times 10^{-10} \mathrm{~m}^{2}
$$

The area of a sphere is $\boldsymbol{A}=4 \pi \boldsymbol{r}^{2}$, so the fullerene has a radius of $3.23 \times$ $10^{-6} \mathrm{~m}$.

The volume of a sphere is $\boldsymbol{V}=(4 / 3) \pi \boldsymbol{r}^{3}$, so $\boldsymbol{V}=1.409 \times 10^{-16} \mathrm{~m}^{3}$.
ii). The fullerene's carbon shell has a density $\rho_{\mathrm{C}}=$ mass $/ \boldsymbol{V}$ :

$$
\begin{aligned}
& \text { mass }=5.0 \times 10^{9} \text { atoms } \times 12.011 \mathrm{~g} \mathrm{~mol}^{-1} /\left(6.02205 \times 10^{23} \text { atom } \mathrm{mol}^{-1}\right) \\
& \text { mass }=9.97 \times 10^{-14} \mathrm{~g} \\
& \text { so } \rho_{\mathrm{C}}=708 \mathrm{~g} \mathrm{~m}^{-3} .
\end{aligned}
$$

The fullerene's inner helium 'atmosphere' has a density:
$\rho_{\mathrm{He}}=\left(\boldsymbol{P}_{\mathrm{He}} / \boldsymbol{P}_{\mathrm{atm}}\right) \times\left(M_{\mathrm{r}}(\mathrm{He}) / \boldsymbol{V}_{\mathrm{mol}}\right)$,
where $\boldsymbol{V}_{\mathrm{mol}}$ is the molar volume at STP (i.e. $2.2414 \times 10^{-2} \mathrm{~m}^{3}$ ),
so $\rho_{\mathrm{He}}=214 \mathrm{~g} \mathrm{~m}^{-3}$.
The total density of the fullerene is $\rho_{\mathrm{tot}}=\rho_{\mathrm{C}}+\rho_{\mathrm{He}}=922 \mathrm{~g} \mathrm{~m}^{-3}$.
iii). The density of air is

$$
\rho_{\mathrm{air}}=M_{\mathrm{r}}(\mathrm{air}) / V_{\mathrm{mol}}=1294 \mathrm{~g} \mathrm{~m}^{-3} .
$$

iv). The helium-filled fullerene is less dense than air: a lighter-than-air solid! [Or, if you wish, a molecular helium balloon.]

## PROBLEM 18.

a). If we denote the initial activity as $\mathrm{I}_{0}$ (i.e. $7.0 \times 10^{7} \mathrm{~Bq} \mathrm{~mL}^{-1}$ in each case), and $\mathrm{I}_{\mathrm{t}}$ as the activity after a time $t$ has elapsed, then $I_{t}$ is defined as $I_{t}=I_{0} e^{-(t / t / 2)}$.

It will be helpful to convert all $\mathrm{t}_{1 / 2}$ values into minutes:

$$
\begin{aligned}
& \mathrm{t}_{1 / 2}\left({ }^{67} \mathrm{Ga}\right)=78.25 \mathrm{hr} \times 60 \mathrm{~min} \mathrm{hr} \\
& -1 \\
& \mathrm{t}_{1 / 2}\left({ }^{68} \mathrm{Ge}\right)=287 \text { days } \times 24 \mathrm{hr} \mathrm{day}^{-1} \times 60 \mathrm{~min} \mathrm{hr}^{-1}=4.133 \times 10^{5} \mathrm{~min}
\end{aligned}
$$

We can now determine i) $I_{\mathrm{t}}$, and ii) $I_{\mathrm{t}}$ after dilution [the latter quantity is (1/2500) of the former]:

| nuclide | $I_{t}$ | $I_{t}$ after dilution |
| :---: | :--- | :--- |


|  | $\left(\mathrm{Bq} \mathrm{mL}^{-1}\right)$ | $\left(\mathrm{Bq} \mathrm{mL}^{-1}\right)$ |
| :--- | :--- | :--- |
| ${ }^{71} \mathrm{Zn}$ | 261 | 0.104 |
| ${ }^{67} \mathrm{Ga}$ | $6.96 \times 10^{7}$ | $2.78 \times 10^{4}$ |
| ${ }^{68} \mathrm{Ge}$ | $6.9995 \times 10^{7}$ | $2.80 \times 10^{4}$ |

b). $\quad{ }^{71} \mathrm{Zn}$ has too short a half-life to remain active for long: after 30 minutes, almost all of the activity has ceased. The count rate, especially after dilution into the patient's blood volume, is too low to give a reliable measurement. Furthermore, such a short half-life means that the nuclide needs to be synthesized for each patient: it has negligible storage time!
${ }^{68} \mathrm{Ge}$ has the opposite problem: it's still almost as active after 30 minutes, and with a half-life of almost a year will remain active over a very long time. If the nuclide is retained within the patient, this means that the patient is being subjected to an unacceptably high dose of radiation over this period, with consequent dangers of cellular damage etc.
${ }^{67} \mathrm{Ga}$ has a lifetime which is sufficiently long for convenience, but sufficiently short that a reliable measurement (of blood volume) can be made using a comparatively small dose of radioactive material.
c).

$$
\begin{array}{ll}
{ }_{30}^{71} \mathrm{Zn} & \rightarrow \\
{ }_{31}^{71} \mathrm{Ga}+{ }_{-1}^{0} \mathrm{e} \quad(+\gamma) \\
{ }_{31}^{67} \mathrm{Ga}+{ }_{-1}^{0} \mathrm{e} & \rightarrow \\
{ }_{30}^{67} \mathrm{Zn}(+\gamma) \\
{ }_{32}^{68} \mathrm{Ge}+{ }_{-1}^{0} \mathrm{e} & \rightarrow \\
{ }_{31}^{68} \mathrm{Ga}(+\gamma)
\end{array}
$$

d). i). The radiopharmaceutical initially contains $\left(1.025 \times 10^{-2} \mathrm{~g} / 69.72 \mathrm{~g} \mathrm{~mol}^{-1}=\right)$ $1.47 \times 10^{-4}$ moles Ga , and therefore contains $\left(1.47 \times 10^{-4} \times 5.0 \times 10^{-7}=\right) 7.35 \times$ $10^{-11}$ moles of ${ }^{67} \mathrm{Ga}$ (i.e. $4.43 \times 10^{13}$ atoms of this nuclide).

For radioactive decay, first-order kinetics gives

$$
\text { Rate }=\mathrm{I}_{\mathrm{t}}=k n_{\mathrm{t}}\left({ }^{67} \mathrm{Ga}\right),
$$

(where $\mathrm{I}_{\mathrm{t}}$ is in Becquerels and $n_{\mathrm{t}}\left({ }^{67} \mathrm{Ga}\right.$ ) is the number of atoms of ${ }^{67} \mathrm{Ga}$ present at time t ),
and $k=\ln (2) / \mathrm{t}_{1 / 2}$, where $\mathrm{t}_{1 / 2}=78.25 \mathrm{hr}=2.817 \times 10^{5} \mathrm{~s}$.
Thus, $k=2.461 \times 10^{-6} \mathrm{~s}^{-1}$ and $\mathrm{I}_{0}=1.09 \times 10^{8} \mathrm{~Bq}$ (in 100 mL at $\mathrm{t}=0$ ).
In the 1 mL dose at $\mathrm{t}=8 \mathrm{hr}$,

$$
\begin{aligned}
& \mathrm{I}_{\mathrm{t}}=I_{0} \mathrm{e}^{-\left(\mathrm{t} / \mathrm{t}_{1 / 2}\right)} \times V_{\text {dose }} / V_{\text {total }}=1.09 \times 10^{8} \mathrm{~Bq} \times \mathrm{e}^{-(8 / 78.25)} \times 1 / 100 \\
& \mathrm{I}_{\mathrm{t}}=9.84 \times 10^{5} \mathrm{~Bq} .
\end{aligned}
$$

ii). The residual activity of the 1 mL dose after a further hour would be

$$
\mathrm{I}_{\mathrm{t}}=9.84 \times 10^{5} \mathrm{~Bq} \times \mathrm{e}^{-(1 / 78.25)}=9.72 \times 10^{5} \mathrm{~Bq} .
$$

Comparison of this activity, with that observed for the 1 mL blood sample, yields the dilution factor:

Dilution factor $=9.72 \times 10^{5} / 105.6=9201$.
The patient's blood volume is thus 9.20 litres.

## PROBLEM 19.

a). Metallic uranium has an oxidation state of zero, by definition. Oxidation states for the other species: $\mathrm{U}(\mathrm{III})\left[\mathrm{U}^{3+}\right] ; \mathrm{U}(\mathrm{IV})\left[\mathrm{U}^{4+}\right] ; \mathrm{U}(\mathrm{V})\left[\mathrm{UO}_{2}{ }^{+}\right] ; \mathrm{U}(\mathrm{VI})\left[\mathrm{UO}_{2}{ }^{2+}\right]$.
b). The conditions described are standard conditions, so we can use standard reduction potentials to determine in which directions the reactions are spontaneous. We must also consider the reduction step:

$$
2 \mathrm{H}^{+}+2 \mathrm{e} \quad \rightarrow \quad \mathrm{H}_{2} \quad \mathrm{E}^{\circ}=0.000 \mathrm{~V} \text { by definition. }
$$

Two half-reactions involve metallic U:

$$
\begin{array}{lll}
\mathrm{U}^{3+}+3 \mathrm{e} & \rightarrow & \mathrm{U} \\
\mathrm{UO}_{2}^{2+}+4 \mathrm{H}^{+}+6 \mathrm{e} & \rightarrow & \mathrm{U}+2 \mathrm{H}_{2} \mathrm{O}
\end{array}
$$

these will form the starting points for oxidation of the uranium:

$$
\begin{array}{llll}
2 \mathrm{U}+6 \mathrm{H}^{+} & \rightarrow & 2 \mathrm{U}^{3+}+3 \mathrm{H}_{2} & \mathrm{E}_{\text {cell }}^{\circ}=+1.798 \mathrm{~V} \\
\mathrm{U}+2 \mathrm{H}^{+}+2 \mathrm{H}_{2} \mathrm{O} & \rightarrow & \mathrm{UO}_{2}^{2+}+3 \mathrm{H}_{2} & \mathrm{E}_{\text {cell }}^{\circ}=+1.444 \mathrm{~V}
\end{array}
$$

Regardless of which of these processes is favoured, neither of the 'primary products', $\mathrm{U}^{3+}$ or $\mathrm{UO}_{2}{ }^{2+}$, is the ultimate product.
$\mathrm{U}(\mathrm{III})$ is spontaneously oxidized to $\mathrm{U}(\mathrm{IV})$ :

$$
2 \mathrm{U}^{3+}+2 \mathrm{H}^{+} \quad \rightarrow \quad 2 \mathrm{U}^{4+}+\mathrm{H}_{2} \quad \mathrm{E}_{\text {cell }}^{\circ}=+0.607 \mathrm{~V}
$$

while $U(V I)$ is spontaneously reduced to either $U(I V)$ or $U(V)$ :

$$
\begin{array}{llll}
\mathrm{UO}_{2}^{2+}+2 \mathrm{H}^{+}+\mathrm{H}_{2} & \rightarrow & \mathrm{U}^{4+}+2 \mathrm{H}_{2} \mathrm{O} & \mathrm{E}_{\text {cell }}^{\circ}=+0.327 \mathrm{~V} \\
2 \mathrm{UO}_{2}^{2+}+\mathrm{H}_{2} & \rightarrow & 2 \mathrm{UO}_{2}^{+}+2 \mathrm{H}^{+} & \mathrm{E}_{\text {cell }}^{\circ}=+0.062 \mathrm{~V}
\end{array}
$$

and $\mathrm{U}(\mathrm{V})$ is also spontaneously reduced to $\mathrm{U}(\mathrm{IV})$ :

$$
2 \mathrm{UO}_{2}^{+}+6 \mathrm{H}^{+}+\mathrm{H}_{2} \rightarrow 2 \mathrm{U}^{4+}+4 \mathrm{H}_{2} \mathrm{O} \quad \mathrm{E}_{\text {cell }}^{\circ}=+0.620 \mathrm{~V}
$$

Since $\mathrm{U}^{4+}$ is the only species which cannot spontaneously react with $\mathrm{H}^{+}$or $\mathrm{H}_{2}$, this is the species which will ultimately predominate in aqueous solutions under these conditions.
[A codicil to the above is that, while metallic U is still present, the process

$$
\mathrm{U}^{4+}+3 \mathrm{U} \quad \rightarrow \quad 4 \mathrm{U}^{3+} \quad \mathrm{E}^{\circ}{ }_{\text {cell }}=+1.191 \mathrm{~V}
$$

is favourable, but can only occur until the $U$ is exhausted, after which time $U$ (III) will be oxidized to $\mathrm{U}(\mathrm{IV})$ as above.]
c). Since conditions are standard except for $\left[\mathrm{H}^{+}\right]=1.0 \times 10^{-6} \mathrm{~mol} \mathrm{~L}^{-1}$, we can use a simplified form of the Nernst equation as follows, for the relevant equations:

$$
\begin{array}{ccc}
2 \mathrm{U}+6 \mathrm{H}^{+} & \rightarrow & 2 \mathrm{U}^{3+}+3 \mathrm{H}_{2} \\
\mathrm{E}_{\text {cell }}=\mathrm{E}_{\text {cell }}^{\circ}-(\mathrm{RT} / 6 \mathrm{~F}) \ln \left(\left[\mathrm{H}^{+}\right]^{-6}\right)=+1.444 \mathrm{~V} & \mathrm{E}_{\text {cell }}^{\circ}=+1.798 \mathrm{~V} \\
\mathrm{U}+2 \mathrm{H}^{+}+2 \mathrm{H}_{2} \mathrm{O} & \rightarrow \quad \mathrm{UO}_{2}^{2+}+3 \mathrm{H}_{2} & \mathrm{E}_{\text {cell }}^{\circ}=+1.444 \mathrm{~V} \\
\mathrm{E}_{\text {cell }}=\mathrm{E}^{\circ}{ }_{\text {cell }}-(\mathrm{RT} / 6 \mathrm{~F}) \ln \left(\left[\mathrm{H}^{+}\right]^{-2}\right)=+1.326 \mathrm{~V} & \\
2 \mathrm{U}^{3+}+2 \mathrm{H}^{+} & \rightarrow \quad 2 \mathrm{U}^{4+}+\mathrm{H}_{2} & \mathrm{E}_{\text {cell }}^{\circ}=+0.607 \mathrm{~V} \\
\mathrm{E}_{\text {cell }}=\mathrm{E}_{\text {cell }}^{\circ}-(\mathrm{RT} / 2 \mathrm{~F}) \ln \left(\left[\mathrm{H}^{+}\right]^{-2}\right)=0.253 \mathrm{~V} & \\
\mathrm{UO}_{2}^{2+}+2 \mathrm{H}^{+}+\mathrm{H}_{2} \quad \rightarrow \quad \mathrm{U}^{4+}+2 \mathrm{H}_{2} \mathrm{O} & \mathrm{E}_{\text {cell }}^{\circ}=+0.327 \mathrm{~V} \\
\mathrm{E}_{\text {cell }}=\mathrm{E}_{\text {cell }}^{\circ}-(\mathrm{RT} / 2 \mathrm{~F}) \ln \left(\left[\mathrm{H}^{+}\right]^{-2}\right)=-0.027 \mathrm{~V} & \\
2 \mathrm{UO}_{2}^{2+}+\mathrm{H}_{2} & \rightarrow \quad 2 \mathrm{UO}_{2}^{+}+2 \mathrm{H}^{+} & \mathrm{E}_{\text {cell }}^{\circ}=+0.062 \mathrm{~V} \\
\mathrm{E}_{\text {cell }}=\mathrm{E}_{\text {cell }}^{\circ}-(\mathrm{RT} / 2 \mathrm{~F}) \ln \left(\left[\mathrm{H}^{+}\right]^{2}\right)=+0.293 \mathrm{~V} & \\
2 \mathrm{UO}_{2}^{++}+6 \mathrm{H}^{+}+\mathrm{H}_{2} \quad \rightarrow \quad 2 \mathrm{U}^{4+}+4 \mathrm{H}_{2} \mathrm{O} & \mathrm{E}_{\text {cell }}^{\circ}=+0.620 \mathrm{~V} \\
\mathrm{E}_{\text {cell }}=\mathrm{E}_{\text {cell }}^{\circ}-(\mathrm{RT} / 2 \mathrm{~F}) \ln \left(\left[\mathrm{H}^{+}\right]^{-6}\right)=-0.444 \mathrm{~V} &
\end{array}
$$

All of the above processes have positive $\mathrm{E}^{\circ}$ cell values for reaction as written in the forward direction, and so all are spontaneous in this direction at $\mathrm{pH}=0$. In contrast, $\mathrm{U}(\mathrm{VI}) \rightarrow \mathrm{U}(\mathrm{IV})$ and $\mathrm{U}(\mathrm{V}) \rightarrow \mathrm{U}(\mathrm{IV})$ are spontaneous in the reverse direction at $\mathrm{pH}=6$ (as indicated by the negative $\mathrm{E}_{\text {cell }}$ values): $\mathrm{U}(\mathrm{IV})$ is now oxidized to $U(V)$ or $U(V I)$. Since $U(V I)$ is now the only oxidation state which will not react spontaneously with either $\mathrm{H}^{+}$or $\mathrm{H}_{2}$ under these conditions, the dominant species will be $\mathrm{UO}_{2}{ }^{2+}$.
d). To solve this, we need to consider only those reactions in which $\mathrm{UO}_{2}{ }^{+}$appears:

$$
\begin{aligned}
& 2 \mathrm{UO}_{2}^{2+}+\mathrm{H}_{2} \quad \rightarrow \quad 2 \mathrm{UO}_{2}^{+}+2 \mathrm{H}^{+} \quad \mathrm{E}^{\circ}{ }_{\text {cell }}=+0.062 \mathrm{~V} \\
& \mathrm{E}_{\text {cell }}=\mathrm{E}^{\circ}{ }_{\text {cell }}-(\mathrm{RT} / 2 \mathrm{~F}) \ln \left(\left[\mathrm{H}^{+}\right]^{2} \mathrm{P}\left(\mathrm{H}_{2}\right)^{-2}\right) \\
& 2 \mathrm{UO}_{2}^{+}+6 \mathrm{H}^{+}+\mathrm{H}_{2} \quad \rightarrow \quad 2 \mathrm{U}^{4+}+4 \mathrm{H}_{2} \mathrm{O} \quad \mathrm{E}^{\circ} \text { cell }=+0.620 \mathrm{~V} \\
& \mathrm{E}_{\text {cell }}=\mathrm{E}^{\circ} \text { cell }-(\mathrm{RT} / 2 \mathrm{~F}) \ln \left(\left[\mathrm{H}^{+}\right]^{-6} \mathrm{P}\left(\mathrm{H}_{2}\right)^{-2}\right)
\end{aligned}
$$

At the threshold conditions, $\mathrm{E}_{\text {cell }}=0$, which corresponds to the following cases:

$$
\begin{aligned}
& \left.\left[\mathrm{H}^{+}\right]=\left\{\mathrm{P}\left(\mathrm{H}_{2}\right)^{2} \mathrm{e}^{\left(2 \mathrm{FE}^{\circ}\right. \text { cell }} / \mathrm{RT}\right)\right\}^{1 / 2} \text { for } \mathrm{U}(\mathrm{VI}) \rightleftharpoons \mathrm{U}(\mathrm{~V}) \text {, and } \\
& {\left[\mathrm{H}^{+}\right]=\left\{\mathrm{e}^{\left(-2 \mathrm{FE}^{\circ}{ }_{\text {cell }} / \mathrm{RT}\right)} / \mathrm{P}\left(\mathrm{H}_{2}\right)^{2}\right\}^{1 / 6} \text { for U(IV) } \rightleftharpoons \mathrm{U}(\mathrm{~V}) .}
\end{aligned}
$$

These expressions yield threshold values of:
i). $\quad\left[\mathrm{H}^{+}\right]<11.2 \mathrm{~mol} \mathrm{~L}{ }^{-1}$, i.e. $\mathrm{pH}>-1$ for $\mathrm{U}(\mathrm{V})$ to be stable against $\mathrm{U}(\mathrm{VI})$, and $\left[\mathrm{H}^{+}\right]<3.19 \times 10^{-4} \mathrm{~mol} \mathrm{~L}^{-1}$, i.e. $\mathrm{pH}>3.50$ for $\mathrm{U}(\mathrm{V})$ stable versus $\mathrm{U}(\mathrm{IV})$.
ii). $\left[\mathrm{H}^{+}\right]<1.12 \times 10^{-5} \mathrm{~mol} \mathrm{~L}^{-1}$, i.e. $\mathrm{pH}>4.95$ for $\mathrm{U}(\mathrm{V})$ stable against $\mathrm{U}(\mathrm{VI})$, and $\left[\mathrm{H}^{+}\right]<3.19 \times 10^{-2} \mathrm{~mol} \mathrm{~L}^{-1}$, i.e. $\mathrm{pH}>1.50$ for $\mathrm{U}(\mathrm{V})$ stable versus $\mathrm{U}(\mathrm{IV})$.

Thus $\mathrm{UO}_{2}{ }^{+}$is seen to be stable against other oxidation states over a pH range of 3.5-7 (we are considering only acidic or neutral solutions) under a standard hydrogen atmosphere, but is stable against oxidation to $\mathrm{U}(\mathrm{VI})$ only at pH values greater than 4.95 .

The $\mathrm{H}_{2}$ partial pressure in the atmosphere is very low, so the latter conditions (ie ii)) correspond more closely to those encountered in typical terrestrial environments. $\mathrm{UO}_{2}{ }^{+}$isn't actually as stable as its standard cell potentials would suggest.

## PROBLEM 20.

a). The colour is due to nitrogen dioxide, $\mathrm{NO}_{2}$. Since air is $78 \% \mathrm{~N}_{2}$ and $21 \% \mathrm{O}_{2}$, oxygen is the limiting reagent: if there is complete conversion of $\mathrm{O}_{2}$ to $\mathrm{NO}_{2}$ (which is very unlikely), the nitrogen oxide concentration will be:
$\left[\mathrm{NO}_{2}\right]=0.21\left(\right.$ mole $\%$ of $\left.\mathrm{O}_{2}\right) / 22.414 \mathrm{~L} \mathrm{~mol}^{-1}$ (molar volume at STP) $=9.4 \times 10^{-3} \mathrm{~mol} \mathrm{~L}^{-1}$
b). $2 \mathrm{NO}+\mathrm{O}_{2} \quad \rightarrow \quad 2 \mathrm{NO}_{2}$.
c). i). Orders for NO and $\mathrm{O}_{2}$ can be found from those measurements in which one or other concentration is held approximately constant (i.e. [NO] is essentially constant in measurements \#1, 2, \& 3, while [ $\mathrm{O}_{2}$ ] is similar for \#2, 4, and 5):

Order with respect to NO:

| Measurements | [NO] ratio | Initial rate ratio |
| :---: | :---: | :---: |
| $\# 4: \# 2$ | 2.01 | 4.03 |
| $\# 4: \# 5$ | 4.02 | 15.9 |
| $\# 2: \# 5$ | 2.00 | 3.95 |

The rate is observed to vary as $[\mathrm{NO}]^{2}$ : therefore the reaction is second order in NO.

Order with respect to $\mathrm{O}_{2}$ :

| Measurements | $\left[\mathrm{O}_{2}\right]$ ratio | Initial rate ratio |
| :---: | :---: | :---: |
| $\# 2: \# 1$ | 1.99 | 1.98 |


| $\# 2: \# 3$ | 3.85 | 3.65 |
| :--- | :--- | :--- |
| $\# 1: \# 3$ | 1.93 | 1.84 |

The rate varies essentially as [ $\mathrm{O}_{2}$ ]: the reaction is first order in $\mathrm{O}_{2}$, and is therefore third order overall.
ii). The rate law is

$$
\text { rate }=k[\mathrm{NO}]^{2}\left[\mathrm{O}_{2}\right] \quad \text { so } k=\operatorname{rate} /\left([\mathrm{NO}]^{2}\left[\mathrm{O}_{2}\right]\right)
$$

The various measurements yield the following:

| Measurement | $k$ |
| :---: | :---: |
| $\# 1$ | $7.063 \times 10^{3} 1^{2} \mathrm{~mol}^{-2} \mathrm{~s}^{-1}$ |
| $\# 2$ | $7.154 \times 10^{3} 1^{2} \mathrm{~mol}^{-2} \mathrm{~s}^{-1}$ |
| $\# 3$ | $7.159 \times 10^{3} 1^{2} \mathrm{~mol}^{-2} \mathrm{~s}^{-1}$ |
| $\# 4$ | $7.117 \times 10^{3} 1^{2} \mathrm{~mol}^{-2} \mathrm{~s}^{-1}$ |
| $\# 5$ | $7.165 \times 10^{3} 1^{2} \mathrm{~mol}^{-2} \mathrm{~s}^{-1}$ |

Mean value: $k=7.13 \times 10^{3} 1^{2} \mathrm{~mol}^{-2} \mathrm{~s}^{-1}$.
d). i). Measurements $\# 1,2, \& 3$ feature essentially the same initial [NO], with [ $\mathrm{O}_{2}$ ] varying substantially: the stoichiometric excess of [ $\mathrm{O}_{2}$ ] over [ NO ] is only $7.2 \times$ $10^{-6} \mathrm{~mol} \mathrm{~L}^{-1}$ for measurement \#3, but $3.67 \times 10^{-4} \mathrm{~mol} \mathrm{~L}^{-1}$ for measurement \#2. Thus, if the reaction has not gone to completion, then the $\mathrm{A}_{\infty}:[\mathrm{NO}]_{\text {initial }}$ ratio should vary significantly: but for all of the first three measurements, the ratio of $\mathrm{A}_{\infty}:[\mathrm{NO}]_{\text {initial }}$ is virtually constant. Therefore the reaction has gone to completion, or near enough.
ii). Beer's law defines absorbance:

$$
\mathrm{A}=\ln \left(\mathrm{I}_{0} / \mathrm{I}\right)=\varepsilon \mathrm{c} \mathrm{l},
$$

where $\mathrm{c}=\left[\mathrm{NO}_{2}\right]=[\mathrm{NO}]_{\text {initial }}$ (since reaction has gone to completion, and since NO is the limiting reagent)

$$
\text { and } 1=10 \mathrm{~cm} .
$$

Using measurement \#1 as an example yields

$$
\begin{aligned}
& \varepsilon=\mathrm{A}_{\infty} / \mathrm{cl}=0.341 /\left(1.16 \times 10^{-4} \times 10\right) \\
& =294 \mathrm{~L} \mathrm{~cm}^{-1} \mathrm{~mol}^{-1}
\end{aligned}
$$

iii). $\mathrm{NO}_{2}$ is brown. Of the colours of the visible spectrum, this is closest to orange; thus, if brown is being transmitted, then the colour complement (i.e. blue) is being absorbed. This is consistent with peak absorption at about 400 nm .
e). Compare the volume with PV:

| $\mathrm{V}(\mathrm{mL})$ | $\mathrm{PV}(\operatorname{atm~mL})$ |
| :---: | :---: |
| 1000 | 2.49 |
| 500 | 2.45 |
| 200 | 2.36 |
| 100 | 2.25 |
| 50 | 2.12 |
| 20 | 1.92 |
| 10 | 1.78 |

PV is proportional to the number of moles of gas present in the container. Evidently, the number of moles of gas is decreasing as V decreases. This is due to the following equilibrium:

$$
2 \mathrm{NO}_{2(\mathrm{~g})} \rightleftharpoons \mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g})
$$

If we assume that the pressure at $\mathrm{V}=1000 \mathrm{~mL}$ is due to $\mathrm{NO}_{2}$ only (which is a fair initial approximation, since PV changes only slightly between 1000 and 200 mL ), then we can determine $\mathrm{P}\left(\mathrm{NO}_{2}\right)$ and $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)$ for any other volume, since there is a conversion of 2 moles $\rightarrow 1$ mole in going from left to right:

$$
\begin{aligned}
& \mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right)=\mathrm{P}(1000 \mathrm{~mL}) \times(1000 / \mathrm{V})-\mathrm{P}_{t o t} \\
& \mathrm{P}\left(\mathrm{NO}_{2}\right)=\mathrm{P}_{\text {tot }}-\mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right) .
\end{aligned}
$$

For the measurement at 10 mL , for example,

$$
\begin{aligned}
& \mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right)=7.1 \times 10^{-2} \mathrm{~atm} \\
& \mathrm{P}\left(\mathrm{NO}_{2}\right)=0.107 \mathrm{~atm} \\
& K_{\mathrm{P}}=\mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right) /\left(\mathrm{P}_{2}\left(\mathrm{NO}_{2}\right)^{2}\right)=6.20 .
\end{aligned}
$$

We can now use this value to test whether our hypothesis, that only $\mathrm{NO}_{2}$ is present at $\mathrm{V}=1000 \mathrm{~mL}$, is correct. From $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)=6.20 \times \mathrm{P}\left(\mathrm{NO}_{2}\right)^{2}$, and assuming $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right) \ll \mathrm{P}\left(\mathrm{NO}_{2}\right)$, we get $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)=3.84 \times 10^{-5} \mathrm{~atm}$ (and, by subtraction from $\left.\mathrm{P}_{\text {tot }}, \mathrm{P}\left(\mathrm{NO}_{2}\right)=2.45 \times 10^{-3} \mathrm{~atm}\right)$ at $\mathrm{V}=1000 \mathrm{~mL}$. This means we need to revise our equations for the partial pressures:

$$
\begin{aligned}
& \mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right)=2.53 \times 10^{-3} \mathrm{~atm} \times(1000 / \mathrm{V})-\mathrm{P}_{t o t} \\
& \mathrm{P}\left(\mathrm{NO}_{2}\right)=\mathrm{P}_{t o t}-\mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right)
\end{aligned}
$$

where $2.53 \times 10^{-3}$ atm is $2 \mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)+\mathrm{P}\left(\mathrm{NO}_{2}\right)$ at $\mathrm{V}=1000 \mathrm{~mL}$, i.e. the total pressure if all $\mathrm{N}_{2} \mathrm{O}_{4}$ was converted to $\mathrm{NO}_{2}$ at this volume.

We can now recalculate $K_{\mathrm{P}}$ from the $\mathrm{V}=10 \mathrm{~mL}$ measurement. [Any other measurement would also serve for this purpose, but the lowest volume will have
the highest $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right): \mathrm{P}\left(\mathrm{NO}_{2}\right)$ ratio and thus the least uncertainty in $K_{\mathrm{P}}$.] At $\mathrm{V}=$ 10 mL , we now obtain

$$
\begin{aligned}
& \mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right)=7.5 \times 10^{-2} \mathrm{~atm} \\
& \mathrm{P}\left(\mathrm{NO}_{2}\right)=0.103 \mathrm{~atm} \\
& K_{\mathrm{P}}=\mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right) /\left(\mathrm{P}_{2}\left(\mathrm{NO}_{2}\right)^{2}\right)=7.07
\end{aligned}
$$

Using this revised value of $K_{\mathrm{P}}$, for the $\mathrm{V}=1000 \mathrm{~mL}$ data, yields in turn $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)=$ $4.24 \times 10^{-5} \mathrm{~atm}$ at 1000 mL . While this is somewhat higher than the value determined on the first iteration, it does not make any significant difference to the quantity $2 \mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)+\mathrm{P}\left(\mathrm{NO}_{2}\right)$ : consequently we have arrived at a self-consistent solution, within the accuracy of the quoted measurements, of $K_{\mathrm{P}}=7.07$.
f). The process responsible is the condensation of $\mathrm{N}_{2} \mathrm{O}_{4}$ at sufficiently high pressure:

$$
\mathrm{N}_{2} \mathrm{O}_{4(\mathrm{~g})} \rightleftharpoons \mathrm{N}_{2} \mathrm{O}_{4}(l) .
$$

The pressure stabilizes because gaseous $\mathrm{N}_{2} \mathrm{O}_{4}$ is in equilibrium with its liquid form, and so $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)$ cannot exceed the $\mathrm{N}_{2} \mathrm{O}_{4}$ vapour pressure; equilibrium also continues to exist between $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$, as governed by $K_{\mathrm{P}}$, and since $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)$ is constrained, $\mathrm{P}\left(\mathrm{NO}_{2}\right)$ is also fixed. The pressure will remain constant with continued compression [until the liquid itself begins to become compressed].

We can determine $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)$ and $\mathrm{P}\left(\mathrm{NO}_{2}\right)$ from $K_{\mathrm{P}}$ and $\mathrm{P}_{t o t}$ :

$$
\begin{array}{ll} 
& 2 \mathrm{NO}_{2}(\mathrm{~g}) \\
& \mathrm{P}\left(\mathrm{NO}_{2}\right)=\boldsymbol{x} \mathrm{atm} \\
& \mathrm{P}\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right)=(1.215-\boldsymbol{x}) \mathrm{atm} \\
& K_{\mathrm{P}}=7.07=(1.215-\boldsymbol{g}) / x^{2} \\
\Rightarrow \quad & 7.07 \boldsymbol{x}^{2}+\boldsymbol{x}-1.215=0
\end{array}
$$

Solution of this quadratic yields $\mathrm{P}\left(\mathrm{NO}_{2}\right)=\boldsymbol{x}=0.350 \mathrm{~atm}$ and $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)=0.865$ atm at $\mathrm{V}=1 \mathrm{~mL}$.

The equilibrium constant for $\mathrm{N}_{2} \mathrm{O}_{4}$ condensation is, by definition, $K_{\mathrm{P}}=\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)^{-1}$. [The activity of pure $\mathrm{N}_{2} \mathrm{O}_{4}$ (l) is unity, and so does not appear in the equilibrium constant.] From $\mathrm{P}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)=0.865 \mathrm{~atm}$ in equilibrium with the liquid, we find:

$$
K_{\mathrm{P}}=1.156
$$

## PROBLEM 21.

a). The following values are obtained:

| pH | $\alpha_{\mathrm{Y}^{4}}$ | $\left[\mathrm{Y}^{4-}\right] / \mathrm{mol} \mathrm{L}^{-1}$ |
| :---: | :---: | :---: |


| 2 | $3.712 \times 10^{-14}$ | $8.26 \times 10^{-16}$ |
| :---: | :---: | :---: |
| 6 | $2.249 \times 10^{-6}$ | $5.01 \times 10^{-8}$ |
| 10 | 0.3548 | $7.90 \times 10^{-3}$ |

The anion concentrations are determined using $\mathrm{C}_{\mathrm{T}}($ EDTA $)=0.02226 \mathrm{~mol} \mathrm{~L}^{-1}$ $\left(\mathrm{M}_{\mathrm{r}}\left(\mathrm{C}_{10} \mathrm{H}_{16} \mathrm{~N}_{2} \mathrm{O}_{8}\right)=292.25 \mathrm{~g} \mathrm{~mol}^{-1}\right)$.
b). We need to determine the ratio $\left[\mathrm{MY}^{2-}\right] /\left[\mathrm{M}^{2+}\right]$, which (by the definition of the complex formation constant) has the value $K_{\mathrm{Y}}\left[\mathrm{Y}^{4}\right]$. We can determine [ $\mathrm{Y}^{4-}$ ] from x determined in a). This yields values:

| pH | $\left[\mathrm{Y}^{4-}\right]$ | $\left[\mathrm{HgY}^{2-}\right] /\left[\mathrm{Hg}^{2+}\right]$ | $\left[\mathrm{FeY}^{2-}\right] /\left[\mathrm{Fe}^{2+}\right]$ | $\left[\mathrm{CaY}^{2-}\right] /\left[\mathrm{Ca}^{2+}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 2 | $1.856 \times 10^{-16}$ | $1.17 \times 10^{6}$ | 0.039 | $9.28 \times 10^{-6}$ |
| 6 | $1.1245 \times 10^{-8}$ | $7.08 \times 10^{13}$ | $2.36 \times 10^{6}$ | 562 |
| 10 | $1.774 \times 10^{-3}$ | $1.12 \times 10^{19}$ | $3.73 \times 10^{11}$ | $8.87 \times 10^{7}$ |

It can be seen that, at $\mathrm{pH}=2$, only $\mathrm{Hg}^{2+}$ forms a complex in essentially quantitative yield; at $\mathrm{pH}=6$, both $\mathrm{Hg}^{2+}$ and $\mathrm{Fe}^{2+}$ do so, while at $\mathrm{pH}=10$, all three metal ions form complexes with high efficiency.
c). Since HCl is a strong acid, the equilibrium between $\mathrm{Hg}^{2+}$ and $\mathrm{Cl}^{-}$should be $\mathrm{pH}-$ independent: we can calculate that $\left[\mathrm{HgCl}_{4}{ }^{2-}\right]$ / $\left[\mathrm{Hg}^{2+}\right]$ will have a value of $2.488 \times$ $10^{14}$ for $\left[\mathrm{Cl}^{-}\right]=0.5 \mathrm{~mol} \mathrm{~L}^{-1}$. Using the $\left[\mathrm{HgY}^{2-}\right] /\left[\mathrm{Hg}^{2+}\right]$ values obtained in b ), we find

| pH | $\left[\mathrm{HgY}^{2-}\right] /\left[\mathrm{Hg}^{2+}\right]$ | $\%\left(\mathrm{Hg}^{2+}\right)$ | $\%\left(\mathrm{HgY}^{2-}\right)$ | $\%\left(\mathrm{HgCl}_{4}{ }^{2-}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| 2 | $1.17 \times 10^{6}$ | $4 \times 10^{-13}$ | $5 \times 10^{-7}$ | $>99.9$ |
| 6 | $7.08 \times 10^{13}$ | $3 \times 10^{-13}$ | 22.2 | 78.8 |
| 10 | $1.12 \times 10^{19}$ | $9 \times 10^{-18}$ | $>99.9$ | $2.2 \times 10^{-3}$ |

d). The results from b ) indicate that, at $\mathrm{pH}=2$, the EDTA complexation of $\mathrm{Ca}^{2+}$ is negligible: we can presume that at $\mathrm{pH}=2.6$ this will still be the case, and so the EDTA is reacting only with $\mathrm{Hg}^{2+}$ at such a low pH . At $\mathrm{pH}=10$, the complexation of both $\mathrm{Hg}^{2+}$ and $\mathrm{Ca}^{2+}$ is essentially quantitative, and so at $\mathrm{pH}=9.5$ the titration tells us the total quantity of $\mathrm{Hg}^{2+}$ and $\mathrm{Ca}^{2+}$. We must assume that EDTA does not significantly react with $\mathrm{Na}^{+}$.

At a pH of 2.6 , moles $\mathrm{Y}^{4-}=5.391 \times 10^{-4}$ moles.
This is equal to moles $\left(\mathrm{Hg}^{2+}\right)$ in 25 mL ; so moles $\left(\mathrm{Hg}^{2+}\right)$ in $500 \mathrm{~mL}=1.078 \times 10^{-4}$ moles. Since the atomic mass of Hg is $200.59 \mathrm{~g} \mathrm{~mol}^{-1}$, this indicates a mass of mercury, within the sample, of 2.163 g .

At a pH of 9.5 , moles $\mathrm{Y}^{4-}=7.006 \times 10^{-4}$ moles.

This is equal to moles $\left(\mathrm{Hg}^{2+}+\mathrm{Ca}^{2+}\right)$ in 10 mL ; so moles $\left(\mathrm{Hg}^{2+}+\mathrm{Ca}^{2+}\right)$ in 500 mL $=3.503 \times 10^{-2}$ moles, and therefore moles $\left(\mathrm{Ca}^{2+}\right)$ in $500 \mathrm{~mL}=2.425 \times 10^{-2}$ moles. This corresponds to 0.972 g of calcium within the sample.

By subtraction, the mass of sodium in the sample (assuming no other contamination) is 2.083 g . Thus the sample's content is: Hg ( $41.45 \%$ ), Na (39.92\%), Ca (18.63\%).

## PROBLEM 22.

a). Greenhouse gases warm the lower atmosphere, because some IR photons (originating from Earth's surface) which would otherwise escape from the atmosphere are absorbed and re-emitted; the re-emission is as likely to be back towards the surface as away from it, and so a warming of the lower atmosphere results.
b). Greenhouse gases cool the upper atmosphere: because fewer IR photons manage to reach this altitude from the surface, less IR absorption occurs at 15 km than would otherwise be the case. Less absorption implies lower temperatures.
c). The equilibria in question are

$$
\begin{aligned}
& \mathrm{CO}_{2(a q)} \\
\text { and } & =\mathrm{CO}_{2(\mathrm{~g})} \\
\mathrm{H}_{2} \mathrm{O}_{(\mathrm{l})} & =\mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})} .
\end{aligned}
$$

Both of these equilibria will move to the right as the temperature increases: thus the concentration of water vapour, and of $\mathrm{CO}_{2}$, will increase with T . Since both of these species are greenhouse gases, there is a degree of positive feedback involved.
d). In a pure oxygen atmosphere, photochemical production of ozone must involve oxygen photolysis:

$$
\begin{equation*}
\mathrm{O}_{2}+h v \rightarrow \mathrm{O}+\mathrm{O} \tag{i}
\end{equation*}
$$

then

$$
\begin{equation*}
\mathrm{O}+\mathrm{O}_{2} \rightarrow \mathrm{O}_{3} \tag{ii}
\end{equation*}
$$

Photolysis also destroys ozone:

$$
\begin{equation*}
\mathrm{O}_{3}+h v \quad \rightarrow \quad \mathrm{O}_{2}+\mathrm{O} \tag{iii}
\end{equation*}
$$

[Another possible process for ozone destruction is

$$
\begin{equation*}
\mathrm{O}_{3}+\mathrm{O} \quad \rightarrow \quad \mathrm{O}_{2}+\mathrm{O}_{2} \tag{iv}
\end{equation*}
$$

e). From the quoted enthalpies of formation (and that for $\mathrm{O}_{2}$, which is zero by definition), we obtain enthalpies of reaction for (i) and (iii):

$$
\begin{aligned}
& \Delta H^{\circ}{ }_{\text {(i) }}=498 \mathrm{~kJ} \mathrm{~mol}^{-1}=8.27 \times 10^{-19} \mathrm{~J} \text { molecule }^{-1} \\
& \Delta H^{\circ}{ }_{(\mathrm{iii})}=106 \mathrm{~kJ} \mathrm{~mol}^{-1}=1.76 \times 10^{-19} \mathrm{~J} \text { molecule }^{-1} .
\end{aligned}
$$

Now, using $E=h v=h c / \lambda\left(h=6.626 \times 10^{-34} \mathrm{~J} \mathrm{~s} ; c=2.9979 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-1}\right)$, we obtain

$$
\begin{aligned}
& \lambda_{\text {(i) }}=2.40 \times 10^{-7} \mathrm{~m}=240 \mathrm{~nm} \\
& \lambda_{\text {(iii) }}=1.129 \times 10^{-6} \mathrm{~m}=1129 \mathrm{~nm} .
\end{aligned}
$$

These are the longest-wavelength photons possessing sufficient energy to photolyze $\mathrm{O}_{2}$ and $\mathrm{O}_{3}$, respectively [in practice, the efficient photolysis of ozone requires shorter wavelengths than the value suggested, because production of ground-state products is symmetry-forbidden; but that's beyond the scope of this question.]
f). All three of these equilibria involve the formation of a bond of some sort in going from left to right, so the equilibria will lie more to the left at high temperature and more to the right at low temperature.
g). Three hypotheses can be rejected as follows:
i). The notion that Northern hemisphere levels of CFC abundance have lagged behind Southern hemisphere levels is counterintuitive: most industrialization, and most CFC release, is in the North. [In fact, the CFC concentrations in the lower atmosphere are fairly similar over the whole globe: they're mixed pretty thoroughly.]
iii). While it's likely that an increase in water vapour would increase the probability of PSC formation, there's no suggestion in the 'information supplied above' that increased transport of water vapour to the Arctic stratosphere (rather than to the lower atmosphere) is occurring.
iv). The effect of increasing greenhouse gas concentrations (and they are still increasing!) is to decrease the amount of IR reaching the stratosphere. Besides, even though near-infra-red photons possess more energy than the $\mathrm{O}_{2}-\mathrm{O}$ bond strength, they don't actually photolyse ozone.

Hypothesis ii) is the answer which makes the most sense - greenhouse gases will warm the lower atmosphere at the expense of the upper atmosphere. [That's not to say, however, that this mechanism is the true cause - natural chemical systems have a tendency to always be more complex than we expect!]

## PROBLEM 23.

Since $C=65.2 \% \quad H=8.75 \% \quad \Rightarrow \quad O=26.05 \%$
This corresponds to an empirical formula of $\mathrm{C}_{10} \mathrm{H}_{16} \mathrm{O}_{3}$.
The relative molecular mass of this molecule is
$(10 \times 12.01+16 \times 1.008+3 \times 16.00)=120.1+16.13+48=184.13$
Now we are told that the molecular mass of $\mathbf{Q}$ is in the vicinity of 200 so it follows that the empirical formula of $\mathbf{Q}$ is the same as the molecular formula.

$$
\mathrm{C}_{10} \mathrm{H}_{16} \mathrm{O}_{3}
$$

Next the problem tells us that $\mathbf{Q}$ is acidic and we can infer that it might contain $\mathrm{CO}_{2} \mathrm{H}$ groups. If this is so there can only be one group since there are 3 oxygens in total and a $\mathrm{CO}_{2} \mathrm{H}$ group requires 2. This proposal would lead us to believe that $\mathbf{Q}$ is monoprotic. That is to say 1 mole of Q would react with 1 mole of NaOH :

$$
\mathrm{R}-\mathrm{CO}_{2} \mathrm{H}+\mathrm{NaOH} \rightarrow \mathrm{R}-\mathrm{CO}_{2}^{-} \mathrm{Na}^{+}+\mathrm{H}_{2} \mathrm{O}
$$

Now $43.7 \mathrm{mg} \equiv \frac{43.7}{1000} \mathrm{~g}$ of Q react with 23.7 mL of 0.0100 M NaOH .
This is equivalent to $\frac{23.7}{1000} \times 0.0100$ moles of NaOH
So if $\frac{43.7}{1000} \mathrm{~g}$ of Q reacts with $\frac{23.7}{1000} \times 0.0100$ moles of NaOH
$\frac{43.7}{1000} \times \frac{1000}{23.7 \times 0.01} \mathrm{~g}$ Q reacts with 1 mole of NaOH .
i.e. 184.3 g of Q reacts with 1 mole of NaOH .

This proves 1 mole of $\mathbf{Q}$ reacts with 1 mole of NaOH and hence we conclude $\mathbf{Q}$ is a monoprotic acid of the type $\mathrm{R}-\mathrm{CO}_{2} \mathrm{H}$.

Next we need to address the remaining oxygen in $\mathrm{C}_{10} \mathrm{H}_{16} \mathrm{O}_{3}$ (or $\mathrm{C}_{9} \mathrm{H}_{15} \mathrm{O}-\mathrm{CO}_{2} \mathrm{H}$ )
This could be an ether
$\mathrm{R}-\mathrm{O}-\mathrm{R}$
an alcohol
$\mathrm{R}-\mathrm{O}-\mathrm{H}$
a ketone

or an aldehyde

and at this point we cannot choose between these possibilities.
To proceed further we need to look at the double bond equivalents (DBE's) in $\mathbf{Q}$.
Recall that for $\mathrm{C}_{\mathrm{a}} \mathrm{H}_{\mathrm{b}} \mathrm{O}_{\mathrm{c}} \quad$ DBE $=\frac{(2 \mathrm{a}+2)-\mathrm{b}}{2}$

In the case of $\mathbf{Q}, \mathrm{DBE}=\frac{(20+2)-16}{2}=\frac{22-16}{2}=3$
Now clearly two (2) of these DBE have yet to be explained but one (1) is in the


Next we look at the Chemistry of the problem

$$
\mathrm{Q} \xrightarrow{\mathrm{H}_{2} / \mathrm{Pt}} \mathrm{~A} \xrightarrow{\mathrm{NaBH}_{4} / \mathrm{EtOH}} \mathrm{~B} \xrightarrow{\mathrm{H}^{+} / \Delta} \mathrm{C}+\mathrm{H}_{2} \mathrm{O}
$$

$\mathbf{C}$ is an alkene which suggests $B$ is an alcohol, since $\mathbf{B}$ loses water when heated with $\mathrm{H}^{+}$.

Furthermore since $\mathbf{C}$ shows a methyl group attached to a double bond we might expect the chemistry to reflect


If this were correct and so far it looks very promising A must have been a ketone i.e.


You are expected to know that aldehydes and ketones are reduced with $\mathrm{NaBH}_{4}$ to give $1^{\circ}$ and $2^{\circ}$ alcohols respectively.

Now if $\mathbf{A}$ contains a ketone group as well as a carboxylic acid we could think of $\mathbf{A}$ as follows

which now accounts for $\underline{\underline{\mathbf{2}}}$ of the double bond equivalents. One (1) in the carboxylic acid and one (1) in the ketone.

This means that in $\mathbf{Q}$ there is one DBE left to be accounted for and since $\mathbf{Q}$ reacts with hydrogen it means that the remaining functionality must be a double bond.

You are epected to know that carbon-carbon double bonds add hydrogen.
The outstanding problem is to know where to place the double bond in $\mathbf{Q}$ and this becomes evident in the last part of the problem.

We already suspect in principle that

and our hypothesis is confirmed since $\mathbf{C}$ cleaves with ozone and an oxidant to yield acetic acid and a straight chain dicarboxylic acid


$$
\begin{gathered}
\mathrm{O}=\underset{\substack{\mathrm{C} \\
\mathrm{HO}}}{ }\left(\mathrm{CH}_{2}\right)_{6} \mathrm{CO}_{2} \mathrm{H} \\
\end{gathered}
$$

This uniquely defines $\mathbf{C}$ and hence we are certain of $\mathbf{A}$.
$\mathbf{Q}$ we are now certain is simply a molecule which contains a ketone (as does $\mathbf{A}$ ), a carboxylic acid (as does A) and a double bond.

But $\mathbf{Q}$ on ozonolysis and oxidation affords

together with $\mathbf{E}$.
It turns out that we don't need to worry about $\mathbf{E}$ because the small fragment can only come from a molecule of the general type


This uniquely defines $\mathbf{Q}$ as


The only problem remains in the cis/trans isomerisation of the double bond

and this can't be decided on the information given.

## Key Points to Aid Study.

- Degrees of unsaturation (also known as "double bond equivalents").
- Functional groups.
- Reduction.

Ozonolysis with both oxidative and reductive work ups especially for molecules which contain more functionality than simply double bonds.

## PROBLEM 24.

The total solution to the question is as follows



## Notes on the solution

a). Compound B is the expected Birch reduction product.
b). $\quad \mathrm{C}$ being a conjugated isomer of B could be any of the structures $\mathrm{C}-1, \mathrm{C}-2, \mathrm{C}-3$

C-1

C-2

C-3

Of these three structures only two, C-1 and C-2 fit the NMR data. Hence C-3 is discarded at this stage at least as far as the final answer is concerned.
c). Any three Diels Alder products derived from C-1 to C-3 would be acceptable as an answer to part three since they will all contain an intramolecularly bonded hydroxyl. Whilst this is relatively easy to answer the unique solution to the problem requires more thought.

Distinguishing between $\mathrm{C}-1$ and $\mathrm{C}-2$ as the correct answer for C is not possible at this stage of the problem. At the end however it becomes clear that answers which have been generated through either D-1 or D-11, that is the cycloadducts of $\mathrm{C}-1$ are not acceptable since they will not be demethylated with BCl 3 . This reagent at least at -10 o is selective for cleaving methyl ethers peri to a carbonyl; in this regard it is more selective than BBr 3 The full solution, shown above, is worked through for the correct isomer C.


D-1


D-11

However even here there is the possibility of another outcome but not one which can yield chrysophanic acid. The regiochemistry of the cycloaddition shown above is in fact the one found in practice but the Diels Alder reaction could have proceeded to give the alternative isomer as shown below. This would not lead to chrysophanic acid and since this structure was given in the question the student can deduce the answer. However it is worth pointing out that as a synthesis this is not truly unambiguous and could not have been used as a proof of the structure of chrysophanic acid. Given this information it is possible to answer Question d) which really addresses the regiochemistry of the cycloaddition of C-2 and the 5-hydroxynaphthalene-1,4- dione



## Key Points to Aid Study

- Birch reduction or aromatics - no mechanism required.
- Diels-Alder reaction - regiochemistry or the direction of addition.
- Broad concept of nmr. No coupling details are required but rather an appreciation of the information simple NMR data can give the practising chemist.
- Enolisation of ketones.
- Oxidation of phenols to quinones.
- $\quad \mathrm{BCl} 3$ as a selective demethylating agent which demethylates only ethers which are peri to a carbonyl. i.e. to be effective it needs two oxygens, that of the carbonyl and that of the methoxy group to chelate to the boron.
- The stategy to solve road map problems.


## PROBLEM 25.



## Notes on the Solution

At first sight this problem seems very difficult. However the problem is rich in information and tests an understanding of reactions together with a knowledge of simple oxidations, reductions and esterifications. The most difficult part of the problem is setting up the conversion of B to C .


There is no need to have this depth of mechanistic chemistry as the problem gives in its introduction a significant clue as to how this chemistry must work in overall terms.

The oxidation with pyridinium chlorochromate is noteworthy in as much that under anhydrous conditions the primary alcohol is oxidised only to the aldehyde and NOT the carboxylic acid. The reductants hold no special significance and do not need to be learned as special reagents. They simply achieve selective reductions and the nature of these are outlined in the problem.

The conversion of C to D must involve reduction of the methyl ester since D still contains silicon. Had the trimethylsilylethyl ester been reduced the silicon would have been removed. This is a nice challenge for the student to work out and requires no advanced knowledge of the different ester reactivities - it simply follows from the elemental composition.

Finally it is worth noting that this problem uses the symbolism for a Wittig reagent, ie a structure with a formal double bond rather than the more frequently used dipolar structure for the ylid. It is worth noting that reagent $G$ effectively allows one to extend the chain length of an aldehyde.

## Key Points to Aid Study

- Claisen like rearrangements- students may care to look at the rearrangement of the allyl ethers of phenols as another example.
- Oxidation and reduction.
- Esterification with simple and complex alcohols.
- Wittig reactions.
- $\quad \mathrm{E} / \mathrm{Z}$ isomerism and notation.
- Degree of unsaturation (also known as double bond equivalents)


## PROBLEM 26.

## REDUCTIONS

(i)

(ii)

(iii)

(iv)

(v)

(vi)

(Note: XS reductant may reduce the polarised alkene)
(vii)

(viii)


## OXIDATIONS

(ix)

(x)

(xi)

(xii)

(xiii)

(xiv)

(xv)

(xvi)


## OTHER REACTIONS

(xvii)

(xviii) No reaction except at extreme temperatures
(xix)

(xx)

(xxi)


Students should be aware that the outcome of a Wittig reaction i.e. cis/trans isomer may vary with reaction conditions, and reaction/reagent structure.
(xxii)

(xxiii)

(xxiv)

(xxv)

(xxvi)

(xxvii)

(xxviii)



[^0]:    $\ddagger$ For more background information on the starship Enterprise, refer to the WWW sites:
    http://startrek.msn.com/; http://startrek.simplenet.com/startrek/;
    http://www.cs.cityu.edu.hk/~ckmau/engineer.html; or http://public.logica.com/~stepneys/sf/filk/dilithim.htm

[^1]:    $\dagger$ With regard to the continued use of dilithium as the fuel of choice for 24th-century starships, we can only assume that 24th century replicator technology is sufficiently advanced to produce very large quantities of dilithium out of nothingness!

[^2]:    * $0.1=$ dilution factor [ $50 \mathrm{~mL} \mathbf{X}$ diluted to 500 mL , in c )]

